## Practice Problems

1. Evaluate $\int \frac{1}{(3 x-1)^{4}} d x$.
A. $-\frac{12}{(3 x-1)^{5}}+C$
B. $-\frac{1}{9(3 x-1)^{3}}+C$
C. $\frac{1}{(3 x-1)^{3}}+C$
D. $-\frac{1}{3(3 x-1)^{3}}+C$
E. $-\frac{4}{(3 x-1)^{5}}+C$
2. Evaluate $\int e^{3-2 x} d x$.
A. $-2 e^{3-2 x}+C$
B. $-\frac{1}{2} e^{3-2 x}+C$
C. $\frac{e^{4-2 x}}{4-2 x}+C$
D. $\frac{1}{3} e^{3-2 x}+C$
E. $\frac{e^{3-2 x}}{3-2 x}+C$
3. Find a function $f$ whose tangent line has slope $x \sqrt{5-x^{2}}$ for each value of $x$ and whose graph passes through the point $(2,10)$.
A. $f(x)=-\frac{1}{3}\left(5-x^{2}\right)^{3 / 2}$
B. $f(x)=\frac{2}{3}\left(5-x^{2}\right)^{3 / 2}+\frac{28}{3}$
C. $f(x)=\frac{1}{3}\left(5-x^{2}\right)^{3 / 2}+\frac{29}{3}$
D. $f(x)=-\frac{1}{3}\left(5-x^{2}\right)^{3 / 2}+\frac{31}{3}$
E. $f(x)=\frac{3}{2}\left(5-x^{2}\right)^{3 / 2}+\frac{17}{2}$
4. Evaluate $\int x \ln \left(x^{2}\right) d x$.
A. $\frac{1}{2} x^{2} \ln x^{2}-\frac{1}{2} x^{2}+C$
B. $\frac{1}{2} x^{2} \ln x^{2}-\frac{1}{2} x+C$
C. $\frac{1}{2} x^{2} \ln x^{2}-\frac{1}{6} x^{3}+C$
D. $x \ln x^{2}+\frac{1}{x}+C$
E. $\frac{1}{2} x^{2} \ln x-\frac{1}{2} x^{2}+C$
5. The area of the region bounded by the curves $y=x^{2}+1$ and $y=3 x+5$ is
A. $\frac{125}{6}$
B. $\frac{56}{3}$
C. $\frac{27}{2}$
D. $\frac{25}{6}$
E. $\frac{32}{3}$
6. If $f(x, y)=(x y+1)^{2}-\sqrt{y^{2}-x^{2}}$, evaluate $f(-2,1)$.
A. 1
B. $1-\sqrt{5}$
C. Not defined
D. $-1-\sqrt{5}$
E. $-1-\sqrt{3}$
7. A paint store carries two brands of latex paint. Sales figures indicate that if the first brand is sold for $x_{1}$ dollars per gallon and the second for $x_{2}$ dollars per gallon, the demand for the first brand will be $D_{1}\left(x_{1}, x_{2}\right)=100+5 x_{1}-10 x_{2}$ gallons per month and the demand for the second brand will be $D_{2}\left(x_{1}, x_{2}\right)=200-10 x_{1}+15 x_{2}$ gallons per month. Express the paint store's total monthly revenue, $R$, as a function of $x_{1}$ and $x_{2}$.
A. $R=x_{1} D_{1}\left(x_{1}, x_{2}\right)+x_{2} D_{2}\left(x_{1}, x_{2}\right)$
B. $R=D_{1}\left(x_{1}, x_{2}\right)+D_{2}\left(x_{1}, x_{2}\right)$
C. $R=D_{1}\left(x_{1}, x_{2}\right) D_{2}\left(x_{1}, x_{2}\right)$
D. $R=x_{2} D\left(x_{1}, x_{2}\right)+x_{1} D_{2}\left(x_{1}, x_{2}\right)$
E. $R=x_{1} x_{2}+D_{1}\left(x_{1}, x_{2}\right) D_{2}\left(x_{1}, x_{2}\right)$
8. Compute $\frac{\partial z}{\partial x}$, where $z=\ln (x y)$.
A. $\frac{1}{x}$
B. $\frac{1}{y}$
C. $\frac{1}{x y}$
D. $\frac{1}{x}+\frac{1}{y}$
E. $\frac{y}{x}$
9. Compute $f_{u v}$ if $f=u v+e^{u+2 v}$.
A. 0
B. $u+2 e^{u+2 v}$
C. $v+2 e^{u+2 v}$
D. $1+2 e^{u+2 v}$
E. $1+e^{u+2 v}$
10. Find and classify the critical points of $f(x, y)=(x-2)^{2}+2 y^{3}-6 y^{2}-18 y+7$.
A. $(2,3)$ saddle point; $(2,-1)$ relative minimum
B. $(2,3)$ relative maximum; $(2,-1)$ relative minimum
C. $(2,3)$ relative minimum; $(2,-1)$ relative maximum
D. $(2,3)$ relative maximum; $(2,-1)$ saddle point
E. $(2,3)$ relative minimum; $(2,-1)$ saddle point
11. A manufacturer sells two brands of foot powder, brand A and brand B. When the price of A is $x$ cents per can and the price of B is $y$ cents per can the manufacturer sells $40-8 x+5 y$ thousand cans of A and $50+9 x-7 y$ thousand cans of B . The cost to produce A is 10 cents per can and the cost to produce B is 20 cents per can. Determine the selling price of brand A which will maximize the profit.
A. 40 cents
B. 45 cents
C. 15 cents
D. 50 cents
E. 35 cents
12. Use increments to estimate the change in $z$ at $(1,3)$ if $\frac{\partial z}{\partial x}=2 x-4, \frac{\partial z}{\partial y}=2 y+7$, the change in $x$ is 0.3 and the change in $y$ is 0.5 .
A. 7.1
B. 2.9
C. 4.9
D. 5.9
E. 6.3
13. Using $x$ worker-hours of skilled labor and $y$ worker-hours of unskilled labor, a manufacturer can produce $f(x, y)=x^{2} y$ units. Currently 16 worker-hours of skilled labor and 32 workerhours of unskilled labor are used. If the manufacturer increases the unskilled labor by 10 worker-hours, use calculus to estimate the corresponding change that the manufacturer should make in the level of skilled labor so that the total output will remain the same.
A. Reduce by 4 hours.
B. Reduce by 10 hours.
C. Reduce by $\frac{5}{4}$ hours.
D. Reduce by $\frac{5}{2}$ hours.
E. Reduce by 5 hours.
14. Find the maximum value of the function $f(x, y)=20 x^{3 / 2} y$ subject to the constraint $x+y=60$. Round your answer to the nearest integer.
A. 84,654
B. 188,334
C. 4,320
D. 259,200
E. 103,680
15. Evaluate $\int_{1}^{2} \int_{0}^{1}(2 x+y) d y d x$.
A. $\frac{9}{2}$
B. $\frac{5}{2}$
C. $\frac{3}{2}$
D. $\frac{7}{2}$
E. $\frac{1}{2}$
16. The general solution of the differential equation $\frac{d y}{d x}=2 y+1$ is:
A. $x=y^{2}+y+C$
B. $2 y+1=C e^{2 x}$
C. $y=2 x y+x+C$
D. $y=C e^{2 x}-2 y-1$
E. $y=C e^{2 x}$
17. The value, $V$, of a certain $\$ 1500$ IRA account grows at a rate equal to $13.5 \%$ of its value. Its value after $t$ years is:
A. $V=1500 e^{-0.135 t}$
B. $V=1500+0.135 t$
C. $V=1500 e^{0.135 t}$
D. $V=1500(1+0.135 t)$
E. $V=1500 \ln (0.135 t)$
18. It is estimated that $t$ years from now the population of a certain town will be increasing at a rate of $5+3 t^{2 / 3}$ hundred people per year. If the population is presently 100,000 , by how many people will the population increase over the next 8 years?
A. 100
B. 9,760
C. 6,260
D. 24,760
E. 17,260
19. Calculate the improper integral $\int_{0}^{\infty} x e^{-x^{2}} d x$.
A. $-\frac{1}{2}$
B. 1
C. $\frac{1}{2}$
D. $\frac{5}{2}$
E. The integral diverges.
20. An object moves so that its velocity after $t$ minutes is given by the formula $v=20 e^{-0.01 t}$. The distance it travels during the 10th minute is
A. $\int_{0}^{10} 20 e^{-0.01 t} d t$
B. $\int_{9}^{10}\left(-20 e^{-0.01 t}\right) d t$
C. $\int_{0}^{10}\left(-20 e^{-0.01 t}\right) d t$
D. $\int_{9}^{10} 20 e^{-0.01 t} d t$
E. $\int_{9}^{10}\left(-0.2 e^{-0.01 t}\right) d t$
21. Find the sum of the series $\sum_{n=1}^{\infty}\left(-\frac{2}{3}\right)^{n}$.
A. $\frac{2}{5}$
B. $-\frac{2}{5}$
C. $\frac{3}{2}$
D. $-\frac{3}{2}$
E. The series diverges.
22. Use a Taylor polynomial of degree 2 to approximate $\int_{0}^{0.1} \frac{100}{x^{2}+1} d x$. Round your answer to five decimal places.
A. 9.96687
B. 10.00000
C. 9.96677
D. 9.66667
E. 9.96667
23. Find the radius of convergence of the power series $\sum_{n=0}^{\infty} \frac{n 3^{n} x^{n}}{5^{n+1}}$.
A. $\frac{5}{3}$
B. 1
C. $\frac{3}{25}$
D. $\frac{3}{5}$
E. $\infty$
24. Find the Taylor series of $f(x)=\frac{x}{2+x^{2}}$ at $x=0$.
A. $\sum_{n=0}^{\infty} \frac{x^{n+1}}{2^{n+1}}$
B. $\sum_{n=0}^{\infty} \frac{(-1)^{n} x^{2 n+1}}{2^{n}}$
C. $\sum_{n=0}^{\infty}(-1)^{n} 2^{n-1} x^{2 n+1}$
D. $\sum_{n=0}^{\infty} \frac{x^{2 n}}{2^{n-1}}$
E. $\sum_{n=0}^{\infty} \frac{(-1)^{n} x^{2 n+1}}{2^{n+1}}$
25. Write the following infinite series in summation notation.

$$
5-\frac{7}{8}+\frac{9}{27}-\frac{11}{64}+\ldots
$$

A. $\sum_{n=1}^{\infty}(-1)^{n+1} \frac{2 n+5}{n^{3}}$
B. $\sum_{n=1}^{\infty}(-1)^{n+1} \frac{2 n+3}{n^{3}}$
C. $\sum_{n=1}^{\infty}(-1)^{n+1} \frac{3 n+2}{n^{3}}$
D. $\sum_{n=1}^{\infty}(-1)^{n} \frac{2 n+5}{2^{n}}$
E. $\sum_{n=1}^{\infty}(-1)^{n} \frac{2 n+3}{2^{n}}$
26. Determine which of the following series converge.
I. $\sum_{k=2}^{\infty} \frac{k^{2}}{5^{k}}$
II. $\sum_{k=3}^{\infty} \frac{(3 k+1) \pi^{2 k}}{10^{k+1}}$
III. $\sum_{k=1}^{\infty} \frac{k!}{(-2)^{k}}$
A. III
B. I \& II
C. I \& III
D. II \& III
E. II
27. Find the Taylor series about $x=0$ for the indefinite integral

$$
\int x e^{-x^{3}} d x .
$$

A. $\sum_{n=0}^{\infty} \frac{1}{n!(3 n+1)} x^{3 n+2}+C$
B. $\sum_{n=0}^{\infty} \frac{(-1)^{n}}{n!(3 n+2)} x^{3 n+2}+C$
C. $\sum_{n=0}^{\infty} \frac{(-1)^{n}}{n!(3 n+1)} x^{3 n+2}+C$
D. $\sum_{n=0}^{\infty} \frac{1}{n!(3 n+2)} x^{3 n+2}+C$
E. $\sum_{n=0}^{\infty} \frac{(-1)^{n}}{n!(3 n+1)} x^{3 n+1}+C$
28. A patient is given an injection of 50 milligrams of a drug every 24 hours. After $t$ days, the fraction of the drug remaining in the patient's body is

$$
f(t)=2^{-t / 3} .
$$

If the treatment is continued indefinitely, approximately how many milligrams of the drug will eventually be in the patient's body just prior to an injection?
A. 202.7
B. 152.7
C. 305.4
D. 242.4
E. 192.4
29. Compute $\int(\sin x-\cos x)(\sin x+\cos x)^{5} d x$.
A. $\frac{1}{6}(-\cos x+\sin x)^{6}+C$
B. $-6(-\cos x+\sin x)^{6}+C$
C. $-\frac{1}{6}(\sin x+\cos x)^{6}+C$
D. $6(\sin x+\cos x)^{6}+C$
E. $\frac{1}{6}(\sin x+\cos x)^{6}+C$
30. Evaluate $\int x^{2} \cos (-5 x) d x$.
A. $-\frac{1}{5} x^{2} \sin (-5 x)+\frac{2}{25} x \cos (-5 x)+\frac{2}{125} \sin (-5 x)+C$
B. $\frac{1}{5} x^{2} \sin (-5 x)-\frac{2}{25} x \cos (-5 x)-\frac{2}{125} \sin (-5 x)+C$
C. $-5 x^{2} \sin (-5 x)+50 x \cos (-5 x)+250 \sin (-5 x)+C$
D. $5 x^{2} \cos (-5 x)-50 x \sin (-5 x)-250 \cos (-5 x)+C$
E. $5 x^{2} \sin (-5 x)-50 x \cos (-5 x)-250 \sin (-5 x)+C$
31. Evaluate $\int_{e}^{5} \frac{\ln \left(x^{4}\right)}{x} d x$.
A. $\frac{1}{8}\left(25-e^{2}\right)$
B. $2\left(25-e^{2}\right)$
C. $2(\ln 5)^{2}-2$
D. $\frac{1}{8}(\ln 5)^{2}-\frac{1}{8}$
E. $\ln (25)-2$
32. Find the volume of the solid generated by revolving the region bounded by:

$$
y=3 e^{2 x}, y=0, x=1, \text { and } x=3
$$

about the x -axis.
A. $\frac{3 \pi}{4}\left(e^{8}-1\right) e^{4}$
B. $\frac{3 \pi}{4}\left(e^{8}-1\right) e^{2}$
C. $\frac{9 \pi}{2}\left(e^{4}-1\right) e^{2}$
D. $\frac{9 \pi}{4}\left(e^{8}-1\right) e^{4}$
E. $\frac{3 \pi}{2}\left(e^{4}-1\right) e^{2}$
33. Find the volume of the solid which has square cross-sections with side length $5 x^{2}$ at each point $2 \leq x \leq 4$.
A. $\int_{2}^{4} 5 \pi x^{2} d x$
B. $\int_{2}^{4} 5 x^{2} d x$
C. $\int_{2}^{4} 5 x^{4} d x$
D. $\int_{2}^{4} 25 \pi x^{4} d x$
E. $\int_{2}^{4} 25 x^{4} d x$
34. The velocity of a car over the time period $0 \leq t \leq 3$ is given by the function

$$
v(t)=60 t e^{\frac{-t}{4}}
$$

miles per hour, where $t$ is time in hours. What was the distance the car traveled in the first 90 minutes? Round your answer to two decimal places.
A. 166.42 miles
B. 156.19 miles
C. 126.63 miles
D. 75.85 miles
E. 52.78 miles
35. Given that $f(x, y)=\tan \left(x y^{3}\right)$, compute $f_{x}\left(2 \pi, \frac{1}{2}\right)$.
A. $\frac{3}{2}$
B. $\frac{\pi}{2}$
C. 1
D. $6 \pi$
E. $\frac{1}{4}$
36. Let $h(x, y)=y \sin (x y)$. Find $\frac{\partial^{2} h}{\partial y \partial x}$.
A. $-2 x y \sin (x y)$
B. $2 y \cos (x y)-x y^{2} \sin (x y)$
C. $-y^{3} \sin (x y)$
D. $\cos (x y)+y^{2} \sin (x y)$
E. $(x+1) \cos (x y)-x^{2} y \sin (x y)$
37. A nature preserve wishes to construct a large compound which will hold both lions and gazelles. They currently have 6 gazelles. They estimate that if they use an area of $A$ square miles and introduce $L$ lions, then they will be able to support a population of $G$ gazelles, given by the function

$$
G(A, L)=6+40 A-A^{2}-18 L^{2}+176 L-8 A L
$$

What conditions will lead to the largest number of gazelles?
A. $L=3, A=5$
B. $L=4, A=4$
C. $L=5, A=4$
D. $L=5, A=3$
E. There are no such conditions because the function does not have a maximum.
38. Evaluate $\iint_{R}\left(e^{x^{2}+1}\right) d A$, where $R$ is the region indicated by the boundaries below:

$$
0 \leq x \leq 1 ; \quad 0 \leq y \leq x
$$

A. 0
B. $\frac{1}{2} e$
C. $\frac{1}{2} e^{2}$
D. $\frac{1}{2}\left(e^{2}-e\right)$
E. $e^{2}-e$
39. Compute $A B$ and $B A$, if possible, for the matrices:

$$
A=\left[\begin{array}{ll}
2 & -1 \\
0 & -3
\end{array}\right] \text { and } B=\left[\begin{array}{cc}
0 & 1 \\
-5 & 1 \\
2 & 0
\end{array}\right]
$$

A. $B A$ is not possible, and $A B=\left[\begin{array}{cc}-1 & -3 \\ -11 & -3 \\ 4 & 0\end{array}\right]$
B. $B A$ is not possible, and $A B=\left[\begin{array}{ccc}-1 & -11 & 4 \\ -3 & -3 & 0\end{array}\right]$
C. $A B$ is not possible, and $B A=\left[\begin{array}{cc}0 & -3 \\ -10 & 2 \\ 4 & -2\end{array}\right]$
D. $A B$ is not possible, and $B A=\left[\begin{array}{ccc}0 & -10 & 4 \\ -3 & 2 & -2\end{array}\right]$
E. Both $A B$ and $B A$ are not possible.
40. Find the general solution to the differential equation

$$
-x^{5} \sin x+x y^{\prime}=3 y, \quad x>0
$$

A. $y=-x \cos x-\sin x+C$
B. $y=-x \cos x+\sin x+C$
C. $y=x \cos x+\sin x+C$
D. $y=-x^{4} \cos x+x^{3} \sin x+C x^{3}$
E. $y=x^{4} \cos x+x^{3} \sin x+C x^{3}$
41. The amount of carbon, in grams, in a sample of soil is given by a function, $F(t)$, satisfying the differential equation:

$$
F^{\prime}+a F-b=0
$$

where $a$ and $b$ are constants, and time, $t$, is measured in years. If the sample originally contains 10 grams of carbon, which expression represents the amount of carbon present after 5 years?
A. $\frac{b}{a}+\left(10-\frac{b}{a}\right) e^{5 a}$
B. $\frac{b}{a}+\left(10-\frac{b}{a}\right) e^{-5 a}$
C. $a b+(10-a b) e^{-5 a}$
D. $a b+(10-a b) e^{5 a}$
E. $\frac{b}{a}+10 e^{5 a}$
42. Let $M=\left[\begin{array}{cc}4 & 3 \\ -2 & -1\end{array}\right]$. Compute $3 M-M^{2}$.
A. $\left[\begin{array}{ll}2 & 0 \\ 0 & 2\end{array}\right]$
B. $\left[\begin{array}{ll}2 & 1 \\ 0 & 2\end{array}\right]$
C. $\left[\begin{array}{cc}2 & 0 \\ -1 & 2\end{array}\right]$
D. $\left[\begin{array}{ll}2 & 1 \\ 1 & 2\end{array}\right]$
E. $\left[\begin{array}{cc}2 & -1 \\ 1 & 2\end{array}\right]$
43. Write the following augmented matrix in reduced row-echelon form.

$$
\left[\begin{array}{ccc|c}
2 & -3 & 2 & 1 \\
1 & -6 & 1 & 2 \\
-1 & -3 & -1 & 1
\end{array}\right]
$$

A. $\left[\begin{array}{lll|c}1 & 0 & 1 & 0 \\ 0 & 1 & 0 & -\frac{1}{3} \\ 0 & 0 & 0 & 0\end{array}\right]$
B. $\left[\begin{array}{lll|c}1 & 0 & 0 & 1 \\ 0 & 1 & 0 & -\frac{1}{3} \\ 0 & 0 & 1 & 0\end{array}\right]$
$\mathrm{C}\left[\begin{array}{ccc|c}1 & 0 & 0 & 1 \\ 0 & 1 & 0 & -\frac{1}{3} \\ 0 & 0 & 0 & 0\end{array}\right]$
$\mathrm{D}\left[\begin{array}{ccc|c}1 & 0 & 1 & 0 \\ 0 & 1 & 0 & -\frac{1}{3} \\ 0 & 0 & 1 & 0\end{array}\right]$
E. $\left[\begin{array}{lll|c}1 & 0 & 1 & 0 \\ 0 & 0 & 0 & -\frac{1}{3} \\ 0 & 1 & 0 & 0\end{array}\right]$
44. Find all the eigenvalues of the matrix $\left[\begin{array}{cc}9 & 20 \\ -6 & -13\end{array}\right]$.
A. -5 and 2
B. -3 and -1
C. -4 and 0
D. 3 and 7
E. 2 and -2
45. Find the determinant of the matrix $A$, and determine if $A$ is invertible.

$$
A=\left[\begin{array}{ccc}
1 & 2 & 3 \\
0 & 1 & 2 \\
2 & -3 & 1
\end{array}\right]
$$

A. $A$ is not invertible because $\operatorname{det}(A)=9$.
B. $A$ is invertible because $\operatorname{det}(A)=9$.
C. $A$ is not invertible because $\operatorname{det}(A)=-9$.
D. $A$ is invertible because $\operatorname{det}(A)=-9$.
E. $A$ is not invertible because $\operatorname{det}(A)=0$.
46. The inverse of a certain Leslie matrix

$$
G=\left[\begin{array}{cc}
1 / 2 & 2 \\
1 / 2 & 1 / 2
\end{array}\right]
$$

is

$$
G^{-1}=\left[\begin{array}{cc}
-2 / 3 & 8 / 3 \\
2 / 3 & -2 / 3
\end{array}\right] .
$$

If the population vector in year $\mathbf{2}$ is $p_{2}=\left[\begin{array}{c}\text { hatchlings } \\ \text { adults }\end{array}\right]=\left[\begin{array}{c}129 \\ 72\end{array}\right]$, then the population vector in year 1, $p_{1}=\left[\begin{array}{c}\text { hatchlings } \\ \text { adults }\end{array}\right]=$
A. $\left[\begin{array}{cc}-2 / 3 & 8 / 3 \\ 2 / 3 & -2 / 3\end{array}\right]\left[\begin{array}{c}129 \\ 72\end{array}\right]$
B. $\left[\begin{array}{cc}1 / 2 & 2 \\ 1 / 2 & 1 / 2\end{array}\right]\left[\begin{array}{c}129 \\ 72\end{array}\right]$
C. $\left[\begin{array}{cc}-2 / 3 & 8 / 3 \\ 2 / 3 & -2 / 3\end{array}\right]\left[\begin{array}{cc}1 / 2 & 2 \\ 1 / 2 & 1 / 2\end{array}\right]\left[\begin{array}{c}129 \\ 72\end{array}\right]$
D. $\left[\begin{array}{cc}1 / 2 & 2 \\ 1 / 2 & 1 / 2\end{array}\right]\left[\begin{array}{cc}-2 / 3 & 8 / 3 \\ 2 / 3 & -2 / 3\end{array}\right]\left[\begin{array}{c}129 \\ 72\end{array}\right]$
E. $\left(\left[\begin{array}{cc}-2 / 3 & 8 / 3 \\ 2 / 3 & -2 / 3\end{array}\right]+\left[\begin{array}{cc}1 / 2 & 2 \\ 1 / 2 & 1 / 2\end{array}\right]\right)\left[\begin{array}{c}129 \\ 72\end{array}\right]$
47. Which of the following are eigenvectors of the matrix $\left[\begin{array}{ll}0 & 6 \\ 1 & 1\end{array}\right]$ ?
I. $\left[\begin{array}{c}-3 \\ 1\end{array}\right]$
II. $\left[\begin{array}{l}3 \\ 3\end{array}\right]$
III. $\left[\begin{array}{l}-2 \\ -1\end{array}\right]$
A. I only
B. II only
C. I and II only
D. I and III only
E. II and III only

## Answers to Practice Problems

| 1. B | 2. B | 3. D | 4. A |
| :---: | :---: | :---: | :---: |
| 5. A | 6. C | 7. A | 8. A |
| 9. D | 10. E | 11. A | 12. D |
| 13. D | 14. E | 15. D | 16. B |
| 17. C | 18. B | 19. C | 20. D |
| 21. B | 22. E | 23. A | 24. E |
| 25. B | 26. B | 27. B | 28. E |
| 29. C | 30. A | 31. C | 32. D |
| 33. E | 34. E | 35. E | 36. B |
| 37. B | 38. D | 39. C | 40. D |
| 41. B | 42. A | 43. A | 44. B |
| 45. B | 46. A | 47. D |  |

