

1. Huntington Bank offers an account that pays 3%, compounded daily. Lafayette Bank offers an account with the same annual effective rate, but compounded twice a year. Lafayette Bank's nominal interest rate is  $i\%$  per year, compounded twice a year. Find  $i$ .

$$\begin{aligned} > AEF := \left(1 + \frac{.03}{365}\right)^{365}; \\ & AEF := 1.030453346 \end{aligned} \tag{1}$$

$$\begin{aligned} > 2 \cdot \left(AEF^{\frac{1}{2}} - 1\right); \\ & 0.030224958 \end{aligned} \tag{2}$$

2) You receive an award that pays \$1,000 at the beginning of year 0, \$2,000 at the beginning of year 1, and \$3,000 at the beginning of year 2. What is the present value of this award at 5% interest per year?

$$\begin{aligned} > i := .05; \\ & i := 0.05 \end{aligned} \tag{3}$$

$$\begin{aligned} > 1000 + (1 + i)^{-1} \cdot 2000 + (1 + i)^{-2} \cdot 3000 \\ & 5625.850341 \end{aligned} \tag{4}$$

3) You borrow \$250,000 to buy a house. Compute the monthly payments on a 25 year loan at 5% interest, compounded monthly?

$$\begin{aligned} > i := \frac{.05}{12}; \\ & i := 0.004166666667 \end{aligned} \tag{6}$$

$$\begin{aligned} > \text{solve}\left((1 + i)^{25 \cdot 12} \cdot 250000 - \frac{P \cdot ((1 + i)^{25 \cdot 12} - 1)}{i} = 0, P\right); \\ & 1461.475045 \end{aligned} \tag{7}$$

4) On Jan. 1, 2007, you won a contest that pays \$400 dollars at the end of each month for the next 10 years together with an additional payment of \$100,000 at the end of the last month. Find the present value on Jan. 1, 2007 of this prize at 3% interest, compounded monthly?

$$\begin{aligned} > i := \frac{.03}{12}; \\ & i := 0.002500000000 \end{aligned} \tag{8}$$

$$\begin{aligned} > FV := 100000 + \frac{400 \cdot ((1 + i)^{10 \cdot 12} - 1)}{i}; \\ & FV := 1.558965675 \cdot 10^5 \end{aligned} \tag{9}$$

$$\begin{aligned} > PV := FV \cdot (1 + i)^{-10 \cdot 12}; \\ & PV := 1.155342629 \cdot 10^5 \end{aligned} \tag{10}$$

5) Bob Roarman will sell you a slightly used car for \$5,000 cash or you can buy the same car for 48 payments of only \$135 each (made at the end of each month). What rate of interest is Bob charging? Hint: Try each answer.

6) What is the least amount I can have in my retirement fund to allow me to withdraw \$500 a month at the end of each month for the next 30 years, assuming that my fund earns 4% interest, compounded monthly?

$$\begin{aligned} > i := \frac{.04}{12}; \\ & \hspace{15em} i := 0.0033333333333333 \end{aligned} \tag{11}$$

$$\begin{aligned} > solve\left( (1+i)^{30 \cdot 12} \cdot B - \frac{500 \cdot ((1+i)^{30 \cdot 12} - 1)}{i} = 0, B \right); \\ & \hspace{15em} 1.047306148 \cdot 10^5 \end{aligned} \tag{12}$$

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7) I borrow \$100,000 for 20 years at 5% interest per year with annual payments of \$8,024.25 made at the end of the year. What do I still owe immediately after the 5th payment?

$$\begin{aligned} > i := .05; \\ & \hspace{15em} i := 0.05 \end{aligned} \tag{13}$$

$$\begin{aligned} > PP := 8024.25; \\ & \hspace{15em} PP := 8024.25 \end{aligned} \tag{14}$$

$$\begin{aligned} > BB := (1+i)^5 \cdot 100000 - \frac{PP \cdot ((1+i)^5 - 1)}{i}; \\ & \hspace{15em} BB := 83289.10972 \end{aligned} \tag{15}$$

8) In problem 7, immediately after the 5th payment, I refinance the loan at 4% interest per year. Assuming that the answer to Problem 7 is \$50,000 (which is not correct), find the new annual payment.

$$\begin{aligned} > i := .04; \\ & \hspace{15em} i := 0.04 \end{aligned} \tag{16}$$

$$\begin{aligned} > PP2 := solve\left( (1+i)^{15} \cdot 50000 - \frac{P \cdot ((1+i)^{15} - 1)}{i} = 0, P \right); \\ & \hspace{15em} PP2 := 4497.055017 \end{aligned} \tag{17}$$

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