

the remark about $\omega_* = 0$ for universal coverings to n -connective coverings. Given an $(n-1)$ -connected space X on which G acts, we say X has an equivariant n -connected covering if G lifts to an n -connective covering.

Proposition 13: An $(n-1)$ -connected X on which a connected G acts has an equivariant n -connective covering if and only if $\omega^*(k) = 0$ where $k \in H^n(X; \pi_n(X))$ classifies the n -connective covering.

Proof: We use Proposition 12 and the fact that if X is n -connected, then

$$H^n(G) \xrightarrow{\omega^*} H^n(X) \xrightarrow{i^*} H^n(X_G)$$

is exact for any coefficients. This fact follows by considering the commutative diagram of spectral sequences arising from the commutative square.

$$\begin{array}{ccc} G & \xrightarrow{\omega} & X \\ \downarrow & & \downarrow \\ E_G & \rightarrow & X_G \\ \downarrow & & \downarrow \\ B_G & \xrightarrow{1} & B_G \end{array}$$

A similar argument was made in [10, theorem 4] where G was replaced by the space of homotopy equivalences.