Lesson 17 Homework Multiplication

To illustrate  $23 \times 14$  with base-ten pieces, we could make fourteen collections of two longs and three units each. A much more efficient method is to construct a rectangle with dimensions 23 units by 14 units and then fill it in with base-ten pieces as shown below. Then the product is the number of total units in the rectangle, expressed as a base-ten number. In this case, we see 2 flats, 11 longs, and 12 units, which can be regrouped into 3 flats, 2 longs and 2 units. So  $23 \times 14 = 322$ 



1. Use this method of sketching rectangular arrays to illustrate the following products. a.  $13 \times 13$ 

b.  $21 \times 32$ 

c.  $23 \times 24$ 

2. With a small amount of practice, and by keeping in mind the way base-number pieces relate, this method can be used in bases other then base ten. Consider  $33_{five} \times 41_{five}$ . The beginning of the sketch for this product is shown below. Fill the rectangle outline with base-five pieces to illustrate the product. Then regroup the resulting pieces to form a minimal collection. (The base-five numeral for the product turns out to be  $3003_{five}$ .)



Use this method of sketching rectangular arrays to illustrate the following products. Be sure to include the correct base numeral for your product.

a.  $13_{\text{five}} \times 13_{\text{five}}$ 

**b.**  $22_{four} \times 31_{four}$ 

c.  $24_{six} \times 34_{six}$