

1) If  $f(x) = 5x^2 - 3$  and  $g(x) = 2x + 3$ , find  $g[f(x)]$ .

- A.  $10x^2$
- B.  $20x^2 + 60x + 42$
- C.  $10x^2 - 3$
- D.  $20x^2 + 42$
- E.  $10x^2 + 30x + 21$

2) Find  $f'(x)$  or the derivative of  $f$ , if  $f(x) = (4x^4 - 7x^2 + 2)^3$ . (Write answer completely factored.)

- A.  $f'(x) = 6x(8x^2 - 7)(4x^4 - 7x^2 + 2)^2$
- B.  $f'(x) = 3(16x^3 - 14x)^2$
- C.  $f'(x) = 3x(8x^2 - 7)(4x^4 - 7x^2 + 2)^2$
- D.  $f'(x) = 3(4x^4 - 7x^2 + 2)^2$
- E.  $f'(x) = 6x(8x^2 - 7)(4x^4 - 7x^2 + 2)$

3) Find the derivative of the function below. (Completely factor the derivative.)

$$y = -4x(2x^2 - 3)^5$$

- A.  $-4(2x^2 - 3)^4(20x^2 + 2x - 3)$
- B.  $(2x^2 - 3)^4(1 - 80x^2)$
- C.  $-4(2x^2 - 3)(22x^2 - 3)$
- D.  $-4(2x^2 - 3)^4(22x^2 - 3)$
- E.  $15360x^2(2x^2 + 3)^4$

4) If  $f(x) = e^{-x}(\ln x)$ , find  $f'(x)$  when  $x = 1$ .

- A. 0
- B.  $f'(1)$  does not exist.
- C.  $\frac{2}{e}$
- D.  $e$
- E.  $\frac{1}{e}$

5) Solve the equation below. Then, select the correct choice that describes the solution.

$$32^{2x-3} = 16^{x+1}$$

- A. The solution is greater than 3.
- B. The solution is less than 0.
- C. The solution is greater than 0, but less than 1.
- D. The solution is greater than 1, but less than 2.
- E. The solution is greater than 2, but less than 3.

6) Which statement(s) in the box below is(are) true?

- I  $\log_3 9 = 2$  is equivalent to  $3^2 = 9$ .
- II  $\ln 21$  is approximately 1.322.
- III  $\log_b 50 = \log_b 5 + \log_b 10$ .

- A. I and III only.
- B. III only.
- C. II and III only.
- D. I and II only.
- E. None are true.

- 7) Julie deposits \$1500 in an account that earns a 3% interest rate compounded quarterly. If she leaves the money to grow, how much **interest** has the account earned in 8 years? Round to the nearest dollar. (See the formulas on the cover sheet.)

- A. \$92
- B. \$405
- C. \$46
- D. \$140
- E. None of the above.

- 8) If  $\log_2 32 = a$ ,  $\log_2 3 = b$ , and  $\log_2 7 = c$ , find an expression to represent  $\log_2 \left( \frac{21}{32} \right)$ .

- A.  $bc - a$
- B.  $a - b - c$
- C.  $\frac{bc}{a}$
- D.  $b + c - a$
- E.  $-abc$

- 9) Approximate the solution of this equation (rounded to 3 decimal places).

$$2^x = 11$$

- A. 0.289
- B. 3.317
- C. 3.091
- D. 1.662
- E. 3.459

- 10) Find the derivative of the function below. Factor your answer.

$$y = \ln(x^2 + 24x)$$

A.  $y' = \frac{x+12}{x(x+24)}$

B.  $y' = \frac{2(x+12)}{x(x+24)}$

C.  $y' = \frac{x+12}{x+24}$

D.  $y' = \frac{1}{x^2} + \frac{1}{24x}$

E.  $y' = \frac{1}{x(x+24)}$

- 11) Find the derivative of function  $f$  given below.

$$f(x) = \frac{e^x}{3 \ln x}$$

A.  $f'(x) = \frac{e^x \left( \ln x^3 - \frac{1}{x^3} \right)}{9(\ln x)^2}$

B.  $f'(x) = \frac{e^x \left( \frac{1}{x} - 1 \right)}{3(\ln x)^2}$

C.  $f'(x) = \frac{e^x (\ln x - 1)}{3(\ln x)^2}$

D.  $f'(x) = \frac{xe^x}{3}$

E.  $f'(x) = \frac{e^x \left( \ln x - \frac{1}{x} \right)}{3(\ln x)^2}$

12) Find the value of  $x$  where the tangent to the graph of  $y = xe^{-x}$  is horizontal.

- A. 0
- B.  $\frac{1}{e}$
- C.  $-\frac{1}{e}$
- D. 1
- E. -1

13) Given: function  $y = xe^x$ , with first derivative  $\frac{dy}{dx} = xe^x + e^x$  and second derivative

$$\frac{d^2y}{dx^2} = xe^x + 2e^x.$$

Which of the following statements is(are) true?

- I The function is increasing on the interval  $(-1, \infty)$ .
- II The function is concave upward on the interval  $(-2, \infty)$ .
- III The function is decreasing on the interval  $(-\infty, 2)$ .
- IV There is no interval where the function is concave downward.

- A. II and III only
- B. I and II only
- C. I only
- D. I, III, and IV only
- E. I and IV only

- 14) Which statement below is true about the graph of the function  $f(x) = \frac{x^2 + 4}{2 + 7x - 4x^2}$ ?
- A. The line  $x = 1$  is a vertical asymptote.
  - B. The line  $y = \frac{1}{4}$  is a horizontal asymptote.
  - C. The line  $x = -\frac{1}{4}$  is a vertical asymptote.
  - D. The graph has no vertical or horizontal asymptotes.
  - E. The line  $y = 2$  is a horizontal asymptote.

- 15) Find the second derivative of  $y = e^x(x-1)^2$ .

- A.  $e^x(x-1)^2$
- B.  $e^x(x^2 + 2x - 1)$
- C.  $e^x(x^2 - 2x - 1)$
- D.  $2e^x(x-1)$
- E.  $2e^x$