

1. Find the center and radius of the circle with the following equation:

$$3x^2 + 3y^2 + 18x + 6y - 60 = 0.$$

- 1)  $C(3,1), r = \sqrt{30}$
- 2)  $C(3,1), r = 30$
- 3)  $C(-3,-1), r = \sqrt{30}$
- 4)  $C(-3,-1), r = 30$
- 5)  $C(9,3), r = \sqrt{110}$
- 6)  $C(9,3), r = 110$
- 7)  $C(-9,-3), r = \sqrt{110}$
- 8)  $C(-9,-3), r = 110$
- 9) None of the above

2. Hooke's law states that the force  $F$  required to stretch a spring  $x$  units beyond its natural length is directly proportional to  $x$ . A force of 6 pounds stretches a certain spring from its natural length of 20 inches to a length of 22 inches. Find the force that will stretch the spring from its natural length to 29 inches.

- 1) 87 pounds
- 2)  $\frac{58}{3}$  pounds
- 3)  $\frac{29}{3}$  pounds
- 4)  $\frac{87}{11}$  pounds
- 5) 3 pounds
- 6)  $\frac{21}{11}$  pounds
- 7)  $\frac{12}{7}$  pounds
- 8)  $\frac{4}{3}$  pounds
- 9) None of the above

3. Solve for  $x$ . Find all solutions.

$$x^3 - 64 = 0$$

- 1)  $x = 4$
- 2)  $x = -4$
- 3)  $x = -4, 4$
- 4)  $x = -2 \pm 2\sqrt{3}i$
- 5)  $x = 4, -2 \pm 2\sqrt{3}i$
- 6)  $x = -4, -2 \pm 2\sqrt{3}i$
- 7)  $x = -2 \pm 4\sqrt{3}i$
- 8)  $x = 4, -2 \pm 4\sqrt{3}i$
- 9)  $x = -4, -2 \pm 4\sqrt{3}i$

4. Given  $f(x) = x^2 - 4$  and  $g(x) = \sqrt{x+2}$ , find  $(g \circ f)(7)$ .

- 1) 5
- 2)  $\sqrt{5}$
- 3) 45
- 4)  $\sqrt{45}$
- 5) 47
- 6)  $\sqrt{47}$
- 7)  $\sqrt{77}$
- 8) 77
- 9) None of the above

5. Find the domain of the function  $f(x) = \frac{1}{\sqrt{x^2 - 5x - 14}}$ .

- 1)  $(-\infty, -2] \cup [7, \infty)$
- 2)  $[-2, \infty)$
- 3)  $[-2, 7]$
- 4)  $[7, \infty)$
- 5)  $(-\infty, -2) \cup (7, \infty)$
- 6)  $(-2, \infty)$
- 7)  $(-2, 7)$
- 8)  $(7, \infty)$
- 9) None of the above

6. Solve the inequality.

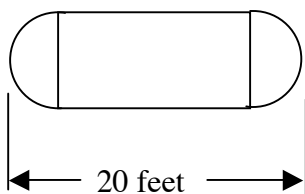
$$|x + 6| + 17 \geq 25$$

- 1)  $(-14, 2)$
- 2)  $[-14, 2]$
- 3)  $[-14, \infty)$
- 4)  $(-\infty, \infty)$
- 5)  $(-\infty, -48] \cup [2, \infty)$
- 6)  $[2, \infty)$
- 7)  $[-48, 2]$
- 8)  $(-48, 2)$
- 9) None of the above

7. If an object is projected vertically upward from ground level with an initial velocity of 150 meters per second, then its height in meters,  $s$ , above the ground after  $t$  seconds is given by  $s = -10t^2 + 150t$ . For what values of  $t$  will the object be more than 440 meters above the ground?

- 1)  $4 < t < 7.5$  seconds
- 2)  $4 < t < 11$  seconds
- 3)  $7.5 < t < 11$  seconds
- 4)  $7.5 < t < 15$  seconds
- 5)  $t > 4$  seconds
- 6)  $t > 7.5$  seconds
- 7)  $t > 11$  seconds
- 8)  $t > 15$  seconds
- 9) None of the above

8. A three-dimensional storage tank is to be constructed in the shape of a right circular cylinder with a hemisphere attached to each end of the cylinder. The length of the tank is to be 20 feet. If  $r$  denotes the radius of the hemispheres, find a formula for the volume of the tank.



- 1)  $V = 20\pi r^2 - \frac{1}{3}\pi r^3$
- 2)  $V = 20\pi r^2 + \frac{1}{3}\pi r^3$
- 3)  $V = 20\pi r^2 - \frac{2}{3}\pi r^3$
- 4)  $V = 20\pi r^2 + \frac{2}{3}\pi r^3$
- 5)  $V = 20\pi r^2 - \frac{4}{3}\pi r^3$
- 6)  $V = 20\pi r^2 + \frac{4}{3}\pi r^3$
- 7)  $V = 20\pi r^2 - \frac{8}{3}\pi r^3$
- 8)  $V = 20\pi r^2 + \frac{8}{3}\pi r^3$
- 9) None of the above

9. Find all the points on the  $y$ -axis that are a distance 13 from the point  $(5, -3)$ .

- 1)  $(0,1)$  and  $(0,-7)$
- 2)  $(0,1)$
- 3)  $(0,-7)$
- 4)  $(0,3\sqrt{15})$  and  $(0,-3\sqrt{15})$
- 5)  $(0,3\sqrt{15})$
- 6)  $(0,-3\sqrt{15})$
- 7)  $(0,9)$  and  $(0,-15)$
- 8)  $(0,9)$
- 9)  $(0,-15)$

10. Let  $f(x) = \frac{3}{x}$ . Simplify the difference quotient  $\frac{f(x+h) - f(x)}{h}$ , where  $h \neq 0$ .

1)  $\frac{3}{h}$

2)  $\frac{3}{h^2}$

3)  $\frac{3-3h}{xh^2}$

4)  $-\frac{3h^2}{x(x+h)}$

5)  $\frac{3h^2}{x(x+h)}$

6)  $-\frac{3h}{x(x+h)}$

7)  $\frac{3h}{x(x+h)}$

8)  $-\frac{3}{x(x+h)}$

9)  $\frac{3}{x(x+h)}$

11. Consider  $g(x) = \frac{9x}{x+9}$ . Find  $g(\sqrt{a})$ , given that  $a$  is a positive real number. Simplify your answer.

1)  $\frac{9(a-9\sqrt{a})}{a+9}$

2)  $\frac{3(a-3\sqrt{a})}{a+9}$

3)  $\frac{3\sqrt{a^2+9a}}{a+9}$

4)  $\frac{9(a-9\sqrt{a})}{a-81}$

5)  $\frac{3(a-3\sqrt{a})}{a-81}$

6)  $\frac{3\sqrt{a^2+9a}}{a-81}$

7)  $\frac{9(a-9\sqrt{a})}{a-9}$

8)  $\frac{3(a-3\sqrt{a})}{a-9}$

9)  $\frac{3\sqrt{a^2+9a}}{a-9}$

12. A music CD sells for \$15. The musician receives 10% of the selling price as a royalty for each copy of the CD sold up to 1000 copies. For any additional copies sold beyond 1000, the musician receives 20% of the selling price as a royalty. Find a piece-wise defined function  $R$  that gives the total amount of royalties earned by the musician if  $x$  copies of the CD are sold.

$$1) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 4.5x + 1500 & \text{if } x > 1000 \end{cases}$$

$$2) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 4.5x & \text{if } x > 1000 \end{cases}$$

$$3) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 4.5x - 1500 & \text{if } x > 1000 \end{cases}$$

$$4) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 4.5x - 3000 & \text{if } x > 1000 \end{cases}$$

$$5) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 3x + 3000 & \text{if } x > 1000 \end{cases}$$

$$6) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 3x + 1500 & \text{if } x > 1000 \end{cases}$$

$$7) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 3x & \text{if } x > 1000 \end{cases}$$

$$8) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 3x - 1500 & \text{if } x > 1000 \end{cases}$$

$$9) R(x) = \begin{cases} 1.5x & \text{if } 0 \leq x \leq 1000 \\ 3x - 3000 & \text{if } x > 1000 \end{cases}$$

13. Given the graph of  $y = f(x)$ , the graph of  $g(x) = 2f(x) - 5$  can be obtained by using graphical transformations applied to the graph of  $f$ . Which of the following sequences of transformations is correct?

- 1) shift right 5 units, then vertical stretch by factor 2
- 2) vertical stretch by factor 2, then shift right 5 units
- 3) shift down 5 units, then vertical stretch by factor 2
- 4) vertical stretch by factor 2, then shift down 5 units
- 5) shift right 5 units, then horizontal stretch by factor 2
- 6) horizontal stretch by factor 2, then shift right 5 units
- 7) shift down 5 units, then horizontal stretch by factor 2
- 8) horizontal stretch by factor 2, then shift down 5 units
- 9) None of the above

14. Find an equation of the perpendicular bisector of the segment  $AB$  with points  $A(0,0)$  and  $B(6,4)$ .

1)  $y = -\frac{3}{2}x$

2)  $y = -\frac{2}{3}x$

3)  $y = \frac{2}{3}x$

4)  $y - 4 = -\frac{3}{2}(x - 6)$

5)  $y - 4 = -\frac{2}{3}(x - 6)$

6)  $y - 4 = \frac{2}{3}(x - 6)$

7)  $y - 2 = -\frac{3}{2}(x - 3)$

8)  $y - 2 = -\frac{2}{3}(x - 3)$

9)  $y - 2 = \frac{2}{3}(x - 3)$

15. Find an equation of a rational function,  $f$ , that satisfies the given conditions.

no zeros

vertical asymptote:  $x = -1$

horizontal asymptote:  $y = 0$

$f(1) = 2$

$f(x) > 0$ :  $(-\infty, -1) \cup (-1, \infty)$

$f(x) < 0$ : none

1)  $f(x) = \frac{16}{x+1}$

2)  $f(x) = \frac{8}{x+1}$

3)  $f(x) = \frac{4}{x+1}$

4)  $f(x) = \frac{16}{(x+1)^2}$

5)  $f(x) = \frac{8}{(x+1)^2}$

6)  $f(x) = \frac{4}{(x+1)^2}$

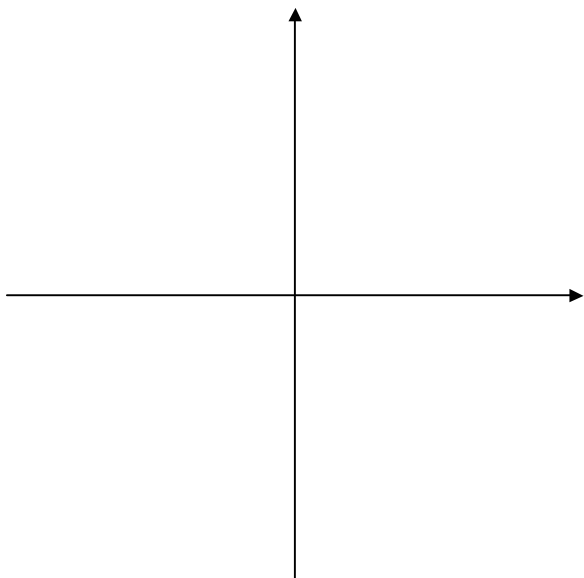
7)  $f(x) = \frac{16}{(x+1)^3}$

8)  $f(x) = \frac{8}{(x+1)^3}$

9)  $f(x) = \frac{4}{(x+1)^3}$

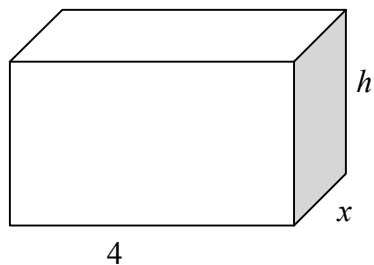
16. Which of the following are true of the function  $f(x) = -3x^2 - 6x - 6$ ?

- I. A zero of  $f$  is  $-2$ .
- II.  $f$  has a  $y$ -intercept at  $(0, 6)$ .
- III. The minimum value of  $f$  is  $-1$ .



- 1) I only
- 2) II only
- 3) III only
- 4) I and II only
- 5) I and III only
- 6) II and III only
- 7) I, II, and III
- 8) Cannot be determined
- 9) None of the above

17. A closed rectangular box has a volume of 20 cubic inches. The length of the box is 4 inches. If  $x$  denotes the width of the box (in inches) and  $h$  denotes the height of the box (in inches), express the surface area of the box,  $S$ , as a function of  $x$ .



- 1)  $S(x) = 40 + \frac{160}{x} + 8x$
- 2)  $S(x) = 10 + \frac{40}{x} + 8x$
- 3)  $S(x) = 10 + \frac{40}{x} + 4x$
- 4)  $S(x) = \frac{40}{x} + 8x$
- 5)  $S(x) = 18x + 40$
- 6)  $S(x) = 4x^2$
- 7)  $S(x) = 2x^2 + 16x$
- 8)  $S(x) = 2x^2 + 12x$
- 9)  $S(x) = 4x \left( \frac{10 - 4x}{x + 4} \right)$

18. Which of the following are true of the function  $f(x) = \frac{x^2}{x^2 - 4}$  ?

- I. The range of the function is  $(-\infty, 0] \cup (1, \infty)$
- II.  $f$  has a  $x$  - intercept at  $(2, 0)$
- III. The graph of  $f$  is decreasing on the interval  $(-2, 0]$

- 1) I
- 2) II
- 3) III
- 4) I and II
- 5) I and III
- 6) II and III
- 7) I, II, and III
- 8) Cannot be determined
- 9) None of the above

19. Find the maximum vertical distance between the graphs of  $y_1 = -x^2 + 4x$  and  $y_2 = x$ , when  $0 \leq x \leq 3$ .

- 1) 3
- 2) 2.75
- 3) 2.50
- 4) 2.25
- 5) 2
- 6) 1.75
- 7) 1.50
- 8) 1.25
- 9) 1