

show how  $\omega_*: \pi_1(G) \rightarrow \pi_1(X)$  completely determines the lifting problem for coverings of  $X$  and how  $\hat{\omega}^*: H^2(X) \rightarrow H^2(G \times X)$  completely determines the principal torus bundle lifting problem for compact Lie groups. We shall show how  $\hat{\omega}^*$  and  $i^*$  on singular cohomology determine liftings up to homotopy for  $n$ -connective coverings and stages of Postnikov systems respectively.

Finally we shall use theorem 1 to study the "equivariantization" problem. That is, given a map  $f: Y \rightarrow X$  and an action of  $G$  on  $X$ , is it possible to find a homotopy equivalent map  $f': Y' \rightarrow X$  which can be made equivariant? We shall study actions in which only equivariant maps must be homotopy equivalent to product space projections. We shall show that a cononical action of  $G$  on  $X_G$ , which extends a given action of  $G$  on  $X$ , has the property that every map into  $X_G$  is "equivariantizable".

We shall mention here the result for the principal torus bundle lifting problem alluded to in the penultimate paragraph above. First, recall that a principal torus bundle  $T \rightarrow E \rightarrow X$  is classified by a characteristic class  $k \in H^2(X; Z^n)$  where  $Z^n$  is the direct sum of  $Z$   $n$ -times where  $n$  is the dimension of the torus  $T$ . We shall assume that  $G$  is a connected compact Lie group with action  $\hat{\omega}: G \times X \rightarrow X$ .