

Homework Set # 8

1. (§4.2) Page 234: # 13.
  2. An object travels along the path  $\mathbf{c}(t) = (t, \frac{2}{3}t^{\frac{3}{2}})$ , for  $0 \leq t \leq 1$ . Find the arc length function  $s(t)$  and use it to reparameterize the path so that the object's speed is a constant 1 unit/sec for all  $t$ .
  3. (§4.3) Page 243: # 5, 9, 16, 21.
  4. Given that  $\mathbf{F}(x, y) = \left( \{1 + 2x \ln y\}, \left\{ \frac{x^2}{y} + 2y \right\} \right) = \nabla\phi(x, y)$ , find the potential function  $\phi(x, y)$  which satisfies  $\phi(-1, 1) = 4$ .
  5. (§4.4) Page 258: # 2, 3, 14, 24.
  6. Prove the **Basic Identity** #11 on Page 255:  
If  $f : U \subset \mathbb{R}^3 \rightarrow \mathbb{R}$  is of class  $C^2$ , prove that  $\nabla \times (\nabla f) = \mathbf{0}$ .
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