## THE SECOND DERIVATIVE TEST

Suppose $f$ is a function of two variables $x$ and $y$, and that all the second-order partial derivatives are continuous. Let

$$
d=f_{x x} f_{y y}-\left(f_{x y}\right)^{2}
$$

and suppose $(a, b)$ is a critical point of $f$.

1. If $d(a, b)>0$ and $f_{x x}(a, b)>0$, then $f$ has a relative minimum at $(a, b)$.
2. If $d(a, b)>0$ and $f_{x x}(a, b)<0$, then $f$ has a relative maximum at $(a, b)$.
3. If $d(a, b)<0$, then $f$ has a saddle point at $(a, b)$.
4. If $d(a, b)=0$, the test is inconclusive.

## LAGRANGE EQUATIONS

For the function $f(x, y)$ subject to the constraint $g(x, y)=c$, the Lagrange equations are

$$
f_{x}=\lambda g_{x} \quad f_{y}=\lambda g_{y} \quad g(x, y)=c
$$

GEOMETRIC SERIES
If $0<|r|<1$, then

$$
\sum_{n=0}^{\infty} a r^{n}=\frac{a}{1-r}
$$

VOLUME \& SURFACE AREA

| Right Circular Cylinder | Sphere | Right Circular Cone |
| :--- | :--- | :--- |
| $V=\pi r^{2} h$ | $V=\frac{4}{3} \pi r^{3}$ | $V=\frac{1}{3} \pi r^{2} h$ |
| $S A=\left\{\begin{array}{ll}2 \pi r^{2}+2 \pi r h & S A=4 \pi r^{2} \\ \pi r^{2}+2 \pi r h & \end{array}\right)$ |  |  |

Right Circular Cylinder $V=\pi r^{2} h$
$S A=\left\{\begin{array}{l}2 \pi r^{2}+2 \pi r h \\ \pi r^{2}+2 \pi r h\end{array}\right.$

Sphere
Right Circular Cone
$V=\frac{1}{3} \pi r^{2} h$
$S A=\pi r \sqrt{r^{2}+h^{2}}+\pi r^{2}$

