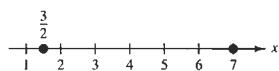
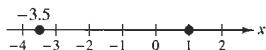
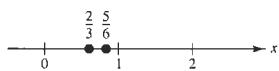
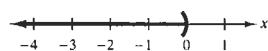
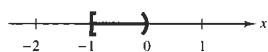


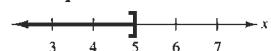
## Answers to Warm Ups, Odd-Numbered Exercises, Quizzes, and Tests

### Chapter R1

#### Section R1.1 (page R8)

1. (a) Natural:  $\{5\}$ (b) Integer:  $\{-9, 5\}$ (c) Rational:  $\{-9, -\frac{7}{2}, 5, \frac{2}{3}, 0.1\}$ (d) Irrational:  $\{\sqrt{2}\}$ 3. (a) Natural:  $\{12, 1, \sqrt{4}\}$  (Note:  $\sqrt{4} = 2$ )(b) Integer:  $\{12, -13, 1, \sqrt{4}\}$ (c) Rational:  $\{12, -13, 1, \sqrt{4}, \frac{3}{2}\}$ (d) Irrational:  $\{\sqrt{6}\}$ 5. (a) Natural:  $\{\frac{8}{2}, 9\}$  (Note:  $\frac{8}{2} = 4$ )(b) Integer:  $\{\frac{8}{2}, -4, 9\}$ (c) Rational:  $\{\frac{8}{2}, -\frac{8}{3}, -4, 9, 14.2\}$ (d) Irrational:  $\{\sqrt{10}\}$ 7. 0.625    9.  $0.\overline{54}$     11.  $-1 < 2.5$ 13.  $\frac{3}{2} < 7$ 15.  $-3.5 < 1$ 17.  $\frac{5}{6} > \frac{2}{3}$ 19.  $\frac{127}{90}, \frac{584}{413}, \frac{7071}{5000}, \sqrt{2}, \frac{47}{33}$ 21.  $x < 0$  denotes all negative real numbers.25.  $x > 3$  denotes all real numbers greater than 3.29.  $-1 \leq x < 0$  denotes all real numbers greater than or equal to  $-1$  and less than 0.31.  $x < 0$     33.  $A \geq 35$  years

37. 10    39. -6    41. -9

23.  $x \leq 5$  denotes all real numbers less than or equal to 5.27.  $-2 < x < 2$  denotes all real numbers greater than  $-2$  and less than 2.35.  $3.5\% \leq r \leq 6\%$ 43. -1    45.  $\pi - 3$ 47.  $|-7| = |7|$     49.  $|-3| > -|-3|$ 51.  $-|-2| = -|2|$     53. 4    55.  $\frac{5}{2}$     57.  $\frac{7}{2}$ 59. 51    61.  $\frac{128}{75}$     63.  $|z - \frac{3}{2}| > 1$ 65.  $|x + 10| \geq 6$     67.  $|y - 0| \geq 6 \Rightarrow |y| \geq 6$ 69. 179 miles    71.  $37^\circ$ 

$ a - b $	0.05b	Passes Budget Variance Test
-----------	-------	-----------------------------

73. \$127.88    \$1250    Yes

75. \$572.59    \$470    No

77. \$671.75    \$1882    No

$ a - b $	0.002b	Passes Quality Control Test
-----------	--------	-----------------------------

79. 0.02    0.03    Yes

81. 0.045    0.033    No

83. 0.035    0.036    No

85. (a) No. If  $u > 0$  and  $v < 0$  or  $u < 0$  and  $v > 0$ , then  $|u + v| \neq |u| + |v|$ .(b) Yes. If the signs of  $u$  and  $v$  are different, then  $|u + v| < |u| + |v|$ .

87. Answers will vary. Example: The set of natural numbers includes only the integers greater than zero. The set of integers include all numbers that have no fractional or decimal parts. The set of rational numbers includes all numbers that can be written as the quotient of two integers. Any real number that is not a rational number is in the set of irrational numbers.

#### Section R1.2 (page R18)

##### Warm Up (page R18)

1.  $-4 < -2$     2.  $0 > -3$     3.  $\sqrt{3} > 1.73$ 4.  $-\pi < -3$     5.  $|6 - 4| = 2$     6.  $|2 - (-2)| = 4$ 7.  $|0 - (-5)| = 5$     8.  $|3 - (-1)| = 4$ 9.  $|-7| + |7| = 7 + 7 = 14$ 10.  $-|8 - 10| = -|-2| = -2$ 1.  $7x, 4$     3.  $x^2, -4x, 8$     5.  $2x^2, -9x, 13$     7.  $-6$ 

9. 6    11. (a) -10    (b) -6    13. (a) 14    (b) 2

15. (a) 0    (b) 0

17. (a) Undefined. You cannot divide by zero.    (b)  $\frac{1}{2}$ 

19. Commutative (addition)    21. Inverse (addition)

## A30 Answers to Warm Ups, Odd-Numbered Exercises, Quizzes, and Tests

23. Distributive Property    25. Inverse (multiplication)  
 27. Identity (addition)    29. Identity (multiplication)  
 31. Associative (addition)  
 33.  $x(3y) = (x \cdot 3)y$  Associative (multiplication)  
        $= (3x)y$  Commutative (multiplication)  
 35.  $2^2 \cdot 3^2$     37.  $2^3 \cdot 5^2$     39.  $-14$     41.  $\frac{1}{24}$   
 43.  $\frac{7}{20}$     45.  $\frac{1}{12}$     47.  $-0.13$     49. 1.56    51. 18.81  
 53. 41.14    55. 16.6%    57.  $\approx 2$  meals  
 59. (a) 34.6%  
       (b) Social Security:  $\approx \$456$  billion  
           Veteran's Benefits:  $\approx \$51$  billion  
           Education:  $\approx \$71$  billion  
           Health:  $\approx \$196$  billion  
           Medicare:  $\approx \$231$  billion  
           Income Security:  $\approx \$312$  billion  
 (c)  $\approx \$260$  billion; Answers will vary. Example: No. Because the total human resources expenses will change, the amounts of money spent on Social Security and healthcare will change, and so the difference between these amounts will change.

61.  $\approx 5237$  students  
 63. (a) Scientific: 5  $\boxed{\times}$   $\boxed{}$  18  $\boxed{-}$  2  $\boxed{yx}$  3  $\boxed{}$   
        $\boxed{+}$  10  $\boxed{=}$   
       Graphing: 5  $\boxed{\times}$   $\boxed{}$  18  $\boxed{-}$  2  $\boxed{\wedge}$  3  $\boxed{}$   
        $\boxed{+}$  10  $\boxed{\text{ENTER}}$   
 (b) Scientific: 6  $\boxed{x^2}$   $\boxed{+/-}$   $\boxed{-}$   $\boxed{(}$  7  $\boxed{+}$   $\boxed{(}$  2  $\boxed{+/-}$   $\boxed{)}$   
        $\boxed{yx}$  3  $\boxed{)}$   $\boxed{=}$   
       Graphing:  $\boxed{(-)}$  6  $\boxed{x^2}$   $\boxed{-}$   $\boxed{(}$  7  $\boxed{+}$   $\boxed{(}$   $\boxed{-}$  2  $\boxed{\wedge}$   
       3  $\boxed{)}$   $\boxed{\text{ENTER}}$

## Section R1.3 (page R27)

### Warm Up (page R27)

1. 1    2. 5    3. 4    4. 4    5.  $\frac{1}{4}$     6. 1  
 7.  $\frac{3}{7}$     8. 0    9.  $-\frac{1}{8}$     10. 1

1. 64    3. 8    5. 729    7.  $-81$     9.  $\frac{1}{2}$     11. 8  
 13.  $-\frac{3}{10}$     15. 5184    17.  $-\frac{3}{5}$     19. 1    21. 18  
 23.  $\frac{7}{16}$     25.  $-125z^3$     27.  $16x^7$     29.  $10x^4$   
 31.  $-3z^7$     33.  $\frac{5y^4}{2}$     35.  $\frac{5184}{y^7}$     37.  $\frac{7}{x}$     39.  $\frac{1}{x}$   
 41.  $3^{3n}$     43.  $1, x \neq 0$     45.  $\frac{1}{(y+2)^3}$     47.  $32y^2$

49.  $\frac{10}{x}$     51.  $\frac{125x^9}{y^{12}}$     53.  $5.73 \times 10^7$  square miles

55.  $9.461 \times 10^{12}$  kilometers    57. 350,000,000 air sacs

59. 0.000000000000000000001602 coulomb

61.  $1 \times 10^{18}$  attoseconds

63. (a)  $6.0 \times 10^4$  (b)  $2.0 \times 10^{11}$

65. (a)  $3.071 \times 10^6$  (b)  $3.077 \times 10^{10}$

67. (a)  $4.907 \times 10^{17}$  (b) 1.479

69. (a)  $(5.1 - 3.6)^5$  (b)  $[1 + 3(2)]^{-2}$

71. (a) \$19,154.30 (b) \$19,147.63

- (c) \$19,121.84 (d) \$19,055.59

As the number of compoundings per year increases, the balance in the account also increases.

73.  $\approx 4.46\%$

## Section R1.4 (page R36)

### Warm Up (page R36)

1.  $\frac{4}{27}$     2. 48    3.  $-8x^3$     4.  $6x^7$   
 5.  $28x^6$     6.  $\frac{1}{5}x^2$     7.  $3z^4$     8.  $\frac{25}{4x^2}$     9. 1  
 10.  $(x + 2)^{10}$

1.  $9^{1/2} = 3$     3.  $\sqrt[3]{32} = 2$     5.  $\sqrt{196} = 14$   
 7.  $(-216)^{1/3} = -6$     9.  $81^{3/4} = 27$     11.  $\sqrt[3]{27^2} = 9$   
 13. 3    15. 3    17.  $\frac{1}{2}$     19.  $-125$     21. 4  
 23. 216    25.  $\sqrt{6}$     27.  $\frac{27}{8}$     29.  $-4$   
 31.  $2x\sqrt[3]{2x^2}$     33.  $\frac{5|x|\sqrt{3}}{y^2}$     35.  $\frac{2\sqrt[3]{2}}{y}$     37.  $\frac{\sqrt{3}}{3}$   
 39.  $4\sqrt[3]{4}$     41.  $\frac{x(5 + \sqrt{3})}{11}$     43.  $3(\sqrt{6} - \sqrt{5})$   
 45. 25    47.  $2^{1/2}$     49.  $x^{3/2}, x \neq 0$     51.  $2\sqrt[4]{2}$   
 53.  $3^{1/2} = \sqrt{3}$     55.  $\sqrt[3]{x}$     57.  $2\sqrt{x}$   
 59.  $31\sqrt{2}$     61.  $-2\sqrt{y}$     63. 3.557    65. 2.006  
 67. 2.938    69. 0.382    71.  $\sqrt{5} + \sqrt{3} > \sqrt{5 + 3}$   
 73.  $5 > \sqrt{3^2 + 2^2}$     75.  $\sqrt{3} \cdot \sqrt[4]{3} > \sqrt[3]{3}$   
 77. 24 inches  $\times$  24 inches  $\times$  24 inches    79.  $\approx 12.8\%$   
 81. No. The escape velocity is equal to approximately 2375 meters per second, which is greater than the velocity of the rocket.  
 83.  $\approx 1.57$  seconds    85.  $\approx 0.026$  inch  
 87.  $\approx 494$  vibrations per second

89. a; Higher notes have higher frequencies.

93.  $a^0 = a^{n-n} = \frac{a^n}{a^n} = 1$

95. Answers will vary.

91. 1

55.  $500r^2 + 1000r + 500$

57. No

59. 9860.37; 11,399.88; In the years 2001 and 2002, the total amounts of Federal Pell Grants were approximately \$9,860,370,000 and \$11,399,880,000, respectively.

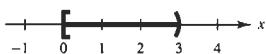
**Mid-Chapter Quiz (page R39)**

1.  $-|-7| < |7|$

2.  $-(-3) = |-3|$

3.  $x \geq 0$

4.  $r \geq 96.5\%$

5.  $0 \leq x < 3$  denotes all numbers greater than or equal to 0 and less than 3.

6.  $3x^2, -7x, 2$

7. 3

8.  $-4$

9.  $\frac{5}{14}$

10.  $\frac{11}{9}$

11.  $-2x^7$

12.  $\frac{1}{3}y^4$

13.  $\frac{27x^6}{y^6}$

14. \$2219.64

15.  $-1$

16.  $-64$

17. 9

18.  $-\sqrt[3]{3}$

19.  $2\sqrt{3}$

20. 26 cm  $\times$  26 cm  $\times$  26 cm

**Section R1.5 (page R46)****Warm Up (page R46)**

1.  $42x^3$

2.  $-20z^2$

3.  $-27x^6$

4.  $-3x^6$

5.  $\frac{9}{4}z^3, z \neq 0$

6.  $4\sqrt{3}$

7.  $\frac{9}{4x^2}$

8. 8

9.  $\sqrt{2}$

10.  $-3x$

1. Degree: 2

3. Degree: 5

Leading coefficient: 2

Leading coefficient: 1

5. Degree: 5

Leading coefficient: 3

7. Polynomial,  $-3x^3 + 2x + 8$ , degree 3

9. Not a polynomial

11. Polynomial,  $-w^4 + 2w^3 + w^2$ , degree 413. (a)  $-1$  (b) 3 (c) 7 (d) 1115. (a)  $-10$  (b)  $-1$  (c) 4 (d) 517.  $-2x - 10$ 

19.  $2x^2 - 4x - 5$

21.  $8x^3 + 29x^2 + 11$

23.  $3x^3 - 6x^2 + 3x$

25.  $4x^4 - 12x$

27.  $30x^3 + 12x^2$

29.  $x^2 + 7x + 12$

31.  $6x^2 - 7x - 5$

33.  $x^2 - 25$

35.  $x^2 + 12x + 36$

37.  $4x^2 - 20xy + 25y^2$

39.  $x^2 + 2xy + y^2 - 6x - 6y + 9$

41.  $x^3 + 3x^2 + 3x + 1$

43.  $8x^3 - 12x^2y + 6xy^2 - y^3$

45.  $9y^4 - 1$

47.  $m^2 - n^2 - 6m + 9$

49.  $x - y$

51.  $x^4 + x^2 + 1$

53.  $2x^2 + 2x$

55.  $500r^2 + 1000r + 500$

57. No

59. 9860.37; 11,399.88; In the years 2001 and 2002, the total amounts of Federal Pell Grants were approximately \$9,860,370,000 and \$11,399,880,000, respectively.

61. Volume =  $4x^3 - 184x^2 + 2052x$

 $x = 5$  inches:  $V = 6160$  cubic inches $x = 7$  inches:  $V = 6720$  cubic inches $x = 9$  inches:  $V = 6480$  cubic inches $x = 7$  inches produces the greatest volume.

63.  $3x^2 + 7x$

**Section R1.6 (page R53)****Warm Up (page R53)**

1.  $15x^2 - 6x$

2.  $-2y^2 - 2y$

3.  $4x^2 + 12x + 9$

4.  $9x^2 - 48x + 64$

5.  $2x^2 + 13x - 24$

6.  $-5z^2 - z + 4$

7.  $4y^2 - 1$

8.  $x^2 - a^2$

9.  $x^3 + 12x^2 + 48x + 64$

10.  $8x^3 - 36x^2 + 54x - 27$

1.  $3(x + 2)$

3.  $4x(x^2 - 2)$

5.  $(x - 1)(x + 5)$

7.  $(x + 6)(x - 6)$

9.  $(4x + 3y)(4x - 3y)$

11.  $(x + 1)(x - 3)$

13.  $(x - 2)^2$

15.  $(2y + 3)^2$

17.  $(5y - 1)^2$

19.  $(x - 2)(x^2 + 2x + 4)$

21.  $(y + 5)(y^2 - 5y + 25)$

23.  $(2t - 1)(4t^2 + 2t + 1)$

25.  $(x + 2)(x - 1)$

27.  $(w - 2)(w - 3)$

29.  $(y + 5)(y - 4)$

31.  $(x - 20)(x - 10)$

33.  $(3x - 2)(x - 1)$

35.  $(3x + 1)(3x - 2)$

37.  $(5x + 1)(x + 5)$

39.  $(x - 1)(x^2 + 2)$

41.  $(2x - 1)(x^2 - 3)$

43.  $(2 - y^3)(3 + y)$

45.  $4x(x - 2)$

47.  $y(y - 3)(y + 3)$

49.  $x^2(x - 4)$

51.  $(x - 1)^2$

53.  $(1 - 2x)^2$

55.  $y(2y + 3)(y - 5)$

57.  $2x(x - 2)(x + 1)$

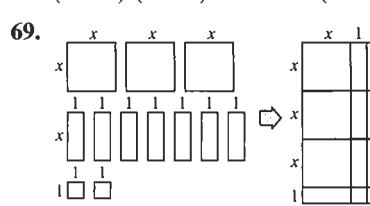
59.  $(3x + 1)(x^2 + 5)$

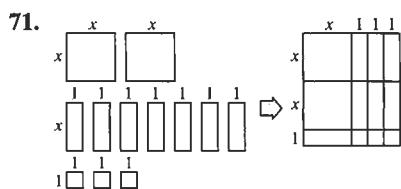
61.  $x(x - 4)(x^2 + 1)$

63.  $-x(x + 10)$

65.  $(x + 1)^2(x - 1)^2$

67.  $2(t - 2)(t^2 + 2t + 4)$



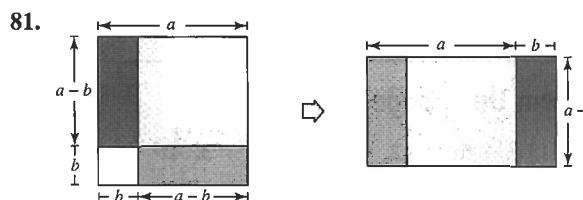


**73.**  $(2x + 1)$  feet

**75.** (a)  $(x - 2)(3x + 4)$  (b)  $(x + 5)(x + 6)$

**77.**  $c = \{9, 16, 21, 24, 25\}$ ; Answers will vary.

**79.** Answers will vary.



## Section R1.7 (page R60)

### Warm Up (page R60)

1.  $5x^2(1 - 3x)$
2.  $(4x + 3)(4x - 3)$
3.  $(3x - 1)^2$
4.  $(2y + 3)^2$
5.  $(z + 3)(z + 1)$
6.  $(x - 5)(x - 10)$
7.  $(3 - x)(1 + 3x)$
8.  $(3x - 1)(x - 15)$
9.  $(s + 1)(s + 2)(s - 2)$
10.  $(y + 4)(y^2 - 4y + 16)$

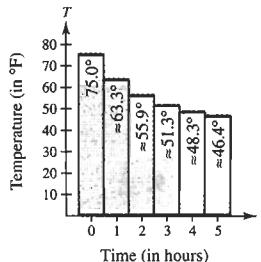
1. All real numbers
3. All real numbers except  $x = 2$
5. All real numbers except  $x = 0$  and  $x = 4$
7. All real numbers greater than or equal to  $-1$
9.  $3x$
11.  $x - 2$ ,  $x \neq 2$
13.  $x + 2$ ,  $x \neq -2$
15.  $\frac{3x}{2}$ ,  $x \neq 0$
17.  $\frac{x}{2(x + 1)}$
19.  $-\frac{1}{2}$ ,  $x \neq 5$
21.  $-(x + 5)$ ,  $x \neq 5$
23.  $\frac{x(x + 3)}{x - 2}$ ,  $x \neq -2$
25.  $\frac{y - 4}{y + 6}$ ,  $y \neq 3$
27.  $-1 - x^2$ ,  $x \neq 2$
29.  $z - 2$
31.  $\frac{1}{5(x - 2)}$ ,  $x \neq 1$
33.  $-\frac{x(x + 7)}{x + 1}$ ,  $x \neq 9$
35.  $\frac{r + 1}{r}$ ,  $r \neq 1$
37.  $\frac{t - 3}{(t + 3)(t - 2)}$ ,  $t \neq -2$
39.  $\frac{x - 1}{x(x + 1)^2}$ ,  $x \neq -2$
41.  $\frac{3}{2}$ ,  $x \neq -y$
43.  $x(x + 1)$ ,  $x \neq -1, 0$
45.  $\frac{x + 5}{x - 1}$
47.  $\frac{2x + 5}{x - 5}$

**49.**  $\frac{6x + 13}{x + 3}$     **51.**  $\frac{x - 4}{(x + 2)(x - 2)(x - 1)}$

**53.**  $\frac{2 - x}{x^2 + 1}$ ,  $x \neq 0$     **55.**  $\frac{1}{2}$ ,  $x \neq 2$     **57.**  $\frac{1}{x}$ ,  $x \neq -1$

**59.**  $\frac{2x - 1}{2x}$ ,  $x > 0$     **61.** (a) 12.65% (b)  $\frac{288(NM - P)}{N(12P + NM)}$

**63.** ; No



## Review Exercises (page R64)

1. (a) Natural: {11}    (b) Integer: {11, -14}    (c) Rational:  $\{11, -14, -\frac{8}{9}, \frac{5}{2}, 0.4\}$     (d) Irrational:  $\{\sqrt{6}\}$
3.  $-4 < -3$
5.  $x \leq -6$  denotes all real numbers less than or equal to  $-6$ .
7.  $x \geq 0$
9.  $-14$
11.  $|-12| > -|12|$
13. 3
15.  $|x - 7| \geq 4$
17.  $2x^2, -3x, 4$
19. (a) 2 (b) 0
21. Distributive Property
23.  $-1$
25.  $\frac{2}{3}$
27. 5
29. 0.10
31.  $-2$
33.  $8x$
35.  $3.5116 \times 10^7$
37. 483,400,000 miles
39. (a) 11,414.125 (b) 18,380.160
41. 

Year	5	10	15
Balance	\$2697.70	\$3638.79	\$4908.19
43.  $16^{1/2} = 4$
45. 13
47.  $2x^2$
49.  $2 + \sqrt{3}$
51.  $-3\sqrt{x}$
53.  $\sqrt{10}$
55.  $\sqrt{5}$
57. 11.269
59.  $-6x + 26$
61.  $x^2 - 8x - 14$
63.  $x^2 - x - 2$
65.  $x^3 - x^2 + 2x - 2$

**67.** 260.74

In 2002, the median sales price for a new one-family home in the northeastern United States was \$260,740.

**69.**  $x = 5$ : 27,132.5

$x = 12$ : 139,620.4

There were 27,132,500 and 139,620,400 cell phone subscribers in the United States in 1995 and 2002, respectively.

**71.**  $4(x + 3)(x - 3)$     **73.**  $3x(x + 1)(x - 2)$ **75.**  $(x^2 - 2)(x - 4)$     **77.** All real numbers except  $x = 3$ **79.** All real numbers    **81.**  $3x$ **83.**  $\frac{x - 2}{2}$ ,  $x \neq -2$     **85.**  $x + 2$ ,  $x \neq 0$ **87.**  $\frac{x - 1}{x - 3}$ ,  $x \neq -1, \frac{1}{2}$     **89.**  $\frac{3x^2 - 4x}{(x - 1)(x - 2)}$ **91.**  $\frac{x + 1}{x - 1}$ ,  $x \neq 0$     **93.**  $\frac{4x}{2x - 3}$ ,  $x \neq 0, -\frac{3}{2}$ **Chapter Test (page R67)****1.** -12

Year	5	10	15
Balance	\$4470	\$6659	\$9921

Year	20	25
Balance	\$14,780	\$22,021

The longer you leave the \$3000 in the account, the more money you earn.

**3.**  $-64x^6$     **4.**  $-4\sqrt{x}$     **5.** 25    **6.**  $4(\sqrt{3} - \sqrt{5})$ **7.**  $2x\sqrt{3x}$     **8.**  $\frac{5 + \sqrt{7}}{9}$     **9.**  $9x^2 + 42x + 49$ **10.**  $-5x^2 + 29x$     **11.**  $5(x + 4)(x - 4)$ **12.**  $(2x + 3)^2$     **13.**  $(x^2 - 3)(x - 6)$ **14.**  $(x + 2)^2(x - 2)$     **15.**  $\frac{1}{3}(x - 4)$ ,  $x \neq -4$ **16.**  $\frac{x + 4}{3x + 5}$ ,  $x \neq -3, \frac{5}{3}$     **17.**  $\frac{4x^2 - 13x}{(x - 3)(x - 4)}$ **18.**  $-\frac{x + 26}{(x + 5)(x - 2)}$ **19.** All real numbers greater than or equal to -3**20.** All real numbers except  $x = 2$ **21.**  $\frac{2x^2 - 5x - 18}{5 + 5x - x^2}$ ,  $x \neq 1, -2$ **22.**  $x = 5$ : 236.75,  $x = 12$ : 294.36

In 1995 and 2002, the total expenditures for U.S. colleges and universities were about \$236.75 billion and \$294.36 billion, respectively.

**Chapter R2****Section R2.1 (page R76)****Warm Up (page R76)**

- |                              |                          |                          |                  |
|------------------------------|--------------------------|--------------------------|------------------|
| 1. $-3x - 10$                | 2. $5x - 12$             | 3. $x$                   | 4. $x + 26$      |
| 5. $\frac{8x}{15}$           | 6. $\frac{3x}{4}$        | 7. $-\frac{1}{x(x + 1)}$ | 8. $\frac{5}{x}$ |
| 9. $\frac{7x - 8}{x(x - 2)}$ | 10. $-\frac{2}{x^2 - 1}$ |                          |                  |

**1.** Identity    **3.** Conditional equation**5.** Conditional equation**7.** (a) No    (b) No    (c) Yes    (d) No**9.** (a) Yes    (b) Yes    (c) No    (d) No**11.** (a) Yes    (b) No    (c) No    (d) No**13.** (a) No    (b) No    (c) No    (d) Yes**15.** (a) No    (b) No    (c) No    (d) No**17.** 5    **19.** -4    **21.** 3    **23.** 9    **25.** -26**27.** -4    **29.**  $-\frac{6}{5}$     **31.** 9    **33.** No solution**35.** 10    **37.** 4    **39.** 3    **41.** 5    **43.** No solution**45.**  $\frac{11}{6}$     **47.** No solution    **49.** 0**51.** All real numbers    **53.** No solution**55.** Because substituting 2 for  $x$  in the equation produces division by zero,  $x = 2$  cannot be a solution to the equation.**57.** Check by substituting in the original equation, by using the *table* feature of a graphing utility, or by evaluating the solution in the original equation using a graphing utility.**59.**  $x \approx 138.889$     **61.**  $x \approx 62.372$     **63.**  $x \approx 19.993$ **65.** Use the *table* feature in ASK mode or use the scientific calculator part of the graphing utility.**67.** (a) 6.46    (b) 6.41; Yes**69.** (a) 56.09    (b) 56.13; Yes**71.** 2004 ( $t \approx 14.02$ )    **73.** 61.2 inches**75.** 1998 ( $t \approx 8.35$ )    **77.** 1999 ( $t \approx 9.29$ )**Section R2.2 (page R87)****Warm Up (page R87)**

- |       |                  |                   |      |                     |
|-------|------------------|-------------------|------|---------------------|
| 1. 14 | 2. 4             | 3. -3             | 4. 4 | 5. -2               |
| 6. 1  | 7. $\frac{2}{5}$ | 8. $\frac{10}{3}$ | 9. 6 | 10. $-\frac{11}{5}$ |

1.  $x + (x + 1) = 2x + 1$     3.  $50t$     5.  $0.2x$     7.  $6x$   
 9.  $1200 + 25x$     11.  $525 = n + (n + 1); 262, 263$

13.  $5x - x = 148; 37, 185$   
 15.  $n^2 - 5 = n(n + 1); -5, -4$   
 17. Coworker's check: \$300  
     Your check: \$345  
 19. Coworker's check: \$348.65  
     Your check: \$296.35  
 21.  $\approx 37.03\%$  decrease    23.  $\approx 39.42\%$  increase

25. (a)  $\approx 498.96$  million users  
     (b)  $\approx 543.87$  million users  
     (c)  $\approx 580.85$  million users  
 27. Two TVs:  $\approx 36.278$  million households  
     Three or more TVs:  $\approx 43.747$  million households  
     VCR:  $\approx 97.097$  million households  
     Basic cable:  $\approx 74.690$  million households  
     Premium cable:  $\approx 51.216$  million households  
 29. 15 feet  $\times$  22.5 feet    31.  $\approx 5.7$  years  
 33. 97 or greater    35. \$22,316.98  
 37. \$1411.76    39.  $\approx 20.13\%$     41. \$361.25  
 43. 3 hours    45.  $\frac{1}{3}$  hour

47. Family 1 (42 miles per hour):  $\approx 3.8$  hours  
     Family 2 (50 miles per hour): 3.2 hours  
 49.  $\approx 1.28$  seconds    51. 62.5 feet    53. \$563,952  
 55. \$4500 at 5.5%    57. 11.43%  
     \$7500 at 7%

59. 8823 units per month    61.  $\approx 48$  feet  
 63.  $\approx 32.1$  gallons    65.  $\approx 12.31$  miles per hour  
 67.  $h = \frac{2A}{b}$     69.  $l = \frac{V}{wh}$     71.  $C = \frac{S}{1 + R}$   
 73.  $r = \frac{A - P}{Pt}$     75.  $b = \frac{2A - ah}{h}$   
 77.  $n = \frac{L + d - a}{d}$     79.  $h = \frac{A}{2\pi r}$

81. A mathematical model should be accurate and easy to use. If the model is very complicated, the user may make errors or choose not to use the model. So, sometimes a reasonably accurate model that is easy to use is better than a very complicated model that is more accurate.

83.  $\approx 192.27$  cubic inches

## Section R2.3 (page R100)

### Warm Up (page R100)

1.  $\frac{\sqrt{14}}{10}$     2.  $4\sqrt{2}$     3. 14    4.  $\frac{\sqrt{10}}{4}$   
 5.  $x(3x + 7)$     6.  $(2x - 5)(2x + 5)$   
 7.  $-(x - 7)(x - 15)$     8.  $(x - 2)(x + 9)$   
 9.  $(5x - 1)(2x + 3)$     10.  $(6x - 1)(x - 12)$

1.  $2x^2 + 5x - 3 = 0$     3.  $x^2 - 25x = 0$   
 5.  $x^2 - 6x + 7 = 0$     7.  $2x^2 - 2x + 1 = 0$   
 9.  $3x^2 - 60x - 10 = 0$     11. 4, -2    13. 0,  $-\frac{1}{2}$   
 15. -5    17. 3,  $-\frac{1}{2}$     19. 2, -6    21. -2, -5  
 23.  $\pm 4$     25.  $\pm\sqrt{7} \approx \pm 2.65$     27.  $\pm 2\sqrt{3} \approx \pm 3.46$   
 29.  $12 + 3\sqrt{2} \approx 16.24$     31.  $-2 + 2\sqrt{3} \approx 1.46$   
      $12 - 3\sqrt{2} \approx 7.76$      $-2 - 2\sqrt{3} \approx -5.46$   
 33.  $\pm 5$     35.  $\pm\frac{\sqrt{115}}{5} \approx \pm 2.14$     37.  $\pm 8$     39. 1  
 41.  $\pm\frac{3}{4}$     43.  $\frac{3}{2}$     45. 6, -12    47.  $\frac{3}{2}, -\frac{1}{2}$     49. 5,  $-\frac{10}{3}$   
 51. 9, 3    53.  $\frac{1}{5}, 1$     55. -1, -5    57.  $-\frac{1}{2}$   
 59. Algebra argument:

$$\begin{aligned}(x + 2)^2 &= (x + 2)(x + 2) && \text{Definition of exponent} \\&= x^2 + 2x + 2x + 4 && \text{FOIL} \\&= x^2 + 4x + 4 && \text{Combine like terms.}\end{aligned}$$

So,  $(x + 2)^2 \neq x^2 + 4$ .

Graphing utility argument:

- (1) Let  $y_1 = (x + 2)^2$  and  $y_2 = x^2 + 4$ . Use the table feature with an arbitrary value of  $x$  (but not  $x = 0$ ). The table will show that  $y_1$  is not the same as  $y_2$ .
- (2) Use the scientific calculator portion of the graphing utility to show that if  $x = 5$ ,  $(5 + 2)^2 = 49$  and  $5^2 + 4 = 29$ . So,  $(x + 2)^2$  is not equal to  $x^2 + 4$ .

61. 34 feet  $\times$  48 feet  
 63. Base:  $2\sqrt{2}$  feet  
     Height:  $2\sqrt{2}$  feet  
 65.  $\approx 3.54$  seconds    67.  $\approx 1.43$  seconds  
 69.  $\approx 24.37$  seconds    71.  $\approx 3.54$  centimeters  
 73. 976 miles    75.  $\approx 1414$  feet  
 77. 50,000 units    79. 2015 ( $t \approx 15.4$ )  
 81. 1987 ( $t \approx 18.74$ ); The model is a good representation through 2002.

83. The model in Exercise 82 is *not* valid for the population in 2050 because it predicts 536,526,000 people (not 419,854,000).
85. 2002 ( $t \approx 11.62$ ); No; for 1980 ( $t = -10$ ) the model yields a value of  $E = 865$ , or 865,000 students. From 1995–2001, the enrollment steadily increased from 708,000 to 897,970 students. It is unlikely that in 1980 the enrollment was significantly higher than it was 15 years later in 1995.

## Section R2.4 (page R110)

### Warm Up (page R110)

1. $3\sqrt{17}$	2. $2\sqrt{3}$	3. $4\sqrt{6}$	4. $3\sqrt{73}$
5. $2, -1$	6. $\frac{3}{2}, -3$	7. $5, -1$	8. $\frac{1}{2}, -7$
9. $3, 2$	10. $4, -1$		

1. One real solution    3. Two real solutions  
 5. No real solutions    7. Two real solutions  
 9.  $\frac{1}{2}, -1$     11.  $\frac{1}{4}, -\frac{3}{4}$     13.  $1 \pm \sqrt{3}$   
 15.  $-7 \pm \sqrt{5}$     17.  $-4 \pm 2\sqrt{5}$     19.  $\frac{2}{3} \pm \frac{\sqrt{7}}{3}$   
 21.  $-\frac{1}{3} \pm \frac{\sqrt{11}}{6}$     23.  $-\frac{1}{2} \pm \sqrt{2}$     25.  $\frac{2}{7}$   
 27.  $2 \pm \frac{\sqrt{6}}{2}$     29.  $6 \pm \sqrt{11}$     31.  $x \approx 0.976, -0.643$   
 33.  $x \approx 0.561, 0.126$     35.  $x \approx 1.687, -0.488$   
 37.  $-11$     39.  $\pm\sqrt{10}$     41.  $-\frac{3}{2} \pm \frac{\sqrt{5}}{2}$     43.  $-2, 4$   
 45.  $\pm 2$     47.  $50, 50$     49.  $7, 8$  or  $-8, -7$   
 51. 200 units    53. 653 units    55. 9 seats per row  
 57. 14 inches  $\times$  14 inches  
 59. Moon:  $\approx 14.9$  seconds  
 Earth:  $\approx 2.6$  seconds  
 61. Shorter period of time on Earth  
 63.  $\approx 259$  miles;  $\approx 541$  miles  
 65. (a) 1999 ( $t \approx 9.28$ )  
 (b) 2005 ( $t \approx 14.85$ )  
 (c) No. The model's prediction of \$899.66 exceeds the expected consumer spending.  
 67. 2010 ( $t = 10$ ); Yes. The model in Exercise 66 predicts a spending amount of \$378 billion, which is close to the industry's projection of \$374 billion.  
 69. Southbound:  $\approx 550$  miles per hour  
 Eastbound:  $\approx 600$  miles per hour

71. 3761 units or 146,239 units  
 73. In an application, one of the solutions may not make sense in the context. In Example 5, the other possible solution is  $t \approx -29.77$ . Because the number of alternative fuel vehicles has been steadily growing since 1993, it is not likely that there were 1,000,000 of them in 1960. So, this solution ( $t \approx -29.77$ ) can be rejected.

## Mid-Chapter Quiz (page R114)

1.  $x = -6$     2.  $x = 6$     3.  $x = -2$     4. No solution  
 5. 328.954    6. 431.398  
 7. Use the table feature in ASK mode or the scientific calculator portion of the graphing utility.  
 8.  $7.50x + 20,000 = 80,000$ ; 8000 units  
 9. 3499 units ( $x \approx 3499.214$ ) or 321,501 units  
 ( $x \approx 321,500.786$ )  
 10.  $x = \frac{2}{3}, -5$     11.  $x = \pm\sqrt{5}; x \approx \pm 2.24$   
 12.  $x = -3 \pm \sqrt{17}; x \approx -7.12, 1.12$   
 13.  $x = -1 \pm \sqrt{6}$     14.  $x = \frac{-7 \pm \sqrt{73}}{6}$   
 15.  $x \approx 1.568, -0.068$     16. No real solutions  
 17. One real solution  
 18. Answers will vary. Sample answer: Use the FOIL method [ $(x + 3)^2 = (x + 3)(x + 3) = x^2 + 6x + 9$ ], use the table feature of your graphing utility, or use the scientific calculator portion of your graphing utility to evaluate the solution.  
 19.  $\approx 3.95$  seconds    20. 6 inches  $\times$  6 inches

## Section R2.5 (page R123)

### Warm Up (page R123)

1. 11	2. 20, -3	3. 5, -45	4. 0, $-\frac{1}{5}$
5. $\frac{2}{3}, -2$	6. $\frac{11}{6}, -\frac{5}{2}$	7. 1, -5	8. $\frac{3}{2}, -\frac{5}{2}$
9. $\frac{3 \pm \sqrt{5}}{2}$	10. $2 \pm \sqrt{2}$		

1.  $3, -1, 0$     3.  $0, \pm\frac{3\sqrt{2}}{2}$     5.  $\pm 3$     7.  $-3, 0$   
 9.  $\pm 2, 7$     11.  $\pm 1$     13.  $\pm\sqrt{11}, \pm 1$     15.  $\pm 2$   
 17.  $\pm\frac{1}{2}, \pm 4$     19. 1, -2    21. 50    23. 26  
 25. -16    27.  $\frac{1}{4}$     29. 6, 5    31. 2, -5    33. 0  
 35. -59, 69    37. 1    39.  $\pm\sqrt{69}$     41.  $\frac{-3 \pm \sqrt{21}}{6}$   
 43. 4, -5    45. -1    47. 1, -3    49. 1, -3

51. 3, -2    53.  $\sqrt{3}$ , -3    55. 10, -1

57. The quadratic equation was not written in standard form before the values for  $a$ ,  $b$ , and  $c$  were substituted in the Quadratic Formula. The standard form for this equation is  $3x^2 - 7x - 4 = 0$  ( $a = 3$ ,  $b = -7$ , and  $c = -4$ ), and the correct solution is

$$x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(3)(-4)}}{2(3)}$$

59.  $x \approx \pm 1.038$     61.  $x \approx 16.756$     63. 34    65. 7%

67.  $\approx 19.2\%$     69. 26,250 passengers

71. 62 years old; This model is not used for people over the age of 65 because, as  $x$  increases past  $x = 65$ , the  $y$ -values are not low enough to produce realistic life expectancies.

73. 2,566,025 units; It does not make sense for demand  $x$  or price  $p$  to be less than zero.

75.  $\approx 12.12$  feet    77.  $13\frac{1}{3}$  minutes    79.  $11\frac{1}{9}$  hours

## Section R2.6 (page R134)

### Warm Up (page R134)

1.  $-\frac{1}{2}$     2.  $-\frac{1}{6}$     3. -3    4. -6    5.  $x \geq 0$   
 6.  $-3 < z < 10$     7.  $P \leq 2$     8.  $W \geq 200$   
 9. 2, 7    10. 0, 1

1.  $-1 \leq x \leq 5$ ; Bounded    3.  $x > 11$ ; Unbounded

5.  $x < -2$ ; Unbounded    7. c    8. h    9. f

10. e    11. g    12. a    13. b    14. d

15. (a) Yes (b) No (c) Yes (d) No

17. (a) Yes (b) No (c) No (d) Yes

19. (a) Yes (b) Yes (c) Yes (d) No

21.  $x \geq 6$

23.  $x > -4$



25.  $x < 25$

27.  $x > 2$



29.  $x \leq -\frac{1}{3}$

31.  $x < -18$



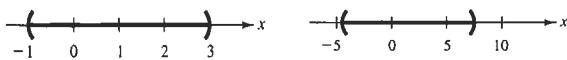
33.  $x > \frac{2}{5}$

35.  $2 \leq x < 4$



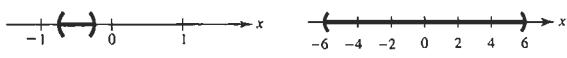
37.  $-1 < x < 3$

39.  $-\frac{9}{2} < x < \frac{15}{2}$



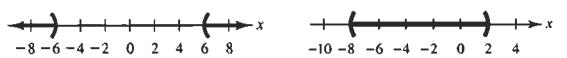
41.  $-\frac{3}{4} < x < -\frac{1}{4}$

43.  $-6 < x < 6$



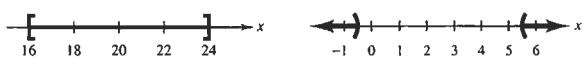
45.  $x < -6, x > 6$

47.  $-8 < x < 2$



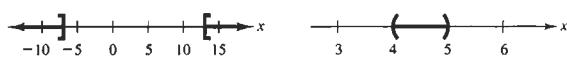
49.  $16 \leq x \leq 24$

51.  $x < -\frac{1}{2}, x > \frac{11}{2}$



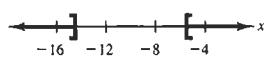
53.  $x \leq -7, x \geq 13$

55.  $4 < x < 5$



57.  $x \leq -\frac{29}{2}, x \geq -\frac{11}{2}$

59. No solution



61.  $|x| \leq 2$     63.  $|x - 9| \geq 3$     65.  $|x - 12| \leq 10$

67.  $|x + 3| > 5$     69. More than 400 miles

71. Greater than 12.5%    73. 24 weeks

75. (a)

$x$	10	20	30	40	50
$R$	\$1159.50	\$2319.00	\$3478.50	\$4638.00	\$5797.50
$C$	\$1700.00	\$2650.00	\$3600.00	\$4550.00	\$5500.00

(b)  $x \geq 36$  units

77. Less than 24,062.5 miles    79.  $x \geq 128.93$

81. 2005 ( $t < 15.07$ )    83. [ $\approx 106.864, \approx 109.464$ ]

85. Overcharged or undercharged up to \$0.47

87. [65.8, 71.2]    89. [20, 80]

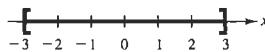
### Math Matters (page R137)

Cube	Ratio of surface area weight
1	6
2	3
3	2
4	1.5

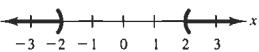
**Section R2.7 (page R145)****Warm Up (page R145)**

1.  $y < -6$     2.  $z > -\frac{9}{2}$     3.  $-3 \leq x < 1$   
 4.  $x \leq -5$     5.  $-3 < x$     6.  $5 < x < 7$   
 7.  $-\frac{7}{2} \leq x \leq \frac{7}{2}$     8.  $x < 2, x > 4$   
 9.  $x < -6, x > -2$     10.  $-2 \leq x \leq 6$

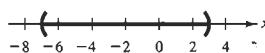
1.  $-3 \leq x \leq 3$



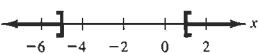
3.  $x < -2, x > 2$



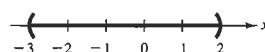
5.  $-7 < x < 3$



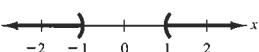
7.  $x \leq -5, x \geq 1$



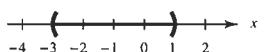
9.  $-3 < x < 2$



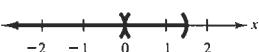
11.  $x < -1, x > 1$



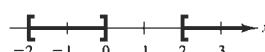
13.  $-3 < x < 1$



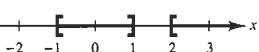
15.  $x < 0, 0 < x < \frac{3}{2}$



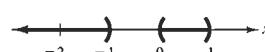
17.  $-2 \leq x \leq 0, x \geq 2$



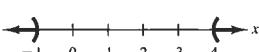
19.  $-1 \leq x \leq 1, x \geq 2$



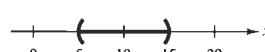
21.  $x < -1, 0 < x < 1$



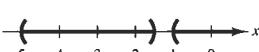
23.  $x < -1, x > 4$



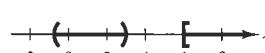
25.  $5 < x < 15$



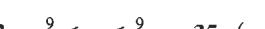
27.  $-5 < x < -\frac{3}{2}, x > -1$



29.  $-\frac{3}{4} < x < 3, x \geq 6$



31.  $[-2, 2]$



33.  $-\frac{9}{2} \leq x \leq \frac{9}{2}$     35.  $(-\infty, 3], [4, \infty)$

37. All real numbers    39. All real numbers

41. The cube root of any real number is a real number.

43.  $-3.51 < x < 3.51$     45.  $-0.13 < x < 25.13$

47.  $2.26 < x < 2.39$     49. Between 4 and 6 seconds

51.  $\approx 13.8$  meters  $\leq l \leq \approx 36.2$  meters

53. (a)  $90,000 \leq x < 100,000$     (b)  $\$30 \leq p \leq \$32$

(c) 185,968 units

55. 9.5%    57. 2006 ( $t > 15.71$ )

59. 2006/2007 ( $t > 17.28$ )

**Review Exercises (page R150)**

1. Conditional equation

3. (a) No    (b) Yes    (c) Yes    (d) No

5.  $-\frac{1}{2}$     7.  $-10$     9.  $-\frac{2}{3}$     11. 377.778    13. 12

15.  $130 - x = 100$ ; 30 pounds    17. 29.5 feet  $\times$  59 feet

19. \$12    21. \$161.25    23. 2 hours

25.  $\approx 2.9$  quarts    27.  $-\frac{1}{2}, \frac{4}{3}$     29. 3, 8

31.  $\pm\sqrt{11}, \approx \pm 3.32$

33.  $-4 + 3\sqrt{2} \approx 0.24$

$-4 - 3\sqrt{2} \approx -8.24$

35. (1) Use the *table* feature in ASK mode with the variable equal to a solution.

(2) Use the scientific calculator portion of the graphing utility to evaluate the quadratic equation at a particular solution.

37. 15 feet  $\times$  27 feet    39. 200,000 units or 300,000 units

41. Two real solutions    43.  $6 \pm \sqrt{6}$

45.  $\frac{-19 \pm \sqrt{165}}{2}$     47.  $-3 \pm 2\sqrt{3}$

49. 1.866, -0.283    51. Moon:  $\approx 6.09$  seconds

Earth: 2.5 seconds

53. 0, -1, 4    55.  $-3, \sqrt[3]{5}$     57.  $\frac{25}{4}$     59. No solution

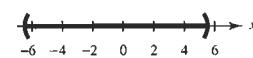
61.  $\pm 4\sqrt{2}$     63.  $-3, \frac{7}{5}$

65.  $2 \pm \sqrt{19}$     67. \$600    69.  $\approx 21.2\%$

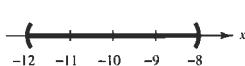
71.  $x < 11$



73.  $-\frac{13}{2} < x < \frac{11}{2}$

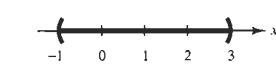


75.  $-12 < x < -8$

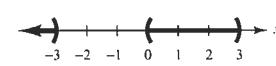


77.  $x \geq 36$  units

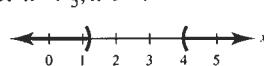
79.  $-1 < x < 3$



81.  $x < -3, 0 < x < 3$



83.  $x < \frac{6}{5}, x > 4$



85.  $-1.69 < x < 1.69$

87.  $1.65 < x < 1.74$     89.  $x \geq 10$

91. All real numbers    93.  $x \leq 6$  or  $x \geq 9$

95. Between 3.65 and 4.72 seconds

97. Greater than 6.96%    99.  $25,359 \leq x \leq 94,641$

101. (a)

$t$	0	5	10	11
$R$	188,175	207,047	225,919	229,693

(b) 2009 ( $t \geq 19.03$ )

### Chapter Test (page R154)

1.  $\frac{17}{23}$     2. (a) All real numbers    (b)  $-3 \leq x \leq 3$

3. April: \$175,364.00    4.  $-\frac{5}{3}, \frac{1}{2}$     5.  $4, -\frac{3}{2}$   
May: \$140,291.20

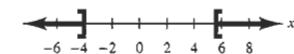
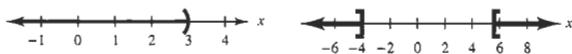
6.  $\pm\sqrt{15}$     7.  $\frac{-13 \pm \sqrt{69}}{2}$     8.  $\frac{11 \pm \sqrt{145}}{6}$

9. 1.038, -0.446    10.  $2, -\frac{10}{3}$     11. 4

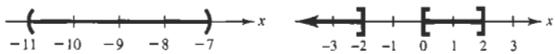
12.  $-1, 1, -3, 3$     13.  $-6, 6$

14. Selling either 341,421 units or 58,579 units will produce a revenue of \$2,000,000.

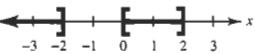
15.  $x < 3$     16.  $x \leq -4, x \geq \frac{28}{5}$



17.  $(-11, -7)$



18.  $x \leq -2, 0 \leq x \leq 2$



19. More than 10,839 units but less than 129,161 units

20. 2004 ( $t > 23.8$ )

### Cumulative Test: Chapters R1–R2 (page R155)

1.  $-32x^6$     2.  $3x^2\sqrt{2x}$     3.  $\frac{3 + \sqrt{5}}{2}$

4.  $(x + \sqrt{3})(x - \sqrt{3})(x - 6)$     5.  $\frac{x + 4}{5}, x \neq 4$

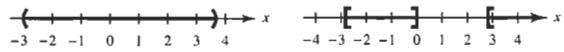
6.  $\frac{y - x}{x + y}, xy \neq 0$

7. (a) 172,000,000    (b) 2006 ( $t = 15.84$ )

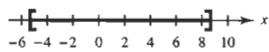
8.  $5, \frac{1}{2}$     9. 0.734, -1.022    10.  $\frac{8}{3}, -\frac{10}{3}$

11.  $5 - 2\sqrt{2}$     12.  $\pm 1, \pm 4$     13.  $\pm 3\sqrt{2}$

14.  $-3 < x < \frac{11}{3}$     15.  $-2\sqrt{2} \leq x \leq 0, x \geq 2\sqrt{2}$



16.  $-\frac{16}{3} \leq x \leq \frac{26}{3}$



17. At least 10,470 units but no more than 222,864 units

18. 2007 ( $t > 16.97$ )

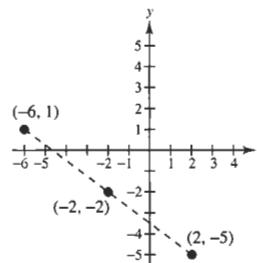
## Chapter 1

### Section 1.1 (page 12)

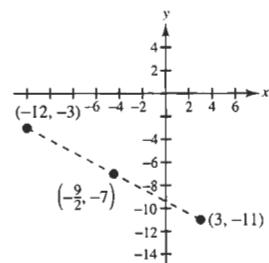
#### Warm Up (page 12)

1. 5    2.  $3\sqrt{2}$     3. 1    4. -2  
5.  $3(\sqrt{2} + \sqrt{5})$     6.  $2(\sqrt{3} + \sqrt{11})$     7. -3, 11  
8. 9, 1    9. 0,  $\pm 3$     10.  $\pm 2$

1. (a)



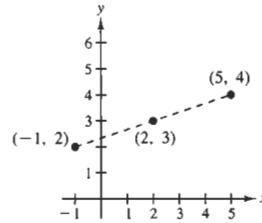
3. (a)



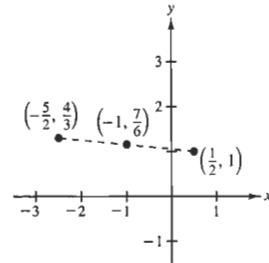
- (b) 10    (c)  $(-2, -2)$

- (b) 17    (c)  $(-\frac{9}{2}, -7)$

5. (a)



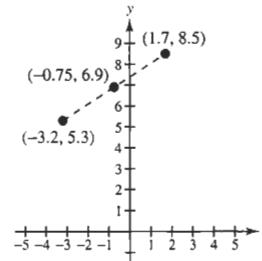
7. (a)



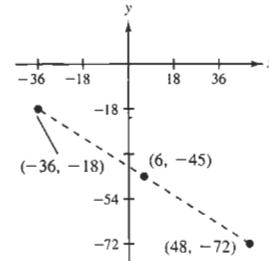
- (b)  $2\sqrt{10}$     (c)  $(2, 3)$

- (b)  $\frac{\sqrt{82}}{3}$     (c)  $(-1, \frac{7}{6})$

9. (a)



11. (a)



- (b)  $\sqrt{34.25}$

- (b)  $6\sqrt{277}$

- (c)  $(-0.75, 6.9)$

- (c)  $(6, -45)$

13. 5    15.  $\sqrt{109}$

21. (a) Yes    (b) Yes

17.  $x = 15, -9$

19.  $y = 9, -23$

23. (a) Yes    (b) Yes