

Now define $\alpha: (X_G)_G \rightarrow B_G \times X_G$ by $\alpha(\langle e, e', x \rangle_G) = \langle e \rangle_G \times \langle e \cdot e', x \rangle_G$ and let $\beta: B_G \times X_G \rightarrow (X_G)_G$ be defined by $\beta(\langle e \rangle_G \times \langle e', x \rangle_G) = \langle e, e^{-1} \cdot e', x \rangle_G$. Then α and β are well defined and $\alpha\beta = \text{identity}$ and $\beta\alpha = \text{identity}$. Hence $\alpha: (X_G)_G \rightarrow B_G \times X_G$ is a homeomorphism.