

Derivative Formulas:

Constant $\frac{d}{dx}(c) = 0$, if c is a constant

Power Rule $\frac{d}{dx}(u^n) = nu^{n-1} \frac{du}{dx}$

Product Rule $\frac{d}{dx}(uv) = u \frac{dv}{dx} + v \frac{du}{dx}$

Quotient Rule $\frac{d}{dx} \left(\frac{u}{v} \right) = \frac{v \left(\frac{du}{dx} \right) - u \left(\frac{dv}{dx} \right)}{v^2}$

Chain Rule $\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$

Special Derivatives

Natural Logarithm

$$\frac{d}{dx}(\ln u) = \frac{1}{u} \frac{du}{dx}$$

Natural Exponential

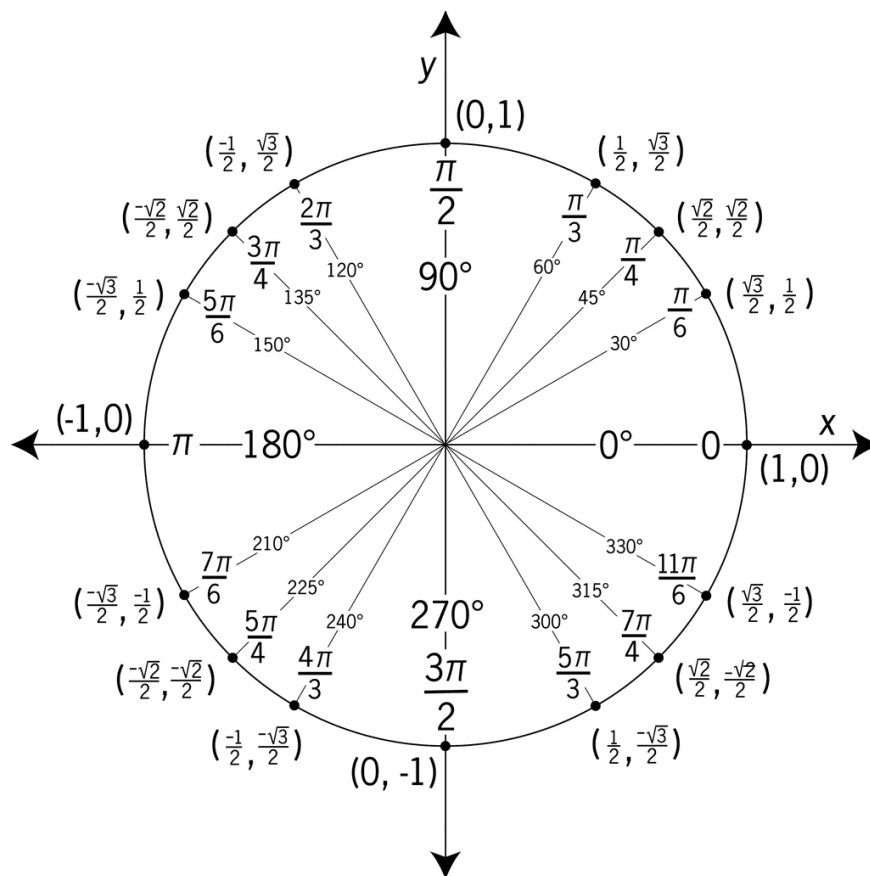
$$\frac{d}{dx}(e^u) = e^u \frac{du}{dx}$$

Logarithm

$$\frac{d}{dx}(\log_a u) = \frac{\log_a u}{u} \frac{du}{dx}$$

Exponential

$$\frac{d}{dx}(a^u) = a^u \ln a \frac{du}{dx}$$



Trigonometric Functions

$$\sin x = \frac{\text{opp}}{\text{hyp}}$$

$$\cos x = \frac{\text{adj}}{\text{hyp}}$$

$$\tan x = \frac{\text{opp}}{\text{adj}} = \frac{\sin x}{\cos x}$$

$$\csc x = \frac{\text{hyp}}{\text{opp}} = \frac{1}{\sin x}$$

$$\sec x = \frac{\text{hyp}}{\text{adj}} = \frac{1}{\cos x}$$

$$\cot x = \frac{\text{adj}}{\text{hyp}} = \frac{1}{\tan x} = \frac{\cos x}{\sin x}$$

Pythagorean Identities

$$\sin^2 x + \cos^2 x = 1$$

$$\tan^2 x + 1 = \sec^2 x$$

$$1 + \cot^2 x = \csc^2 x$$

Sum and Difference Identities

$$\sin(x + y) = \sin x \cos y + \cos x \sin y$$

$$\cos(x + y) = \cos x \cos y - \sin x \sin y$$

$$\tan(x + y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

$$\sin(x - y) = \sin x \cos y - \cos x \sin y$$

$$\cos(x - y) = \cos x \cos y + \sin x \sin y$$

$$\tan(x - y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$$

Double Angle Identities

$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

Half-Angle Identities

$$\sin^2 x = \frac{1}{2}(1 - \cos 2x)$$

$$\cos^2 x = \frac{1}{2}(1 + \cos 2x)$$

Derivatives of Trig Functions

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

Derivatives of Inverse Trig Functions

$$\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx}(\cos^{-1} x) = -\frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2}$$

$$\frac{d}{dx}(\csc^{-1} x) = -\frac{1}{x\sqrt{x^2-1}}$$

$$\frac{d}{dx}(\sec^{-1} x) = \frac{1}{x\sqrt{x^2-1}}$$

$$\frac{d}{dx}(\cot^{-1} x) = -\frac{1}{1+x^2}$$

Integrals of Trig Functions

$$\int \sin u \, du = -\cos u + C$$

$$\int \cos u \, du = \sin u + C$$

$$\int \tan u \, du = \ln |\sec u| + C$$

$$\int \csc u \, du = \ln |\csc u - \cot u| + C$$

$$\int \sec u \, du = \ln |\sec u + \tan u| + C$$

$$\int \cot u \, du = -\ln |\csc u| + C$$

Miscellaneous Trig Integrals

$$\int \sec^2 u \, du = \tan u + C$$

$$\int \sec u \tan u \, du = \sec u + C$$

$$\int \frac{du}{\sqrt{a^2 - u^2}} = \sin^{-1} \frac{u}{a} + C$$

$$\int \csc^2 u \, du = -\cot u + C$$

$$\int \csc u \cot u \, du = -\csc u + C$$

$$\int \frac{du}{a^2 + u^2} = \frac{1}{a} \tan^{-1} \frac{u}{a} + C$$
