**Submitting HW Tips** 

HW # 9

**1** Verify that 
$$\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^2 & b^2 & c^2 \end{vmatrix} = (b-a)(c-a)(c-b).$$

(This is the Vandermonde Determinant, which is used in MA 366/266/303/265/520 and elsewhere.)

**2** Let 
$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 2 & 1 \\ 0 & 2 & 4 & 2 \\ 3 & 5 & 2 & 1 \end{bmatrix}$$
, where  $|A| = 10$ . For the system  $A\mathbf{x} = \mathbf{b}$ , use **Cramer's Rule**  
to compute  $x_2$  when  $\mathbf{b} = \begin{bmatrix} 2 \\ 0 \\ 1 \\ -1 \end{bmatrix}$ .

**3** Let 
$$A = \begin{bmatrix} 5 & -1 & 0 \\ 3 & 2 & 1 \\ 7 & 5 & 2 \end{bmatrix}$$
, compute  $(A^{-1})_{12} + (A^{-1})_{22}$ .

**4 TRUE/FALSE Questions**: Page 279: #5.5, 5.6.

**5** Find all eigenvalues and a basis for each eigenspace of A, where  $A = \begin{bmatrix} 6 & 1 \\ 4 & 9 \end{bmatrix}$ .

**6** If  $A = \begin{bmatrix} 6 & 1 \\ 4 & 9 \end{bmatrix}$  (see above problem), then compute  $A^{20}\mathbf{u}$ , where  $\mathbf{u} = \begin{bmatrix} 1 \\ 4 \end{bmatrix}$ .