

1. Find the domain D of $f(x) = \frac{x-2}{x^2+x-6}$.

A. $D = (-\infty, 2) \cup (2, \infty)$

B. $D = (-\infty, -3) \cup (-3, \infty)$

C. $D = (-\infty, -3) \cup (2, \infty)$

D. $D = (-\infty, -3) \cup (-3, 2) \cup (2, \infty)$

E. $D = (-3, 2)$

2. Given $g(x) = \frac{4}{x}$, then $\frac{g(x+h) - g(x)}{h} =$

A. $\frac{-4}{x^2}$

B. $\frac{4}{x+h} - \frac{4}{x}$

C. $\frac{-4}{(x+h)^2}$

D. $\frac{-4}{x(x+h)}$

E. $\frac{4}{x(x+h)}$

3. $\lim_{x \rightarrow 4} \frac{x-4}{\sqrt{x}-2} =$

A. *Doesn't exist*

B. 0

C. 2

D. 4

E. 1

4. Given distance function $s(t) = 3t - \cos t$, where s is in millimeters and t is in seconds, find the acceleration function $a(t)$.

A. $a(t) = 3 + \cos t$

B. $a(t) = 3 + \sin t$

C. $a(t) = \sin t$

D. $a(t) = -\cos t$

E. $a(t) = \cos t$

5. The derivative of $\frac{x^2+5}{x+1}$ is

A. $\frac{x^2 - 2x - 5}{(x+1)^2}$

B. $\frac{3x^2 + 2x + 6}{(x+1)^2}$

C. $\frac{x^2 + 2x - 5}{(x+1)^2}$

D. $\frac{-x^2 - 2x + 5}{(x+1)^2}$

E. $\frac{-3x^2 - 2x - 6}{(x+1)^2}$

6. Find the x -coordinate only of any points where the slope of tangent lines to the graph of $f(x) = (x^2 - 8)(x + 3)$ is 1.

A. $x = -3, \quad x = 3$

B. $x = -1, \quad x = 0, \quad x = 3$

C. $x = 1, \quad x = -3$

D. $x = 3, \quad x = -1$

E. $x = 1, \quad x = 0, \quad x = -3$

7. What is the slope of the tangent line to the graph

$y = \left(\frac{2x}{x-1}\right)^3$ at the point $(2, 64)$?

- A. 64
- B. 48
- C. -48
- D. -96
- E. 96

8. Given $g(x) = \sqrt{2x+1}$, find out $g''(4) =$

- A. 3
- B. $\frac{1}{3}$
- C. $\frac{-1}{54}$
- D. $\frac{-1}{27}$
- E. $\frac{-1}{108}$

9. $\lim_{x \rightarrow \infty} \frac{3x^2 + x - 1}{1 + 2x - 4x^3} =$

A. *Doesn't exist*

B. $\frac{1}{4}$

C. 3

D. 0

E. $-\frac{3}{4}$

10. Given $f(x) = x^4 - 4x^2$, please choose the correct statement about its relative Max/Min.

A. f has relative max at $x = \pm\sqrt{2}$, a relative min at $x = 0$.

B. f has a relative max at $x = 0$, relative min at $x = \pm\sqrt{2}$.

C. f has a relative max at $x = \sqrt{2}$, a relative min at $x = -\sqrt{2}$.

D. f has a relative max at $x = -\sqrt{2}$, a relative min at $x = \sqrt{2}$.

E. f has no relative max, but has relative min at $x = \pm\sqrt{2}$.

11. If $g(x) = x + \frac{4}{x}$, then on the closed interval $[1, 3]$,

- A. g has an absolute max at $x = 1$, and an absolute min at $x = 3$.
- B. g has an absolute max at $x = 2$, and an absolute min at $x = 3$.
- C. g has an absolute max at $x = 1$, and an absolute min at $x = 2$.
- D. g has an absolute max at $x = 2$, and an absolute min at $x = 1$.
- E. g has an absolute max at $x = 3$, and an absolute min at $x = 1$.

12. A container company is designing an open-top, square-based, rectangular box that will have a volume of 32 in^3 .

What is the minimum surface area of this box?

- A. 32 in^2
- B. 48 in^2
- C. 64 in^2
- D. 24 in^2
- E. 56 in^2

13. Approximate $\sqrt{3.95}$ by using linearization. Round your answer to 4 decimal places.

- A. 1.9875
- B. 1.9906
- C. 1.9938
- D. 1.9972
- E. 1.9998

14. Find an equation of tangent line to the curve $xy^2 + 3xy = 4$ at the point $(1, -1)$.

- A. $4x - 5y = -1$
- B. $4x + 5y = 9$
- C. $5x + 4y = 9$
- D. $5x - 4y = 1$
- E. $x + y = 2$

15. In calm waters oil spilling from the ruptured hull of a grounded tanker spreads in all directions. If the area polluted is a circle and is increasing at a rate of $200\pi \text{ ft}^2/\text{sec}$, determine how fast the radius is increasing when the radius of the circle is 20 ft .

- A. $\frac{1}{2} \text{ ft/sec}$
- B. 2 ft/sec
- C. 5 ft/sec
- D. 10 ft/sec
- E. 0 ft/sec

16. What is the derivative of $2x^2e^{-x}$?

- A. $4xe^{-x}$
- B. $-2x^2e^{-x}$
- C. $2x(x+2)e^{-x}$
- D. $2x(2-x)e^{-x}$
- E. $-2x^2e^{-x-1}$

17. What is the derivative of $\frac{\ln x + 1}{x}$?

- A. $\frac{1}{x^2}$
- B. $\frac{\ln x + 1}{x^2}$
- C. $\frac{-\ln x}{x^2}$
- D. $\frac{1 - \ln x}{x^2}$
- E. $\frac{\ln x + 2}{x^2}$

18. The population of fish in the lake after time t , in months, is given by $P(t) = \frac{1000}{1 + 2e^{-0.5t}}$, what is the rate of change of $P(t)$ at 4 months? Choose the closest answer.

- A. 168/month
- B. -168/month
- C. 84/month
- D. -84/month
- E. 787/month

19. A sample of *E.coli* is growing exponentially at 40°C , represented by $P(t) = 1000e^{0.033t}$, where t is measured in minutes. What is the generation time? Choose the closest answer.

- A. 693 min
- B. 1000 min
- C. 21 min
- D. 42 min
- E. 63 min

20. $\int 2e^{-3x} dx = ?$

- A. $-6e^{-3x} + c$
- B. $-6e^{-3x-1} + c$
- C. $\frac{-2}{3}e^{-3x} + c$
- D. $\frac{2}{3}e^{-3x} + c$
- E. $\frac{-2}{3}e^{-3x-1} + c$

21. Suppose that the acceleration function $a(t) = -6t + 3$, the initial velocity is $v(0) = 10$, and the initial position $s(0) = 20$. Find the distance function $s(t)$.

A. $s(t) = -t^3 + \frac{3}{2}t^2 + 10t$

B. $s(t) = -3t^2 + 3t + 20$

C. $s(t) = -t^3 + \frac{3}{2}t^2 + 10$

D. $s(t) = -t^3 + \frac{3}{2}t^2 + 20$

E. $s(t) = -t^3 + \frac{3}{2}t^2 + 10t + 20$

22. Evaluate $\int_1^e (x + \frac{1}{x}) dx$

A. $\frac{e^2}{2} + 1$

B. $\frac{1}{e} + e$

C. $\frac{e^2}{2} + \frac{1}{2}$

D. $\frac{e^2}{2} + \frac{3}{2}$

E. $e^2 + 1$

23. Find the area under the graph $f(x) = 2\cos 3x$ over the interval $[-\frac{\pi}{6}, \frac{\pi}{6}]$.

- A. 0
- B. $\frac{2}{3}$
- C. $\frac{4}{3}$
- D. 4
- E. 8

24. Find the area of the region bounded by $y = x$ and $y = x^4$.

- A. $\frac{7}{10}$
- B. $\frac{1}{10}$
- C. $\frac{3}{10}$
- D. $-\frac{1}{10}$
- E. $-\frac{3}{10}$

25. A city grows at a rate of $156t+1000$ people per year, where t is time in years after the beginning of 2002. Given that the population at the beginning of 2002 is 13210. What is the population at the beginning of 2007 ?

- A. 18210
- B. 14990
- C. 16410
- D. 20410
- E. 26420