

Name \_\_\_\_\_

1. Prove that for all sets  $A$  and  $B$ ,  $A \subseteq B$  if and only if  $A \cup (B - A) = B$ .

2. Show that if  $F : A \rightarrow B$ ,  $G : B \rightarrow A$  and  $F \circ G = i_B$  then  $F$  maps  $A$  onto  $B$  and  $G$  is 1 - 1.

3. Calculate each of the following:

(a)  $\bigcap_{n \in \mathbb{Z}^+} [0, 1/n]$

(b)  $\bigcup \{(a, b) \mid (a, b) \subseteq [1, 2]\}$

4. (a) Prove that if  $R$  is a linear ordering relation then so is  $R^{-1}$ .

(b) Give an example of a relation  $R$  which is a well-ordering relation but  $R^{-1}$  is not.

5. Find two sets  $X$  and  $Y$  such that  $X \approx Y$  but  
 $(X - Y) \neq (Y - X)$ .