

MA 15400, Fall 2009

EXAM 2

Form A

Answers are on the last page.

| | | |
|---|-------------------------------------|---|
| $\sin^2 \theta + \cos^2 \theta = 1$ | $1 + \tan^2 \theta = \sec^2 \theta$ | $1 + \cot^2 \theta = \csc^2 \theta$ |
| $\sin(u + v) = \sin u \cos v + \cos u \sin v$ | | $\sin(u - v) = \sin u \cos v - \cos u \sin v$ |
| $\cos(u + v) = \cos u \cos v - \sin u \sin v$ | | $\cos(u - v) = \cos u \cos v + \sin u \sin v$ |
| $\tan(u + v) = \frac{\tan u + \tan v}{1 - \tan u \tan v}$ | | $\tan(u - v) = \frac{\tan u - \tan v}{1 + \tan u \tan v}$ |
| $\sin(2u) = 2 \sin u \cos u$ | | $\cos(2u) = \cos^2 u - \sin^2 u$ |

Form A

1. A 25 foot ladder leans against the side of a 100 foot tall building. The angle between the ladder and the building is 23° . If the **bottom** of the ladder is then moved **2 feet closer** to the building, to the nearest tenth of a degree, what is the angle that the ladder now makes with the side of the building?

- A. 28.1°
- B. 20.4°
- C. 18.1°
- D. 22.2°
- E. None of the above

2. Express as a trigonometric function of one angle.

$$\sin 43^\circ \cos 17^\circ - \cos 43^\circ \sin 17^\circ$$

- A. $\sin 26^\circ$
- B. $\cos 60^\circ$
- C. $\sin 60^\circ$
- D. $\cos 26^\circ$
- E. None of the above

3. Given $\triangle ABC$ with $\gamma = 90^\circ$, express side a in terms of angle β and side b .

- A. $a = b \sin \beta$
- B. $a = b \cos \beta$
- C. $a = b \sec \beta$
- D. $a = b \tan \beta$
- E. $a = b \cot \beta$

Questions 4 and 5: An airplane is traveling at 250 miles per hour for 3 hours in the directions 130° and then flies in the direction 220° for 1 hour.

4. To the nearest mile, how far is the plane from its starting point?
- A. 599 miles
 - B. 448 miles
 - C. 559 miles
 - D. 791 miles
 - E. None of the above
5. To the nearest degree, in what direction does the plane need to fly in order to get back to the start point?
- A. 288°
 - B. 328°
 - C. 318°
 - D. 302°
 - E. None of the above

6. Find all solutions of the equation using n as an arbitrary integer.

$$\tan\left(3x - \frac{\pi}{4}\right) = -1$$

- A. $x = \frac{\pi}{4} + \frac{\pi}{4}n$
- B. $x = \frac{7\pi}{36} + \frac{\pi}{3}n$
- C. $x = \frac{\pi}{6} + \frac{\pi}{3}n$
- D. $x = \frac{\pi}{3} + \frac{\pi}{3}n$
- E. $x = \frac{5\pi}{36} + \frac{\pi}{3}n$

7. Find the exact solutions of the equation that are in the interval $[0, 2\pi)$.

$$2\cos^2 t + 3\cos t + 1 = 0$$

- A. $t = \frac{2\pi}{3}, \frac{4\pi}{3}, \pi$
- B. $t = \frac{\pi}{6}, \frac{11\pi}{6}, 0$
- C. $t = \frac{\pi}{3}, \frac{5\pi}{3}, 0$
- D. $t = \frac{5\pi}{6}, \frac{7\pi}{6}, \pi$
- E. None of the above

8. If α and β are second-quadrant angles such that $\tan \alpha = \frac{-4}{3}$, and $\sec \beta = -6$, find $\cos(\alpha + \beta)$.

A. $\frac{4-3\sqrt{35}}{30}$

B. $\frac{3-4\sqrt{35}}{30}$

C. $\frac{4+3\sqrt{35}}{30}$

D. $\frac{3+4\sqrt{35}}{30}$

E. None of the above

9. Find the exact value of $\tan(2\theta)$ if $\cos \theta = \frac{-7}{\sqrt{113}}$; $180^\circ < \theta < 270^\circ$.

A. $\frac{-15}{113}$

B. $\frac{15}{113}$

C. $\frac{-112}{15}$

D. $\frac{112}{15}$

E. None of the above

10. Find the solutions of the equation that are in the interval $[0, 2\pi)$.

$$\sin(2t) - \sin(t) = 0$$

- A. $0, \pi, \frac{\pi}{3}, \frac{5\pi}{3}$
- B. $\frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{6}, \frac{11\pi}{6}$
- C. $\frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{3}, \frac{5\pi}{3}$
- D. $0, \pi, \frac{2\pi}{3}, \frac{4\pi}{3}$
- E. None of the above

11. Find the exact value of the expression whenever it is defined.

$$\sin^{-1}\left(\sin \frac{4\pi}{3}\right)$$

- A. $\frac{5\pi}{3}$
- B. $\frac{4\pi}{3}$
- C. $\frac{2\pi}{3}$
- D. $\frac{-\pi}{3}$
- E. None of the above

12. Which of the following is equivalent to $\sin\left(\theta + \frac{3\pi}{2}\right)$? (There are only four choices)

A. $\cos \theta$

B. $\sin \theta$

C. $-\cos \theta$

D. $-\sin \theta$

13. Find the equivalent algebraic expression in x for $x > 0$.

$$\sin\left(2 \tan^{-1}(3x)\right)$$

A. $\frac{1-9x^2}{9x^2+6x+1}$

B. $\frac{6x}{9x^2+1}$

C. $\frac{6x}{9x^2+6x+1}$

D. $\frac{1-9x^2}{9x^2+1}$

E. None of the above

14. Think about the graph of $y = 2 \sin^{-1}(3x)$. Are you thinking? You might want to sketch it.

Which of the following is true about the graph?

(Hint: Domains refers to the possible values of x and range the possible values of y)

- A. Domain is $\left[\frac{-1}{3}, \frac{1}{3}\right]$, Range is $[-\pi, \pi]$
- B. Domain is $[-3, 3]$, Range is $\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$
- C. Domain is $[-3, 3]$, Range is $[-\pi, \pi]$
- D. Domain is $\left[\frac{-1}{3}, \frac{1}{3}\right]$, Range is $\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$
- E. None of the above

15. Approximate the solutions to four decimal places in the interval $\left(\frac{-\pi}{2}, \frac{\pi}{2}\right)$.

$$2 \tan^2 x - 3 \tan x - 5 = 0$$

- A. 2.3562, -1.9513
- B. 1.2490, -0.9828
- C. 1.4508, -0.1960
- D. 1.1903, -0.7854
- E. None of the above

Exam 2 Answers

| Question | Form A - Green | |
|----------|----------------|---|
| 1. | C | 18.1° |
| 2. | A | $\sin 26^\circ$ |
| 3. | E | $a = b \cot \beta$ |
| 4. | D | 791 miles |
| 5. | B | 328° |
| 6. | D | $x = \frac{\pi}{3} + \frac{\pi}{3}n$ |
| 7. | A | $t = \frac{2\pi}{3}, \frac{4\pi}{3}, \pi$ |
| 8. | B | $\frac{3 - 4\sqrt{35}}{30}$ |
| 9. | C | $\frac{-112}{15}$ |
| 10. | A | $0, \pi, \frac{\pi}{3}, \frac{5\pi}{3}$ |
| 11. | D | $\frac{-\pi}{3}$ |
| 12. | C | $-\cos \theta$ |
| 13. | B | $\frac{6x}{9x^2 + 1}$ |
| 14. | A | Range is $[-\pi, \pi]$, Domain is $\left[\frac{-1}{3}, \frac{1}{3}\right]$ |
| 15. | D | 1.1903, -0.7854 |