MA 22400 – FINAL EXAM FORMULAS CONSUMERS' AND PRODUCERS' SURPLUS

$$CS = \int_0^{q_0} D(q)dq - p_0q_0 \qquad PS = p_0q_0 - \int_0^{q_0} S(q)dq$$
$$\frac{TRAPEZOIDAL RULE}{\int_a^b f(x)dx \equiv \frac{\Delta x}{2} \left[f(x_1) + 2f(x_2) + 2f(x_3) + \dots + 2f(x_n) + f(x_{n+1}) \right],$$

where $a = x_1, x_2, x_3, \dots, x_{n+1} = b$ subdivides [a, b] into n equal subintervals of length $\Delta x = -$

THE SECOND DERIVATIVE TEST

Suppose f is a function of two variables x and y, and that all the second-order partial derivatives are continuous. Let

$$D = f_{xx}f_{yy} - (f_{xy})^2$$

and suppose (a, b) is a critical point of f.

- 1. If D(a, b) < 0, then f has a saddle point at (a, b),
- 2. If D(a,b) > 0 and $f_{xx}(a,b) < 0$, then f has a relative maximum at (a,b).
- 3. If D(a,b) > 0 and $f_{xx}(a,b) > 0$, then f has a relative minimum at (a,b).
- 4. If D(a, b) = 0, the test is inconclusive.

LAGRANGE EQUATIONS

For the function f(x, y) subject to the constraint g(x, y) = k, the Lagrange equations are

$$f_x = \lambda g_x$$
 $f_y = \lambda g_y$ $g(x, y) = k$

LEAST-SQUARES LINE

The equation of the least-squares line for the *n* points (x_1,y_1) , (x_2,y_2) , ..., (x_n,y_n) , is y = mx + b, where

$$m = \frac{n\sum xy - \sum x\sum y}{n\sum x^2 - (\sum x)^2} \qquad b = \frac{\sum x^2 \sum y - \sum x\sum xy}{n\sum x^2 - (\sum x)^2}$$

GEOMETRIC SERIES

If 0 < |r| < 1, then

$$\sum_{n=0}^{\infty} ar^n = \frac{a}{1-r}$$

TAYLOR SERIES

The Taylor series of f(x) about x = a is the power series

$$\sum_{n=0}^{\infty} a_n (x-a)^n \quad \text{where} \quad a_n = \frac{f^{(n)}(a)}{n!}$$

Examples:

$$e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$$
, for $-\infty < x < \infty$; $\ln x = \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} (x-1)^n$, for $0 < x \le 2$

VOLUME & SURFACE AREA

Right Circular Cylinder	Sphere	Right Circular Cone
$V = \pi r^2 h$	$V = \frac{4}{3}\pi r^3$	$V = \frac{1}{3}\pi r^2 h$
$SA = \left\{ egin{array}{c} 2\pi r^2 + 2\pi rh \ \pi r^2 + 2\pi rh \end{array} ight.$	$SA = 4\pi r^2$	$SA = \pi r \sqrt{r^2 + h^2} + \pi r^2$