

ANSWERS TO PRACTICE FOR FINAL MA13900

1. b) 9

c) 9

d) 16

2. b) 12

c) 8

d) 18

3. a) The base of the pyramid is a dodecagon.

b) 24

c) 13

4. a) The base of the prism is a heptagon

b) 14

c) 9

5. Drawing

6. Drawing

7. a) 46 faces

b) No. If that were the case because of Euler's Formula it would have 4 vertices. In which case it would HAVE to be a Tetrahedron, but this does not have 71 faces.

8.

Tetrahedron (Four TRIANGULAR faces)

Octahedron (Eight TRIANGULAR faces)

Icosahedron (Twenty TRIANGULAR faces)

Cube (Six SQUARE faces)

Dodecahedron (Twelve PENTAGONAL faces)

9. a) Two

b) Seven

10.  $900^\circ$ .

11. a)  $1260^\circ$

b)  $140^\circ$

c) 27 diagonals

12. a)  $1440^\circ$

b)  $144^\circ$

c) 35 diagonals

d) 10 lines of symmetry.

ANSWERS TO PRACTICE FOR FINAL MA13900

e) 10 rotational symmetries.  $36^\circ$  ,  $72^\circ$  ,  $108^\circ$  ,  $144^\circ$  ,  $180^\circ$  ,  $216^\circ$  ,  $252^\circ$  ,  $288^\circ$  ,  $324^\circ$  ,  $360^\circ$ .

13. a) 4 planes of symmetry

b) One, line through the apex and the center of the square in the base.

c) Four rotational symmetries.

14. a) 6 planes of symmetry

b) 4 axis of rotation

c) 9 rotational symmetries.

15. a) 7 planes of symmetry.

b) 7 axis of rotation. One through the center of both hexagonal bases. Three through the centers of opposite lateral rectangular faces. Three through the midpoints of opposite lateral edges

c) 12 rotational symmetries

16. a)  $50,000 \text{ cm}^3$ .

b) 4%

17. a) larger than

b) as large as

c) as large as

d) as large as

e) larger than

18. a) 108

b)  $2/3$

c) 70

d) 155

e) 40

19. Drawing.

20. Drawing.

21. a) Rotation and Translation

b) Reflection and Glide-Reflection.

22. a) Same Orientation.

b) Different Orientation

c) Same Orientation.

d) Same Orientation.

e) Different Orientation.

f) Same Orientation.

ANSWERS TO PRACTICE FOR FINAL MA13900

23. Drawing

24. Drawing

25. Drawing

26. Drawing.

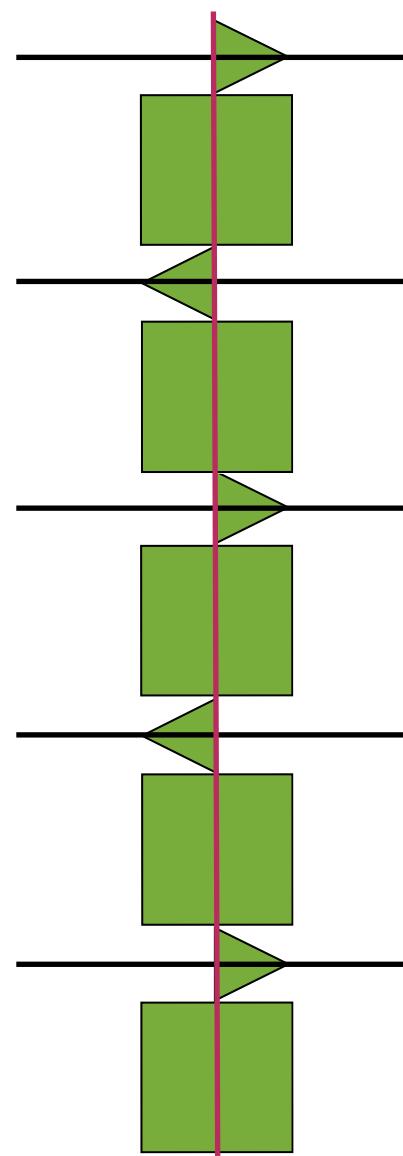
27.

**Rotational symmetries:**  $180^\circ$  around the center of any square.

**Reflection symmetries:** The horizontal lines of symmetries for the triangles. (In black)

**Translation symmetries:** Move any triangle an even number of triangles up or down.

**Glide-Reflection symmetries:** Move any square an odd number of triangles up or down, then reflect on red line.



ANSWERS TO PRACTICE FOR FINAL MA13900

- 28.** a) 1 kiki > 1 qij  
b) 1 rof > 1 wak  
c) 1 vay > 1 yal  
d) 1 gur > 1 tep

- 29.** a)  $y > x$   
b)  $x > y$   
c)  $x > y$   
d)  $x > y$

- 30.** a) 9 fab  
b)  $48/5 \pi r$  or  $1.5 \pi r^2$   
c)  $250/24 \pi r^2$   
d)  $64/5 \pi r^2$

- 31.** a) 23,000 m  
b) 0.0250 m<sup>2</sup>.  
c) 9 yd<sup>3</sup>.  
d) 3,312 in<sup>2</sup>.

- 32.** a) 20.25 in, 49.5 in  
b) 139.50 in  
c) 20.75 in, 50.5 in  
d) 1,047.875 in<sup>2</sup>.

- 33.** a)  $\frac{2000\pi}{3}$  dm<sup>3</sup>.  
b) The cylinder has bigger surface area.

- 34.** a) 13 cm  
b) 36 cm<sup>2</sup>.

- 35.** a)  $\sqrt{220}$  cm or  $2\sqrt{55}$  cm  
b)  $3\sqrt{220}$  cm<sup>2</sup>, or  $6\sqrt{55}$  cm<sup>2</sup>.

**36.** 18 rooms

**37.**

- Net 1: This is not a net for any polyhedra.  
Net 2: This is a net for a regular pyramid. It is also a net for a regular tetrahedron.  
Net 3: This is not a net for any polyhedra.  
Net 4: This is a net for a pyramid. But it is not a net for a regular pyramid.  
Net 5: This is a net for a regular polyhedron (A cube)  
Net 6: This is a net for a regular pyramid.  
Net 7: This is not a net for any polyhedra.

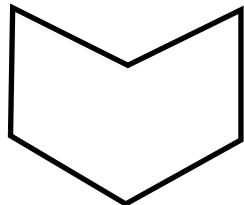
ANSWERS TO PRACTICE FOR FINAL MA13900

Net 8: This is a net for a regular pyramid. It is also a net for a regular tetrahedron.

Net 9: This is not a net for any polyhedra.

Net 10: This is a net for a regular pyramid.

- 38.a) Yes, regular hexagons tessellate the plane.  
b)



39. a) Tessellates

b) Tessellates.

c) Does not tessellate.

d) Tessellates.

e) Tessellates.

f) Does not tessellate.

40. a) Possible.

b) Not possible. Regular octagons are equiangular always.

c) Possible

d) Possible (this is a Rhombus)

e) Not possible. If it is a regular decagon, all interior angles are  $144^\circ$ , so no angle is bigger than  $180^\circ$ , hence it cannot be concave.

f) A square.

g) A rectangle

h) Impossible, the base of a cube is a square (which is also a rectangle), and a cube is a right prism. So it is a right rectangular prism.

i) See 38 b)

j) Impossible, regular tetrahedra are always regular pyramids.

k) Possible.

l) Impossible. If the base of a prism tessellates the plane (and triangles tessellate the plane), then the prism tessellates the space.

41. a) 7 lines of symmetry

b) 7 rotational symmetries.

42. I. 4 lines of symmetry. 4 rotational symmetries  $90^\circ, 180^\circ, 270^\circ, 360^\circ$ .

II. 3 lines of symmetry. 3 rotational symmetries  $120^\circ, 240^\circ, 360^\circ$ .

III. 1 line of symmetry. No rotational symmetries.

IV. 2 lines of symmetry. 2 rotational symmetries  $180^\circ, 360^\circ$ .

43. a) DRE and EAM

ANSWERS TO PRACTICE FOR FINAL MA13900

- b) Because their corresponding angles are congruent  
c) 4 in.

44.  $16\text{cm}^2$ .

45. a)  $4\text{m}^2$ .  
b) 30 m.

46. a) They are parallel.  
b)  $24/5$  or  $4.8 \text{ cm}$ .

47. a) Top sides are 5 cm each. All angles where diagonals cross are right. The shortest diagonal is bisected in two segments that are 3 cm each. The angle at the bottom is bisected in two congruent angles  $40^\circ$  each.

- b) All sides are 10 in. The big angles are bisected in two congruent angles  $60^\circ$  each. The small angles are bisected in two congruent angles  $30^\circ$  each. The smaller diagonal is bisected in two segments that are 5 in each. The longer diagonal is bisected in two segments that are  $\sqrt{75}$  in or  $5\sqrt{3}$  in each.
- c) Base is 7 cm. Lower bottom angle is  $40^\circ$ , top right angle is  $110^\circ$ , top left angle is cut in a lower angle that is  $70^\circ$ , and upper angle that is  $40^\circ$ .
- d) Top side is 8 cm, left and right side are both  $\sqrt{260}$  cm or  $2\sqrt{65}$  cm. All angles are right.

48. Unit I: 2.5

Unit II: 7.5

49.  $x = 20^\circ$ ,  $y = 35^\circ$ ,  $z = 55^\circ$ ,  $v = 35^\circ$ .

50. a)  $128\pi/3 \text{ cm}^3$ .  
b)  $48\pi \text{ cm}^2$ .

51. a) 6 cm  
b) 10 cm  
c)  $\sqrt{91}$  cm  
d)  $54\sqrt{3} \text{ cm}^2$  or  $18\sqrt{27} \text{ cm}^2$ .  
e)  $54\sqrt{3} + 18\sqrt{91} \text{ cm}^2$  or  $18\sqrt{27} + 18\sqrt{91} \text{ cm}^2$ .  
f)  $144\sqrt{2} \text{ cm}^3$  or  $48\sqrt{27} \text{ cm}^3$ .