

# Solutions 1-8

all 10 pts except #2

## Form A

- 1 D
- 2 C
- 3 D
- 4 ~~A B~~
- 5 C
- 6 D
- 7 A
- 8 C

## Form B

- 1 E
- 2 A
- ~~3~~
- 4 ~~A B~~
- 5 D
- 6 ~~D E~~
- 7 C
- 8 D

**Problem 9 (10 pts)** Let  $\mathbf{r}(t) = (x(t), y(t))$ ,  $t \geq 0$  denote the position of a particle at time  $t$  with acceleration  $\mathbf{a}(t) = (3t, -2)$ , initial velocity  $\mathbf{v}_0 = (2, 1)$  and initial position  $\mathbf{r}_0 = (0, 6)$ . The value of  $x(t)$  when  $y(t) = 0$  is

$$\text{y data } v_y = -2t + 1$$

$$r_y = -t^2 + t + 6 = -(t-3)(t+2)$$

Smallest positive root is

$$t = 3$$

4 pts for this

$$\text{x data } v_x = \frac{3}{2}t^2 + 2$$

$$r_x = \frac{1}{2}t^3 + 2t$$

$$\text{when } t = 3 \text{ this is } \frac{27}{2} + 6 = \frac{39}{2}$$

4 pts for this

Some credit if  $t = -2$  was chosen.

2 for correct ans.

$$x(t) = \frac{27}{2} + 6 \text{ or } \frac{39}{2}$$

Problem 10 Find an equation of the tangent plane to the surface  $z = 5 - 2x^2 - y^2$  at  $(1, 1, 2)$ , and the parametric equation of the line perpendicular to this plane at that point.

Plane

$$\begin{aligned} f_x &= -4x, & f_x &= -4 \\ f_y &= -2y, & f_y &= -2 \end{aligned} \quad \left. \begin{array}{l} f_x = -4 \\ f_y = -2 \end{array} \right\} @ (1, 1, 2)$$

④ pts for both partials

2 more for correct equation

(6 pts) Equation of the Tangent Plane:

$$z - 2 = -4(x-1) - 2(y-1)$$

$$z = -4x - 2y + 8$$

$$\frac{x-1}{-4} = \frac{y-1}{-2} = \frac{z-2}{-1}$$

(6 pts) Equation of Perpendicular Line:

allow 4 points if  $x$  and  $y$  both right (they  $\rightarrow$  may have wrong signs)

$$\begin{aligned} x &= -4t + 1 \\ y &= -2t + 1 \\ z &= -t + 2 \end{aligned}$$