

Use the functions  $f(x) = x^2 - 3x$  and  $g(x) = x - 5$  to answer questions #1 and #2:

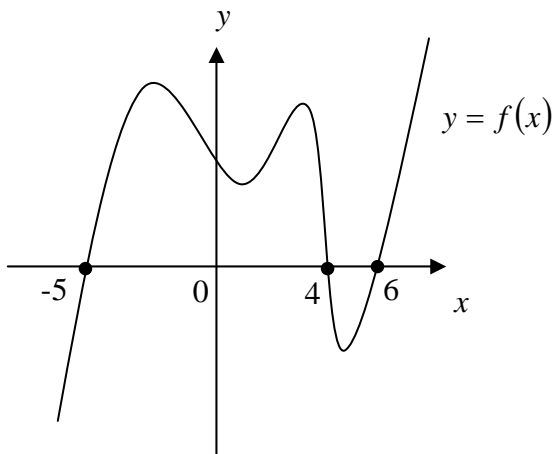
1. Find and simplify  $(f - g)(-2)$ .

- A. -17
- B. 5
- C. 17
- D. 13
- E. None of the above

2. Find and simplify  $(f \circ g)(x)$

- A.  $x^2 - 13x + 40$
- B.  $x^3 - 8x^2 + 15x$
- C.  $x^2 - 3x + 40$
- D.  $x^3 - 3x^2 - 5x$
- E.  $x^2 - 2x - 5$

3. Which of the following sign charts describes the graph of the function  $y = f(x)$  given below.



- A. sign of  $f(x)$   $\begin{array}{c} + \quad | \quad + \quad | \quad - \quad | \quad + \\ \leftarrow \text{-----} \rightarrow \\ -5 \quad 4 \quad 6 \end{array}$
- B. sign of  $f(x)$   $\begin{array}{c} - \quad | \quad + \quad | \quad + \quad | \quad - \\ \leftarrow \text{-----} \rightarrow \\ -5 \quad 4 \quad 6 \end{array}$
- C. sign of  $f(x)$   $\begin{array}{c} + \quad | \quad - \quad | \quad + \quad | \quad - \\ \leftarrow \text{-----} \rightarrow \\ -5 \quad 4 \quad 6 \end{array}$
- D. sign of  $f(x)$   $\begin{array}{c} - \quad | \quad + \quad | \quad - \quad | \quad + \\ \leftarrow \text{-----} \rightarrow \\ -5 \quad 4 \quad 6 \end{array}$
- E. sign of  $f(x)$   $\begin{array}{c} - \quad | \quad - \quad | \quad + \quad | \quad - \\ \leftarrow \text{-----} \rightarrow \\ -5 \quad 4 \quad 6 \end{array}$

4. If the point  $P(-2,3)$  is on the graph of  $y = f(x)$ , find the corresponding point on the graph of  $y = f(4x) + 1$ .

- A.  $\left(-\frac{1}{2}, 4\right)$   
B.  $\left(-\frac{1}{2}, 2\right)$   
C.  $(-8, 4)$   
D.  $(-8, 2)$   
E. None of the above.

5. Solve the following system of equations for  $y$ .

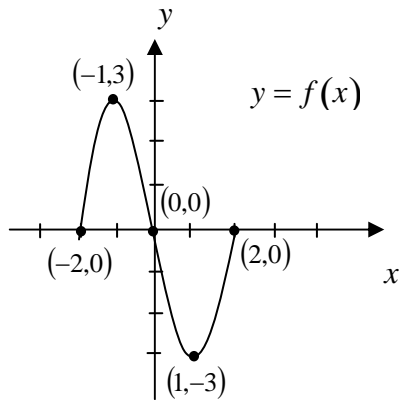
$$\begin{cases} x^2 + y^2 = 25 \\ x^2 - y = 5 \end{cases}$$

- A.  $y = 0, y = 3$   
B.  $y = 0, y = 4$   
C.  $y = -4, y = 5$   
D.  $y = -3, y = 3$   
E.  $y = -5, y = 4$

6. Suppose  $y$  is directly proportional to the square root of  $x$  and inversely proportional to the product of  $v$  and  $w$ . If  $x=36, v=2$  and  $w=1$ , then  $y=9$ . Find the constant of proportionality,  $k$ .

- A.  $k = \frac{1}{3}$   
B.  $k = 3$   
C.  $k = \frac{1}{2}$   
D.  $k = 2$   
E. None of the above

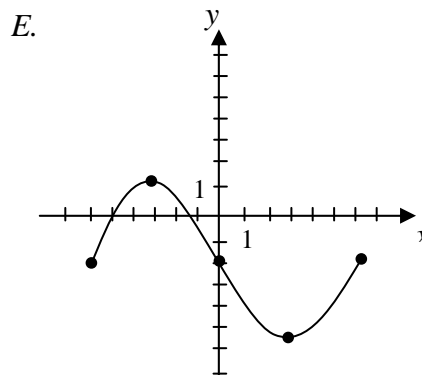
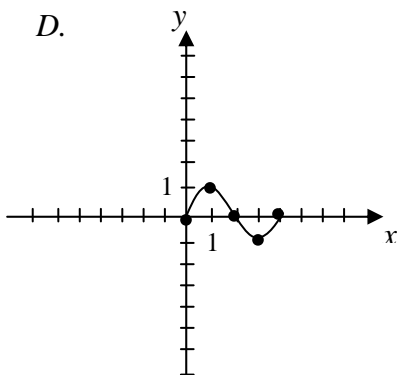
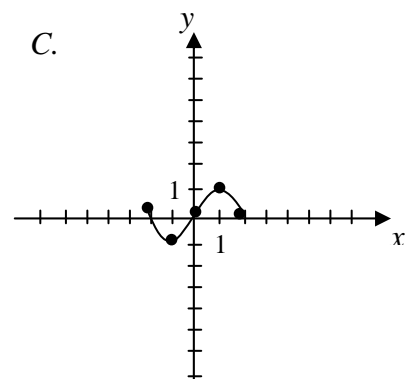
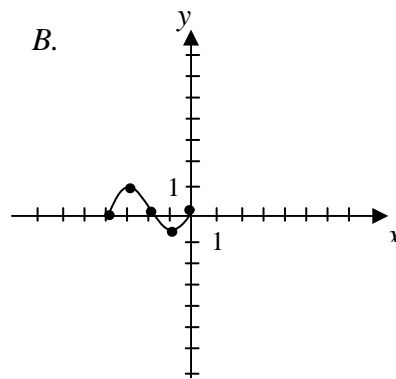
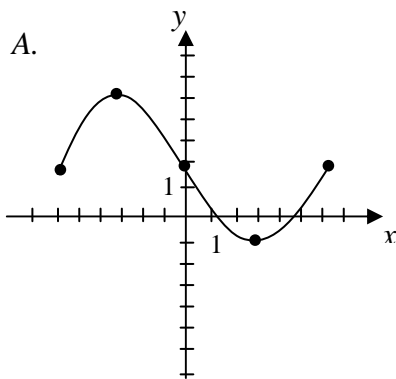
Use the graph of a function  $y = f(x)$  given below to answer questions #7 and #8.



7. Find the interval(s) for which  $f$  is increasing. Express your answer in interval notation.

- A.  $[-2, -1] \cup [1, 2]$
- B.  $[-2, -1] \cup [0, 1]$
- C.  $[-1, 1]$
- D.  $[-2, 0] \cup [1, 2]$
- E.  $[-2, 2]$

8. Choose the graph that depicts the graph of  $y = \frac{1}{3} f(x + 2)$ .



9. Find a linear function such that  $f(1) = 5$  and  $f(2) = 9$ .

- A.  $y = 4x - 19$
- B.  $y = \frac{1}{4}x + 5$
- C.  $y = 4x + 1$
- D.  $y = \frac{1}{4}x - \frac{1}{4}$
- E. None of the above.

10. Find the standard equation of the parabola with vertical axis whose vertex is  $V(-2, -1)$  and passes through the point  $(-4, 5)$ .

- A.  $y = \frac{1}{7}(x - 2)^2 - 1$
- B.  $y = \frac{5}{3}(x + 2)^2 - 1$
- C.  $y = \frac{1}{6}(x - 2)^2 - 1$
- D.  $y = -\frac{3}{49}(x + 2)^2 - 1$
- E.  $y = \frac{3}{2}(x + 2)^2 - 1$

11. Solve the following inequality. Express your answer in interval notation.

$$(x - 2)(x + 3)(x - 1) \leq 0$$

- A.  $(-\infty, -3] \cup [2, \infty)$
- B.  $[-3, 1] \cup [2, \infty)$
- C.  $(-\infty, -3] \cup [1, 2]$
- D.  $[1, 2]$
- E. None of the above

12. Express the parabola  $f(x) = 2x^2 - 8x - 1$  in standard form.

A.  $y = 2(x - 4)^2 + 15$

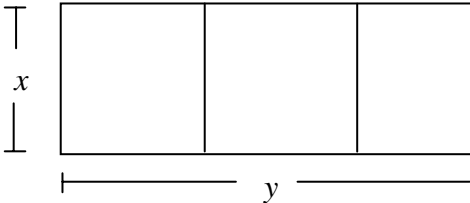
B.  $y = 2(x - 2)^2 - 9$

C.  $y = 2(x - 2)^2 + 7$

D.  $y = 2(x - 4)^2 - 17$

E. None of the above.

13. A farmer has 3000 feet of fence to enclose a rectangular field and subdivide it into three rectangular plots (see the figure). If  $x$  denotes the width of the field and  $y$  the length, find the value of  $x$  so that the total area of the field is maximized.



A.  $x = 250$  feet

B.  $x = 750$  feet

C.  $x = 1000$  feet

D.  $x = 375$  feet

E. Not enough information given.

14. A helicopter lifts off the ground vertically at a rate of 6 meters/second. A person is standing at a point 75 meters away due west of the point at which the helicopter took off. If  $t$  denotes the time (in seconds) since the helicopter lifted off, express the distance,  $d$ , between the helicopter and the person as a function of  $t$ . Simplify the function.

A.  $d(t) = 6t + 75$

B.  $d(t) = \sqrt{6t + 75}$

C.  $d(t) = \sqrt{6t^2 + 5625}$

D.  $d(t) = \sqrt{36 + 5625t^2}$

E.  $d(t) = \sqrt{36t^2 + 5625}$

15. A tour bus company charges fares based on the number of people in a group. For one particular trip, the company charges \$30 per person for a group of 25 people or less. For each additional person above 25, the company charges \$28 per person. Let  $C$  be the total charge for the trip and  $x$  the number of people. Express  $C$  as a function of  $x$ . Simplify the function.

$$A. C(x) = \begin{cases} 30x & \text{if } x \leq 25 \\ 28x + 50 & \text{if } x > 25 \end{cases}$$

$$B. C(x) = \begin{cases} 30x & \text{if } x \leq 25 \\ 58x & \text{if } x > 25 \end{cases}$$

$$C. C(x) = \begin{cases} 30x & \text{if } x \leq 25 \\ 28x & \text{if } x > 25 \end{cases}$$

$$D. C(x) = \begin{cases} 30x & \text{if } x \leq 25 \\ 28x + 750 & \text{if } x > 25 \end{cases}$$

$$E. C(x) = \begin{cases} 30x & \text{if } x \leq 25 \\ 58x - 25 & \text{if } x > 25 \end{cases}$$