

Inequalities for Martingales, Singular Integral and related topics, A Bibliography

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Abstract

We make an attempt to compile an extensive list of references to literature on inequalities for martingales, singular integrals and related topics, particularly on results related to the Beurling–Ahlfors operator. Despite our efforts, we are absolutely certain that we have missed many references and would be happy to include them if you would inform us about them by sending one of us email.

*Supported in part by NSF Grant # 9700585-DMS

†Supported by the NSF VIGRE program

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