

The Formula Page may be used. It will be attached to the final exam.

- Calculate $\frac{dy}{dx}$ if $y = \cos(1 - 2x)$.
A. $-\sin(1 - 2x)$ B. $-2\sin(1 - 2x)$ C. $2\sin(1 - 2x)$ D. $\sin(1 - 2x)$ E. $-2\cos(1 - 2x)$
- Find y' if $y = x \tan^2 x$.
A. $2x \tan x + \tan^2 x$ B. $2x \tan x \sec^2 x$ C. $x \sec^2 x + \tan^2 x$ D. $2x \tan x \sec^2 x + \tan^2 x$
E. None of these.
- If $\sin \theta = -0.5473$ and $\pi < \theta < \frac{3\pi}{2}$, find θ in radians. Give your answer correct to 4 decimal places.
A. -0.5791 B. 3.7207 C. 3.1511 D. 2.5625 E. 1.761
- Find the slope of the line perpendicular to the line containing the points $(-2, 4)$ and $(6, -3)$.
A. $-8/7$ B. $-7/8$ C. $1/4$ D. $8/7$ E. $-1/2$
- Give the equation, in slope-intercept form, of the line which is parallel to the line $2y - 6x - 5 = 0$ and passes through the point $(-1, 3)$.
A. $y = 3x + 10$ B. $y = \frac{1}{3}x - 9$ C. $y = \frac{1}{3}x + 2$ D. $y = -3x$ E. $y = 3x + 6$
- If $f(x) = \frac{x}{x^2 + 1}$, find $\frac{1}{f(3)}$.
A. $3/10$ B. $3/16$ C. $16/3$ D. $10/3$ E. $1/3$
- If $f(x) = \frac{2}{x}$ then $\frac{f(x + \Delta x) - f(x)}{\Delta x} =$
A. $\frac{-2}{x^2}$ B. $\frac{2}{x + \Delta x} - \frac{2}{x}$ C. $\frac{-2}{x(x + \Delta x)}$ D. $\frac{2}{x(x + \Delta x)}$ E. $\frac{-2}{x^2 + \Delta x}$
- $\lim_{x \rightarrow 1} \frac{x^2 + 4x - 5}{x^2 - 1} =$
A. 3 B. 1 C. ∞ D. 0 E. 5
- If the tangent line to the graph of $y = f(x)$ at $(2, 3)$ has equation $x - y + 1 = 0$, then $f'(2) =$
A. 1 B. $3/2$ C. $2/3$ D. $-2/3$ E. $-3/2$
- The derivative of $\frac{x^2 + 1}{x + 5}$ is
A. $\frac{(x + 5)(2x) - (x^2 + 1)}{(x + 5)^2}$ B. $2x$ C. $\frac{(x + 5)(2x)}{(x^2 + 1)^2}$ D. $\frac{(x^2 + 1) + (x + 5)(2x)}{(x + 5)^2}$ E. $\frac{(x^2 + 1) - (x + 5)(2x)}{(x + 5)^2}$
- If $y = (3 - x^2)^3$ then $y'' =$
A. $-6x(3 - x^2)^2$ B. $24x^2(3 - x^2) - 6(3 - x^2)^2$ C. $6(3 - x^2)$ D. $24x^2(3 - x^2)$ E. None of these.
- The line tangent to the graph of $f(x) = x - \frac{1}{x}$ at $(2, 3/2)$ has slope
A. $3/4$ B. $3/2$ C. 0 D. $1/4$ E. $5/4$
- A point moves along the x -axis in such a way that its distance, s , from the origin at time $t \geq 1$ is given by $s = (t^3 - t)^{3/2}$. Find the velocity of the point when $t = 2$. Give your answer correct to two decimal places.
A. 3.67 B. 3.83 C. 40.42 D. 36.74 E. 21.08
- Differentiate $y = \sin(x^2)$. $\frac{dy}{dx} =$
A. $\cos(x^2)$ B. $2x \cos(x^2)$ C. $-\cos(x^2)$ D. $\cos(2x)$ E. $-2x \cos(x^2)$

15. Find y' if $y = x \tan x$.
A. $\sec^2 x$ B. $x \sec^2 x$ C. $x \tan 1 + \tan x$ D. $1 + \sec^2 x$ E. $x \sec^2 x + \tan x$
16. Find $f'(x)$ if $f(x) = \frac{x}{\cos(4x)}$. $f'(x) =$
A. $\frac{\cos(4x) + 4x \sin(4x)}{\cos^2(4x)}$ B. $\frac{-1}{4 \sin(4x)}$ C. $\frac{\cos(4x) - x \sin(4x)}{\cos^2(4x)}$ D. $\frac{\cos(4x) + x \sin(4x)}{\cos^2(4x)}$
E. $\frac{-4x \sin(4x)}{\cos^2(4x)}$
17. The maximum value of $f(x) = x^3(40 - x)^2$ on the closed interval, $0 \leq x \leq 40$, occurs at $x =$
A. 20 B. 15 C. 35 D. 18 E. 24
18. Which of the following best describes the graph of $y = 4x^3 - 3x^4$? The graph has a
A. relative maximum point and two points of inflection.
B. relative maximum point, a relative minimum point and one point of inflection.
C. a relative minimum point and two points of inflection.
D. a relative minimum point, two relative maximum points and two points of inflection.
E. None of these.
19. Which of the following best describes the graph of $f(x) = \frac{x^2 + 1}{x^2 - 1}$?
A. Vertical asymptotes $x = 1, x = -1$, and symmetric to the x -axis.
B. Vertical asymptotes $x = 1, x = -1$ but not symmetric to either the x or the y -axis.
C. Vertical asymptotes $x = 1, x = -1$ and symmetric to the y -axis.
D. No vertical asymptotes and symmetric to the y -axis.
E. Vertical asymptote $x = 1$ and symmetric to the x -axis.
20. Find the area of the region bounded by the curves $x^2 + 4y = 0$ and $x^2 - 4y - 8 = 0$.
A. $2/3$ B. $16/3$ C. 6 D. $4/3$ E. $10/3$
21. What is the area of the largest rectangle with sides parallel to the axes which can be inscribed in the first quadrant under the parabola $y = 4 - x^2$? (Give your answer correct to 2 decimal places.)
A. 1.15 B. 1.33 C. 3.08 D. 4.00 E. 2.67
22. A box with square base and no top is to have a volume of 108 in.^3 . What is the smallest possible surface area of such a box.
A. 32 in.^2 B. 24 in.^2 C. 256 in.^2 D. 108 in.^2 E. 56 in.^2
23. Find the value of dy and Δy for $y = 2x^3 - 4x, x = 2$ and $dx = \Delta x = 0.1$. Give your answer correct to two decimal places.
A. $dy = 2, \Delta y = 2.12$ B. $dy = 2, \Delta y = 2.46$ C. $dy = 2.12, \Delta y = 2$ D. $dy = 2.46, \Delta y = 2$
E. None of these.
24. Calculate $\lim_{x \rightarrow \infty} \frac{2 + 3x - 2x^3}{3 - 4x + x^3}$.
A. 2 B. ∞ C. $2/3$ D. $-3/4$ E. -2
25. Evaluate $\int \sqrt{2x+1} dx$
A. $\frac{2}{3}(2x+1)^{3/2} + C$ B. $\frac{1}{3}(2x+1)^{3/2} + C$ C. $(2x+1)^{-1/2} + C$ D. $2(2x+1)^{1/2} + C$
E. None of these.

26. Evaluate $\int_1^2 (6\sqrt{x} - \frac{1}{2\sqrt{x}})dx$. Give your answer correct to 2 decimal places.
A. 9.90 B. 6.90 C. 5.66 D. 7.35 E. None of these
27. An object is thrown vertically downward from the top of a building 200 ft high with an initial velocity of 40 ft/sec. Find its velocity when it hits the ground. ($s = -16t^2 - 40t + 200$.)
A. -40 ft/sec B. -200 ft/sec C. -120 ft/sec D. -80 ft/sec E. None of these.
28. Calculate the area bounded by the parabola $y = x^2$ and the line $y = x + 2$.
A. 9/2 B. 10/3 C. 7/6 D. 15/2 E. None of these.
29. Calculate the volume generated by revolving the area bounded by $y = \sqrt{x}$, the x-axis and $x = 4$ about the y-axis. (Express your answer as a definite integral.)
A. $\pi \int_0^4 x dx$ B. $\pi \int_0^4 \sqrt{x} dx$ C. $2\pi \int_0^4 (4-x)\sqrt{x} dx$ D. $2\pi \int_0^4 x^2 dx$ E. $2\pi \int_0^4 x^{3/2} dx$
30. Find the function, y , satisfying the following conditions: $\frac{dy}{dx} = 3x^2 - 1$, and the graph of y passes through the point (1, 3).
A. $y = x^3 - x + 3$ B. $y = x^3 - x$ C. $y = 6x - 3$ D. $y = 6x$ E. $y = 3x^3 - x + 1$
31. Calculate the volume generated by revolving the area bounded by $y = \sqrt{x}$, the y-axis, and the line $y = 2$, about the x-axis. (Express your answer as a definite integral.)
A. $\pi \int_0^4 (2 - \sqrt{x})^2 dx$ B. $\pi \int_0^4 (4 - x) dx$ C. $2\pi \int_0^4 (2 - \sqrt{x}) dx$ D. $2\pi \int_0^4 (4\sqrt{x} - x) dx$
E. $\pi \int_0^4 x dx$
32. If $f'(x) = 4x - 3$ and $f(0) = 7$ calculate $f(2)$.
A. 5 B. 2 C. 7 D. 9 E. 3
33. Calculate the centroid of a quarter circle of radius r .
A. $\bar{x} = \frac{r}{3\pi}, \bar{y} = \frac{r}{3\pi}$ B. $\bar{x} = \frac{4r}{3}, \bar{y} = \frac{4r}{3}$ C. $\bar{x} = \frac{4r}{\pi}, \bar{y} = 0$ D. $\bar{x} = \frac{4r}{\pi}, \bar{y} = \frac{4r}{\pi}$
E. $\bar{x} = \frac{4r}{3\pi}, \bar{y} = \frac{4r}{3\pi}$
34. Calculate the x -coordinate of the centroid, \bar{x} , of the area given in problem 26, if the area is $16/3$ square units.
A. $\bar{x} = 2$ B. $\bar{x} = 3/2$ C. $\bar{x} = 9/5$ D. $\bar{x} = 12/5$ E. $\bar{x} = 1/5$
35. Find the work done in pumping the water out of the top of a cylindrical tank 5 ft in radius and 10 ft high, if the tank is initially half full of water, which weighs 62.4 lb/ft³.
A. $93,750\pi$ ft-lb B. $58,500\pi$ ft-lb C. $7,800\pi$ ft-lb D. $15,600\pi$ ft-lb E. None of these.
36. A spring of natural length 12 ft. requires a force of 6 lb. to stretch it 2 ft. Find the work done in stretching it 6 ft. ($F = kx$)
A. 54 ft-lb B. 108 ft-lb C. 6 ft-lb D. 36 ft-lb E. 24 ft-lb
37. A vertical rectangular floodgate on a dam is 5 ft long and 4 ft deep. Find the force on the floodgate if its upper edge is 3 ft below the surface. (The weight of water is 62.4 lb/ft³.) Give your answer correct to the nearest integer.
A. 7644 lb B. 3900 lb C. 1248 lb D. 6240 lb E. 2100 lb

38. A horizontal tank with vertical circular ends is filled with oil. If the radius of each end is 2 m, find the force on one end of the tank. (Assume w is the weight of the oil.) Express your answer as a definite integral. (Hint: Assume that the origin is at the center of one of the circular ends.)
 A. $2w \int_0^2 y\sqrt{4-y^2}dy$ B. $w \int_{-2}^2 \sqrt{4-y^2}dy$ C. $2w \int_{-2}^2 (2-y)\sqrt{4-y^2}dy$ D. $2w \int_{-2}^2 (2-y)dy$
 E. None of these.
39. Grant and Stadium Streets are straight and perpendicular to each other. A black 1997 Porsche 911 is going on Grant Street toward the intersection of the two streets at 60 mph (miles per hour), and a red 1993 Volkswagen Golf is going on Stadium Street toward the same intersection at a rate of 40 mph. At what rate is the distance between the two cars decreasing when the Porsche is $1/2$ mile from the intersection and the Golf is $3/8$ mile from it?
 A. 40 mph B. 56 mph C. 60 mph D. 72 mph E. 32 mph
40. The line perpendicular to the graph of $f(x) = x - \frac{1}{x}$ at $(2, \frac{3}{2})$ has slope
 A. $3/4$ B. $3/2$ C. 0 D. $1/4$ E. $-4/5$
41. Find the center C and radius r of the circle whose equation is

$$x^2 + y^2 - 10x + 6y + 30 = 0$$

 A. $C = (-5, 3); r = 2$ B. $C = (-5, 3); r = 4$ C. $C = (5, -3); r = 8$ D. $C = (5, -3); r = 4$
 E. $C = (5, -3); r = 2$
42. If $y^3 + x^2 = 9$ and $\frac{dx}{dt} = 5$, find $\frac{dy}{dt}$ when $x = 1$.
 A. $-5/6$ B. $2/3$ C. -10 D. $1/3$ E. $10/3$
43. Water is flowing into a tank which is in the shape of a right circular cylinder standing on its circular base. If the water is flowing in at a rate of 80 cu. ft. per min. and the radius of the base of the tank is 4 ft., how fast is the water rising when the water is 10 ft. deep?
 A. $\frac{\pi}{5}$ ft/min B. 5π ft/min C. $\frac{50}{\pi}$ ft/min D. $\frac{5}{\pi}$ ft/min E. 50π ft/min
44. Find the mean value of $f(x) = x^{1/3}$ on the interval $[0, 2]$.
 A. $\frac{3}{2^{2/3}}$ B. $\frac{3}{4}$ C. $\frac{1}{2^{4/3}}$ D. $\frac{3}{2^{1/3}}$ E. $\frac{3}{2^{5/3}}$
45. Find the root mean square of $f(x) = \sqrt{x}(1-x)$ on the interval $[0, 2]$.
 A. $1/\sqrt{3}$ B. $2/3$ C. $2/\sqrt{3}$ D. $\sqrt{3}/2$ E. $1/\sqrt{6}$

Answers

1. C; 2. D; 3. B; 4. D; 5. E; 6. D; 7. C; 8. A; 9. A; 10. A; 11. B; 12. E; 13. C; 14. B; 15. E; 16. A; 17. E; 18. A; 19. C; 20. B; 21. C; 22. D; 23. A; 24. E; 25. B; 26. B; 27. C; 28. A; 29. E; 30. A; 31. B; 32. D; 33. E; 34. D; 35. B; 36. A; 37. D; 38. C; 39. D; 40. E; 41. E; 42. A; 43. D; 44. E; 45. A.