

MA 15910 Review Worksheet for Exam 2, Spring 2015

1) Complete the table below, then use it to approximate

$$\lim_{x \rightarrow -1} f(x), \text{ where } f(x) = \frac{2x^3 + 3x^2 - 4x - 5}{x + 1}.$$

x	-1.1	-1.01	-1.001	-0.999	-0.99	-0.9
$f(x)$						

2) Find the limit values if they exist.

a) $\lim_{x \rightarrow 3} \left(\frac{x^2 + 2x - 15}{x^2 + x - 12} \right)$

b) $\lim_{z \rightarrow 0} \left(\frac{\frac{-1}{z+2} + \frac{1}{2}}{z} \right)$

c) $\lim_{x \rightarrow 16} \left(\frac{\sqrt{x} - 4}{x - 16} \right)$

d) $\lim_{x \rightarrow \infty} \left(\frac{2x^3 - 5x^2 + 9x}{3x^3 - 4x} \right)$

e) $\lim_{x \rightarrow -\infty} \left(\frac{2x^2 - 5}{3x^3 + 2x} \right)$

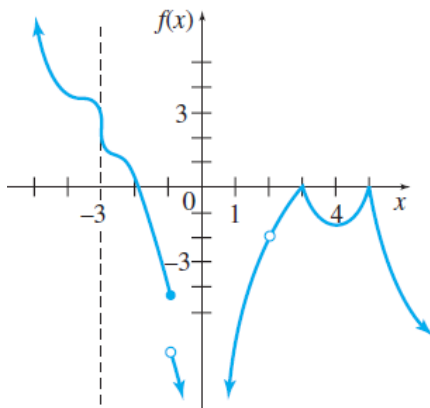
3) Find the average rate of change for each function over the given interval.

a) $y = -4x^2 - 6$ $[2, 6]$ b) $y = \sqrt{3x - 2}$ $[1, 6]$

4) Suppose the position of an object moving in a straight line is given by $s(t) = t^2 + 5t + 2$. Find the instantaneous velocity when $t = 5$.

5) Suppose the total profit in hundreds of dollars from selling x items is given by $P(x) = 2x^2 - 4x + 5$. (a) Find the average rate of change of profit for the changes for 2 to 5 items. (b) Find the instantaneous rate of change of profit when $x = 2$.

6) For what x values would the function graphed below not have derivatives.



7) The revenue in dollars generated from the sale of x items is given by $R(x) = 10x - \frac{x^2}{100}$.

(a) Find the marginal revenue when 500 items have been sold. (b) Estimate the revenue from the sale of the 601st item by finding $R'(600)$.

Find the derivative of each. (8 – 13)

8) $y = 3x^5 - 6x^3 + \frac{1}{2}x^2 - 2x$

9) $f(x) = 10x^{-4} - \frac{7}{x^3} + 3x$

10) $g(x) = (2x^2 - 5)^2$

11) $y = (3x^2 + 1)(2x^2 - 4x + 3)$

12) $q(x) = \frac{x^2 + 7x - 2}{x^2 - 2}$

13) $r(x) = \sqrt{5x^3 - 4x^2}$

14) Find $f'(2)$ if $f(x) = x^4 - \frac{4}{3}x^3 + 2x^2 - 5x + 8$.

15) Find all points on the graph of $g(x) = x^3 + 9x^2 + 19x - 10$ where the slope of the tangent line is -5.

6) Find an equation of the line tangent to the graph of $f(x) = \frac{x}{x-2}$ at the point (3,3).

17) Assume that the total number (in millions) of bacteria present in a culture at t hours is given by $N(t) = 4t^2(t-20)^2 + 20$. Find the rate at which the population of bacteria is changing at 5 hours and at 8 hours.