

$\bar{p}: N/i_*(A) \rightarrow \pi_1(B_G)$ is induced by $p_*: \pi_1(X_G) \rightarrow \pi_1(B_G)$:

a) $\omega_*(\pi_1(G)) \subset A$

b) $\bar{p}: N/i_*(A) \rightarrow \pi_1(B_G)$ has a cross-section.

We will display two immediate corollaries, the first one appears in [4], the second may be new. Of course both have direct proofs.

Corollary 10: If G acts on X with a fixed point, then G lifts to the universal covering.

Proof: This follows from theorem 5'. The existence of the fixed point makes ω homotopic to a constant and gives rise to a cross-section in the bundle $X \rightarrow X_G \rightarrow B_G$. These two facts insure that conditions a and b are met.

Corollary 11: Suppose G is connected and the covering $\tilde{X} \rightarrow X$ corresponds to the subgroup $A \subset \pi_1(X)$. Then G lifts if and only if $\omega_*(\pi_1(G)) \subset A$.

Proof: Since G is connected, $\pi_1(B_G) = 0$ and condition b of theorem 5" is always satisfied.

Now Corollary 11 shows that if $\omega_*: \pi_1(G) \rightarrow \pi_1(X)$ is trivial, a connected G action will lift to any covering. Thus we always get a lifting if $\pi_1(X)$ has a trivial center,