

MA 22000 Lesson 18 Notes  
(Calculus part of text) Section 4.3 (part 2)  
The Chain Rule

**Chain Rule Forms:**

If  $y = f(u)$  and  $u = g(x)$ , such that  $y = f(u) = f[g(x)]$ , then

$$\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx} \quad \text{or} \quad \frac{dy}{dx} = f'[g(x)] \cdot g'(x)$$

Derivative of a composite function = derivative of the 'outer' function (with respect to  $u$  or  $g(x)$ ) times the derivative on the 'inner' function (with respect to  $x$ ).

- 1) Use the table below to find: (a)  $D_x(g[f(x)])$  at  $x=2$ , (b)  $D_x(g[f(x)])$  at  $x=1$ .

$x$	1	2	3	4
$f(x)$	2	3	1	2
$f'(x)$	-8	-9	-10	-11
$g(x)$	2	1	4	3
$g'(x)$	0	5	6	9

a)  $D_x(g[f(x)])$  (at  $x=2$ ) =  $g'[f(2)] \cdot f'(2)$

b)

Find the equation of the tangent lines to the graph of the given function at the given value of  $x$ .

2)  $f(x) = (x^3 + 1)^{\frac{3}{2}}$  for  $x = 2$

3)  $g(x) = x^2\sqrt{x^4 - 12}$  for  $x = 2$

Find all values of  $x$  for the given functions where the tangent line is horizontal.

4)  $f(x) = 2\left(\frac{3x-6}{5x}\right)^2$

5)  $h(x) = 2\sqrt{x} - (\sqrt{x})^5$

- 6) A sum of \$2500 is deposited in an account with an interest rate of  $r\%$  per year, compounded daily. At the end of 5 years, the balance in the account is given by  $A = 2500 \left( 1 + \frac{r}{36500} \right)^{1825}$ . Find the rate of change of  $A$  with respect to  $r$  if  $r = 4\%$ .

- 7) The value  $V$  of a machine  $t$  years after it is purchased is given by the equation  $V(t) = \frac{10000}{\sqrt{t+1}}$ . Find the rate of depreciation when (a)  $t = 1$  and when (b)  $t = 3$ .