Lesson 29 Section 5.8

Using Factoring to Solve Some Equations.

<u>Principle of Zero Products</u>: If two factors have a product of 0, at least one of the factors must be zero. $ab = 0 \rightarrow a = 0$ or b = 0

Solve: 1) (x-2)(x+3) = 0

2)
$$3y(2y+1)(y-5) = 0$$

Steps for Solving Some Polynomial Equations:

- 1. Write the polynomial in descending order set equal to zero.
- 2. Factor the polynomial completely using appropriate means.
- 3. Apply the Principle of Zero Products rule by setting each factor equal to zero.
- 4. Solve each equation.

Solve:

3) $x^2 - 6x + 8 = 0$

$$4) \qquad m^2 - 9m = 0$$

$$5) \qquad 6a^2 = 8a$$

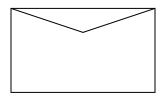
6) $y^2 - 25 = 0$

7)
$$a^3 - 3a^2 = 40a$$

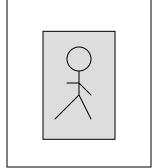
8)
$$(r-3)(r+2) = 14$$

9) If
$$f(x) = 6x^2 + 19x$$
, find all a , such that $f(a) = 7$

<u>Application Problems:</u>
1) An envelope with an area of 96 square centimeters has a length 4 cm more than its width. Find the length and width.



2) A picture frame measures 14 cm by 20 cm and 160 square cm of the picture shows. (See picture below.) Find the width of the frame.



3) Three consecutive **even** integers are such that the square of the first plus the square of the third is 136. Find the 3 integers.

4) A company that makes cabinet sets has the following revenue and cost functions to make *x* sets of cabinets (in thousands of dollars).

 $R(x) = 2x^2 + x$

$$C(x) = x^2 - 2x + 10$$

How many cabinets should be made for the company to break even?

Pythagorean Theorem:

The two shorter sides of a right triangle are called legs and the longest side is called the hypotenuse. Legs are usually labeled a and b and the hypotenuse is labeled c. There is a theorem, called the Pythagorean Theorem that relates the lengths of the three sides of a right triangle.

$$a^2 + b^2 = c^2$$

5) The deck behind a house is a right triangle, where one side is 7 feet longer than the smallest side and the longest side is 8 feet longer than the smallest side. Find the length of the 3 sides.

