Defect relation for targets of large codimension

A. Eremenko

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Let $f : \mathbf{C} \to \mathbf{P^2}$ be a holomorphic curve and $T(r)$ its Nevanlinna characteristic. For a point $a \in \mathbf{P^2}$, let us define the proximity function

$$m(r, a, f) = \frac{1}{2\pi} \int_0^{2\pi} \log \frac{1}{d(f(re^{it}), a)} dt,$$

where d is the Fubini–Study distance. Then the deficiency is defined in the usual way

$$\delta(a, f) = \liminf_{r \to \infty} \frac{m(r, a, f)}{T(r, f)}.$$

Conjecture. *For every system of points in general position, and every non-constant f, we have*

$$\sum_a \delta(a, f) \le 1.$$

Cartan's Second Fundamental theorem gives $3/2$ instead of 1.