## MA54600: Introduction to Functional Analysis

Instructor: Marius Dadarlat Time: MWF, 12:30pm-1:20pm Location: UNIV 303

## Syllabus:

- 1. Banach spaces
- 2. Hilbert spaces
- 3. Linear Operators and functionals
- 4. The Hahn-Banach Theorem
- 5. Duality
- 6. The Open Mapping Theorem
- 7. The Uniform Boundedness Principle
- 8. Weak Topologies
- 9. Spectra of operators
- 10. Compact operators
- 11. Banach algebras and C\*-algebras
- 12. Riesz calculus
- 13. Fredholm index
- 14. Gelfand transform
- 15. Spectral theorem for normal operators
- If time allows:
- 16. Unbounded Operators
- 17. Applications: Differential operators, Peter-Weyl theorem

Prerequisites: Familiarity with basic measure theory

## Grading:

Attendance 35%, HW 40%, Final Exam 25% (a take-home 36 hours no collaboration exam).

No specific textbook is required. These topics are covered by most books on functional analysis. A good reference is: Gert Pedersen, *Analysis Now*, (Graduate Texts in Mathematics) *Corrected Edition*!