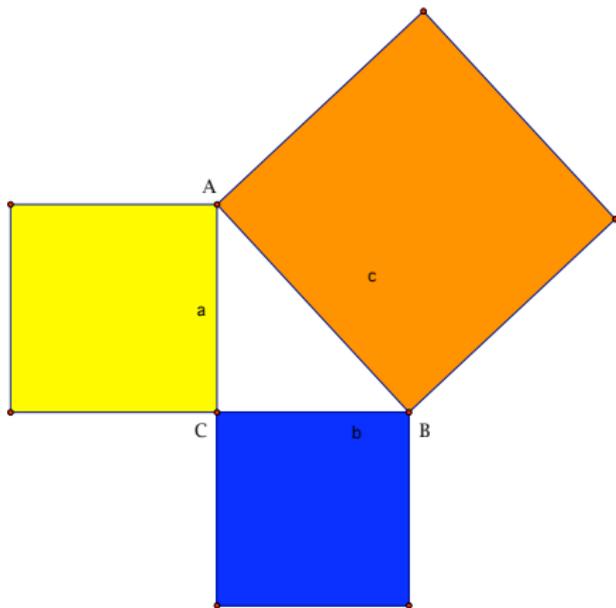


# Theorem 9: (Pythagorean Theorem)

*In a right triangle the sum of the squares of the legs equals the square of the hypotenuse.*

Pythagorean  
Theorem

**Note:** This is a statement about area:

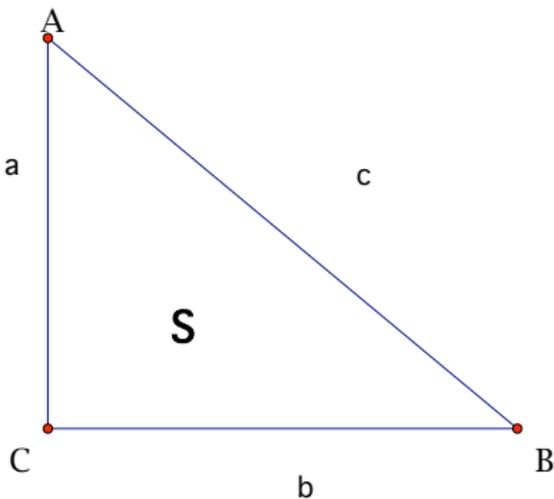


## Sketch of proof:

Let  $\triangle ABC$  have  $\angle BCA$  as a right angle. Let  $a = AC$ ,  $b = BC$ , and  $c = AB$ . We need to show  $a^2 + b^2 = c^2$ . Let  $S = \text{area}(\triangle ABC)$ .

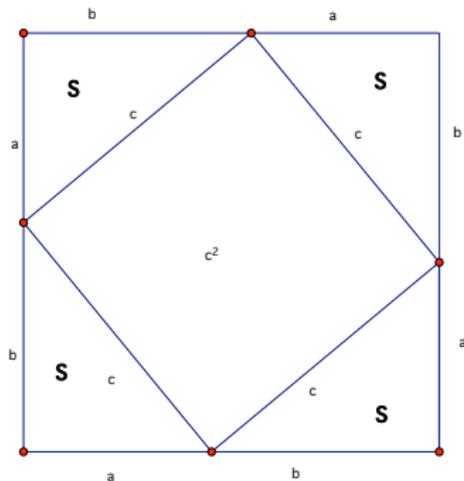
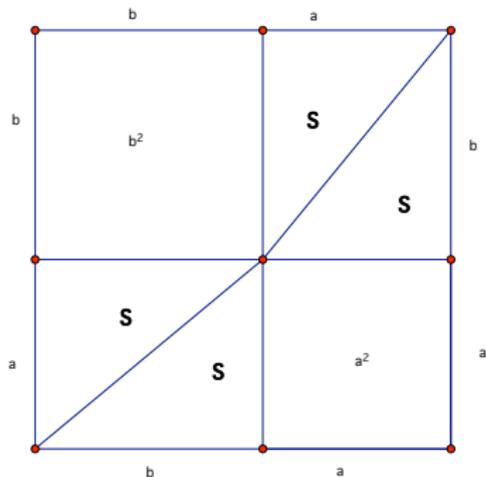
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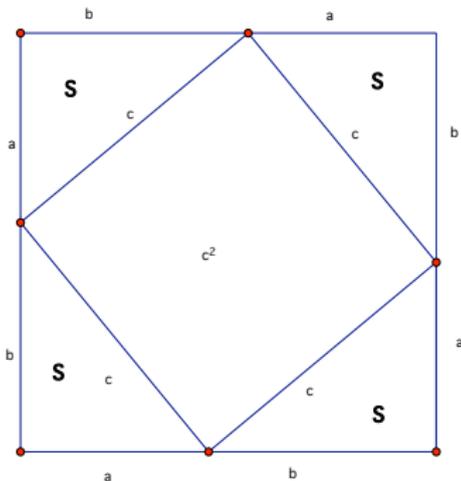
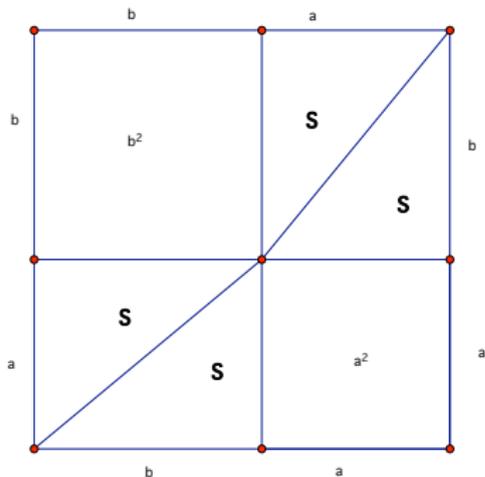


Consider a square of side  $a + b$ , and subdivide the square in two ways:

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On the left we see the area of the square is  $a^2 + b^2 + 4S$ , while on the right we have the area as  $c^2 + 4S$ . Thus,  $a^2 + b^2 = c^2$ . This is the claim.  $\square$