MA 22400 FORMULAS

CONSUMERS' AND PRODUCERS' SURPLUS

$$CS = \int_0^{q_0} D(q)dq - p_o q_0$$

$$PS = p_o q_0 - \int_0^{q_0} S(q)dq$$

TRAPEZOIDAL RULE

$$\int_{a}^{b} f(x)dx \equiv \frac{\Delta x}{2} \left[f(x_1) + 2f(x_2) + 2f(x_3) + \dots + 2f(x_n) + f(x_{n+1}) \right],$$

where $a = x_1, x_2, x_3, \dots, x_{n+1} = b$ subdivides [a, b] into n equal subintervals of length $\Delta x = \frac{b-a}{n}$.

THE SECOND DERIVATIVE TEST

Suppose f is a function of two variables x and y, and that all the second-order partial derivatives are continuous. Let

$$D = f_{xx}f_{yy} - (f_{xy})^2$$

and suppose (a, b) is a critical point of f.

- 1. If D(a,b) < 0, then f has a saddle point at (a,b),
- 2. If D(a,b) > 0 and $f_{xx}(a,b) < 0$, then f has a relative maximum at (a,b).
- 3. If D(a,b) > 0 and $f_{xx}(a,b) > 0$, then f has a relative minimum at (a,b).
- 4. If D(a, b) = 0, the test is inconclusive.

LAGRANGE EQUATIONS

For the function f(x,y) subject to the constraint g(x,y)=k, the Lagrange equations are

$$f_x = \lambda g_x$$
 $f_y = \lambda g_y$ $g(x, y) = k$

LEAST-SQUARES LINE

The equation of the least-squares line for the *n* points (x_1,y_1) , (x_2,y_2) , ..., (x_n,y_n) , is y=mx+b, where

$$m = \frac{n\sum xy - \sum x\sum y}{n\sum x^2 - (\sum x)^2} \qquad b = \frac{\sum x^2 \sum y - \sum x\sum xy}{n\sum x^2 - (\sum x)^2}$$

GEOMETRIC SERIES

If 0 < |r| < 1, then

$$\sum_{n=0}^{\infty} ar^n = \frac{a}{1-r}$$

TAYLOR SERIES

The Taylor series of f(x) about x = a is the power series

$$\sum_{n=0}^{\infty} a_n (x-a)^n \quad \text{where} \quad a_n = \frac{f^{(n)}(a)}{n!}$$

Examples:

$$e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$$
, for $-\infty < x < \infty$; $\ln x = \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} (x-1)^n$, for $0 < x \le 2$