

Use the functions,  $f(x) = \frac{2x+1}{x-5}$  and  $g(x) = x+3$ , to answer questions #1 and #2:

1. Find and simplify  $(f+g)(3)$ .

A.  $\frac{5}{2}$

B.  $-\frac{1}{2}$

C.  $-\frac{13}{2}$

D.  $\frac{3}{2}$

E. None of the above.

2. Find and simplify  $(f \circ g)(x)$ .

A.  $\frac{5x-14}{x-5}$

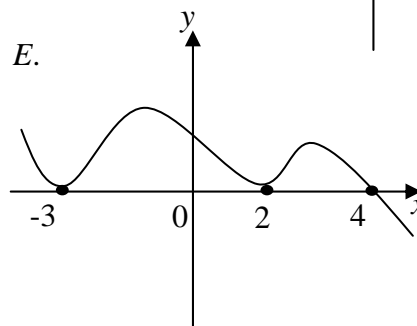
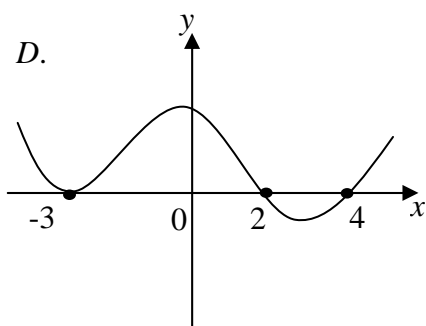
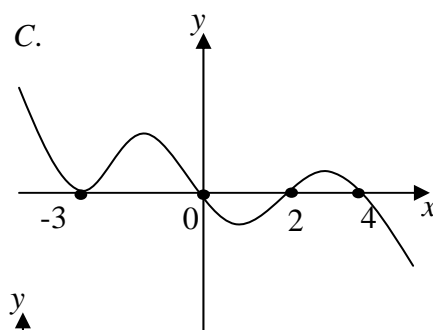
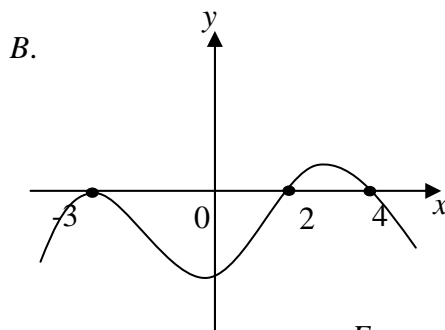
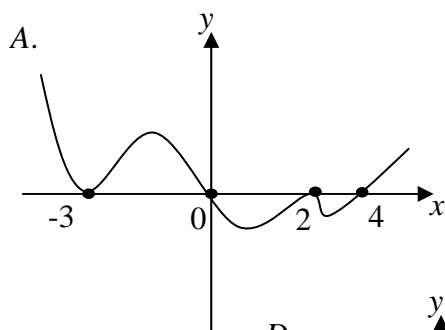
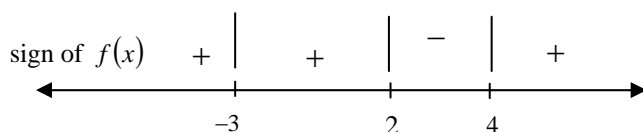
B.  $\frac{2x^2+4x-15}{x-5}$

C.  $\frac{2x+7}{x-2}$

D.  $\frac{2x^2+6x+1}{x^2+3x-5}$

E. None of the above.

3. Which of the following graph best depicts the sign chart given by:



4. Suppose  $y$  is directly proportional to the product of  $w$  and the square root of  $x$  and inversely proportional to the cube of  $p$ . If  $w = 4$ ,  $x = 25$ , and  $p = 2$ , then  $y = 6$ . Find  $y$  if  $w = 7$ ,  $x = 4$ , and  $p = 1$ .

A.  $y = \frac{12}{5}$

B.  $y = \frac{168}{5}$

C.  $y = \frac{121}{2}$

D.  $y = \frac{5}{2}$

E. Cannot be determined.

5. Given the function,  $f(x) = x^2 - x + 1$ , find and simplify  $\frac{f(a+h) - f(a)}{h}$  (assume  $h \neq 0$ ).

A.  $\frac{h^2 - 2a + h + 2}{h}$

B.  $h$

C.  $2a + h$

D.  $h - 1$

E.  $2a + h - 1$

6. Solve the following system of equations for  $x$ :

$$\begin{cases} xy = 6 \\ 2x - y = 1 \end{cases}$$

A.  $x = -\frac{3}{2}, x = 2$

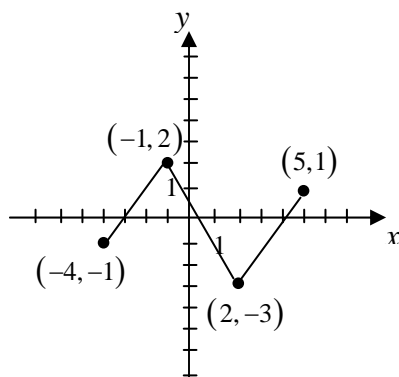
B.  $x = -\frac{7}{2}, x = 6$

C.  $x = -2, x = \frac{3}{2}$

D.  $x = -6, x = \frac{7}{2}$

E.  $x = -\sqrt{\frac{7}{2}}, x = \sqrt{\frac{7}{2}}$

Use the graph of  $y = f(x)$  given below to answer questions #7 and #8:



7. Find the interval(s) for which  $f$  is increasing.

- A.  $[-3, 1]$
- B.  $[-4, -1] \cup [1, 5]$
- C.  $[-1, 2]$
- D.  $[-4, -1] \cup [2, 5]$
- E. No intervals of increasing.

8. Find the domain,  $D$ , and range,  $R$ , of  $y = 4f(x-1)$ .

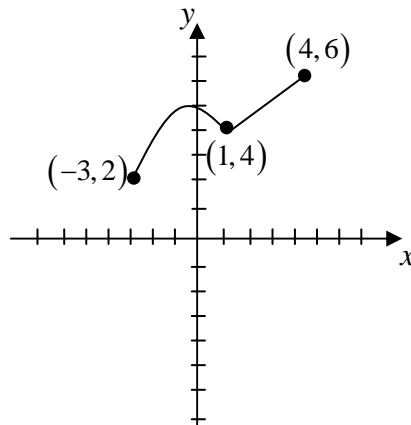
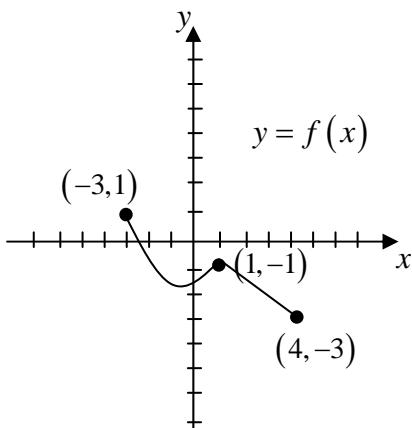
- A.  $D = [-3, 6]; R = [-12, 8]$
- B.  $D = [-3, 20]; R = [-2, 8]$
- C.  $D = [-5, 4]; R = [-12, 8]$
- D.  $D = [-4, 5]; R = \left[-\frac{3}{4}, \frac{1}{2}\right]$
- E.  $D = [-3, 6]; R = \left[-\frac{3}{4}, \frac{1}{2}\right]$

9. Solve the inequality. Express your answer in interval notation.

$$\frac{x-3}{(x+5)(x+1)} \geq 0$$

- A.  $(-5, -1) \cup (-1, 3]$
- B.  $(-5, -1) \cup [3, \infty)$
- C.  $(-\infty, -5) \cup (-1, 3]$
- D.  $[3, \infty)$
- E.  $(-\infty, -5) \cup [3, \infty)$

10. Given below, on the left, is the graph of a basic function,  $y = f(x)$ . The graph on the right was obtained by shifting, reflecting, stretching, and/or compressing the basic graph. Which of the following best describes the graph on the right?



- A.  $y = -f(x+3)$
- B.  $y = f(-x) - 3$
- C.  $y = f(-x) + 3$
- D.  $y = -f(x) - 3$
- E.  $y = -f(x) + 3$

11. Find the standard equation of the parabola whose  $x$ -intercepts are  $-6$  and  $4$  and the highest point has  $y$ -coordinate  $8$ .

- A.  $y = -\frac{8}{25}(x+1)^2 + 8$
- B.  $y = -\frac{8}{9}(x-1)^2 + 8$
- C.  $y = -\frac{2}{9}(x+2)^2 + 8$
- D.  $y = -4(x+1)^2 + 8$
- E.  $y = -2(x-2)^2 + 8$

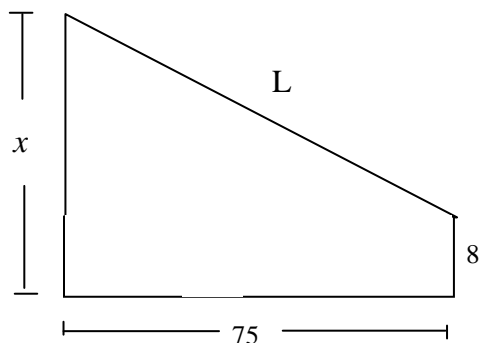
12. Find the maximum or minimum value of the parabola given by  $f(x) = 4x^2 + 24x + 38$  and specify whether it is a maximum or minimum value.

A.  $-3$ ; Maximum  
B.  $2$ ; Minimum  
C.  $-3$ ; Minimum  
D.  $2$ ; Maximum  
E. Not enough information given.

13. Anthony enters a candy store equipped with \$2.10 to buy two kinds of his favorite candy, Gummi bears and jellybeans. Gummi bears sell for \$3.00 per pound and jellybeans sell for \$2.50 per pound. If he is to buy a total of 0.75 pounds of candy, find the system of equations that would be used to find the amount of each that should be purchased. Let  $x$  represent the number of pounds of Gummi bears and  $y$  the number of pounds of jellybeans.

A.  $\begin{cases} x + y = 2.10 \\ 3.00x + 2.50y = 0.75 \end{cases}$   
B.  $\begin{cases} x + y = 0.75 \\ 3.00x + 2.50y = 0.75 \end{cases}$   
C.  $\begin{cases} x + y = 0.75 \\ 3.00x + 2.50y = 2.10 \end{cases}$   
D.  $\begin{cases} x + y = 2.10 \\ 3.00x + 2.50y = 2.10 \end{cases}$   
E. None of the above.

14. Shown below is the apparatus for a zip line (where a person repels down a cable). The two poles are set 75 feet apart. The height of the longer pole is  $x$  and the height of the shorter pole is 8 feet. Express the length  $L$  of the cable as a function of  $x$ . Simplify the function.



A.  $L(x) = \sqrt{x^2 - 16x + 5689}$

B.  $L(x) = \sqrt{x^2 + 5625}$

C.  $L(x) = \sqrt{x^2 + 5689}$

D.  $L(x) = x + 75$

E.  $L(x) = x + 67$

15. A tour bus company charges \$30 per person up to and including the first 10 people and then \$25 per person for each additional person in the group. Find and simplify a piecewise-defined function,  $C$ , that specifies the total charge of a tour of  $x$  people.

A.  $C(x) = \begin{cases} 30x & \text{if } 0 < x \leq 10 \\ 25x & \text{if } x > 10 \end{cases}$

B.  $C(x) = \begin{cases} 30x & \text{if } 0 < x \leq 10 \\ 25x + 10 & \text{if } x > 10 \end{cases}$

C.  $C(x) = \begin{cases} 30x & \text{if } 0 < x \leq 10 \\ 25x + 300 & \text{if } x > 10 \end{cases}$

D.  $C(x) = \begin{cases} 30x & \text{if } 0 < x \leq 10 \\ 25x + 50 & \text{if } x > 10 \end{cases}$

E.  $C(x) = \begin{cases} 30x & \text{if } 0 < x \leq 10 \\ 25x + 550 & \text{if } x > 10 \end{cases}$