

MA 16200 Exam II, Oct 19, 2017

Name \_\_\_\_\_

10-digit PUID number \_\_\_\_\_

Recitation Instructor \_\_\_\_\_

Recitation Section Number and Time \_\_\_\_\_

Instructions: **MARK TEST NUMBER 13 ON YOUR SCANTRON**

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2. Fill in all the information requested above and on the scantron sheet. On the scantron sheet fill in the little circles for your name, section number and PUID.
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9. Some useful formulas:

$$\sin(a + b) = \sin a \cos b + \cos a \sin b$$

$$\cos(a + b) = \cos a \cos b - \sin a \sin b$$

$$1 - \cos 2a = 2 \sin^2 a$$

$$1 + \cos 2a = 2 \cos^2 a$$

$$\int \sec x \tan x \, dx = \sec x + C \quad \int \sec^2 x \, dx = \tan x + C$$

$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right) + C \quad \int \frac{1}{\sqrt{x^2 - a^2}} dx = \sin^{-1} \left( \frac{x}{a} \right) + C$$

## Questions

1.  $\int_0^{3/2} \frac{1}{4y^2 + 9} dy =$

- A.  $\pi/6$
- B.  $3\pi/16$
- C.  $\pi/24$
- D.  $\pi/12$
- E.  $2\pi/9$

2.  $\int_2^{\infty} \frac{2+u}{u^2} du =$

- A. 1
- B. 2
- C.  $1/2$
- D. The integral is divergent
- E.  $\ln 2$

3. Find the  $x$ -coordinate,  $\bar{x}$ , of the centroid for the region bounded by  $y = 2x$  and  $y = x^2$ .

- A.  $2/3$
- B.  $5/3$
- C.  $2$
- D.  $3/2$
- E.  $1$

4. Consider the two series

$$\sum_{n=0}^{\infty} \frac{n^2 - 1}{3n^4 + 1}, \quad \sum_{n=0}^{\infty} \frac{1}{\sqrt{n^2 + 1}}.$$

- A. Both are convergent
- B. Both are divergent
- C. The first one is convergent while the second one is divergent
- D. The first one is divergent while the second one is convergent
- E. None of the above

5. Find the length of the curve  $y = f(x)$  from  $x = 0$  to  $x = \pi/3$ , given its derivative  $f'(x) = \sqrt{\sec^2 x \tan^2 x - 1}$ .

- A. 2
- B.  $\sqrt{3}/3$
- C. 4
- D.  $\sqrt{2}$
- E. 1

6. The area of the surface obtained by revolving the curve  $y = 2\sqrt{x}$  from  $(0, 0)$  to  $(1, 2)$  about the  $x$ -axis is:

- A.  $2\pi/3$
- B.  $8\pi$
- C.  $8\pi(\sqrt{2} - 1)/3$
- D.  $8\pi(2\sqrt{2} - 1)/3$
- E.  $4\pi(\sqrt{2} - 1)/3$

7.  $\int_0^{\pi/2} \cos^4 x \, dx =$

- A.  $\pi/6$
- B.  $2\pi/9$
- C.  $3\pi/16$
- D.  $\pi/5$
- E.  $5\pi/8$

8. To compute  $\int \frac{x^2 + 1}{x^2 - 4x + 4} \, dx$ , one should reduce the integrand to

- A.  $\frac{A}{x-2} + \frac{B}{x-2}$
- B.  $x + \frac{A}{x-2} + \frac{B}{(x-2)^2}$
- C.  $\frac{A}{x-2} + \frac{B}{(x-2)^2}$
- D.  $1 + \frac{A}{x-2} + \frac{B}{(x-2)^2}$
- E.  $\frac{A}{x^2} + \frac{B}{x} + C$

9.  $\int_0^{\pi/2} \sin^3 t \cos^4 t \, dt =$

- A. 5/12
- B. 1/7
- C. 2/35
- D. 3/28
- E. 5/16

10. To compute  $\int_0^1 \frac{x^2}{\sqrt{x^2 - 2x + 2}} \, dx$ , the first step is to reduce the integral to:

- A.  $\int_0^{\pi/2} \sin^2 t \tan t \, dt$
- B.  $\int_{-\pi/4}^{\pi/4} (1 + \sin t)^2 \tan t \, dt$
- C.  $\int_{-\pi/4}^0 (1 + \tan t)^2 \sec t \, dt$
- D.  $\int_0^{\pi/4} \tan^2 t \sec t \, dt$
- E.  $\int_0^{\pi/2} \sin^2 t (1 + \sec t) \, dt$

11. Find all  $p$  such that the series  $\sum_{k=1}^{\infty} \sqrt{\frac{k^4}{k^p + 2}}$  converges.

- A.  $p > 1$
- B.  $p > 5$
- C.  $p \geq 6$
- D.  $p > 6$
- E.  $p > 7$

12.  $\sum_{k=0}^{\infty} \frac{2 + 2^k}{3^k} =$

- A.  $\infty$
- B. 3
- C.  $8/3$
- D. 6
- E.  $14/33$

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Recitation Instructor \_\_\_\_\_

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$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right) + C \quad \int \frac{1}{\sqrt{x^2 - a^2}} dx = \sin^{-1} \left( \frac{x}{a} \right) + C$$



## Questions

1.  $\int_0^{\pi/2} \cos^4 x \, dx =$

- A.  $\pi/6$
- B.  $3\pi/16$
- C.  $2\pi/9$
- D.  $\pi/5$
- E.  $5\pi/8$

2. To compute  $\int \frac{x^2 + 1}{x^2 - 4x + 4} \, dx$ , one should reduce the integrand to

- A.  $\frac{A}{x^2} + \frac{B}{x} + C$
- B.  $\frac{A}{x-2} + \frac{B}{x-2}$
- C.  $x + \frac{A}{x-2} + \frac{B}{(x-2)^2}$
- D.  $\frac{A}{x-2} + \frac{B}{(x-2)^2}$
- E.  $1 + \frac{A}{x-2} + \frac{B}{(x-2)^2}$

3.  $\int_0^{\pi/2} \sin^3 t \cos^4 t dt =$

A.  $2/35$

B.  $5/12$

C.  $1/7$

D.  $3/28$

E.  $5/16$

4. To compute  $\int_0^1 \frac{x^2}{\sqrt{x^2 - 2x + 2}} dx$ , the first step is to reduce the integral to:

A.  $\int_0^{\pi/2} \sin^2 t \tan t dt$

B.  $\int_0^{\pi/2} \sin^2 t (1 + \sec t) dt$

C.  $\int_{-\pi/4}^{\pi/4} (1 + \sin t)^2 \tan t dt$

D.  $\int_{-\pi/4}^0 (1 + \tan t)^2 \sec t dt$

E.  $\int_0^{\pi/4} \tan^2 t \sec t dt$

5.  $\int_0^{3/2} \frac{1}{4y^2 + 9} dy =$

- A.  $\pi/6$
- B.  $3\pi/16$
- C.  $2\pi/9$
- D.  $\pi/24$
- E.  $\pi/12$

6.  $\int_2^{\infty} \frac{2+u}{u^2} du =$

- A. 1
- B. 2
- C.  $1/2$
- D.  $\ln 2$
- E. The integral is divergent

7. Find the  $x$ -coordinate,  $\bar{x}$ , of the centroid for the region bounded by  $y = 2x$  and  $y = x^2$ .

- A. 1
- B.  $2/3$
- C.  $5/3$
- D. 2
- E.  $3/2$

8. Consider the two series

$$\sum_{n=0}^{\infty} \frac{n^2 - 1}{3n^4 + 1}, \quad \sum_{n=0}^{\infty} \frac{1}{\sqrt{n^2 + 1}}.$$

- A. Both are convergent
- B. Both are divergent
- C. The first one is convergent while the second one is divergent
- D. The first one is divergent while the second one is convergent
- E. None of the above

9. Find the length of the curve  $y = f(x)$  from  $x = 0$  to  $x = \pi/3$ , given its derivative  $f'(x) = \sqrt{\sec^2 x \tan^2 x - 1}$ .

- A. 2
- B.  $\sqrt{3}/3$
- C. 1
- D. 4
- E.  $\sqrt{2}$

10. The area of the surface obtained by revolving the curve  $y = 2\sqrt{x}$  from  $(0, 0)$  to  $(1, 2)$  about the  $x$ -axis is:

- A.  $2\pi/3$
- B.  $8\pi(2\sqrt{2} - 1)/3$
- C.  $8\pi$
- D.  $8\pi(\sqrt{2} - 1)/3$
- E.  $4\pi(\sqrt{2} - 1)/3$

11. Find all  $p$  such that the series  $\sum_{k=1}^{\infty} \sqrt{\frac{k^4}{k^p + 2}}$  converges.

- A.  $p > 1$
- B.  $p > 6$
- C.  $p > 5$
- D.  $p \geq 6$
- E.  $p > 7$

12.  $\sum_{k=0}^{\infty} \frac{2 + 2^k}{3^k} =$

- A.  $\infty$
- B. 6
- C. 3
- D.  $8/3$
- E.  $14/33$

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Name \_\_\_\_\_

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Recitation Instructor \_\_\_\_\_

Recitation Section Number and Time \_\_\_\_\_

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$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right) + C \quad \int \frac{1}{\sqrt{x^2 - a^2}} dx = \sin^{-1} \left( \frac{x}{a} \right) + C$$

## Questions

1. Find all  $p$  such that the series  $\sum_{k=1}^{\infty} \sqrt{\frac{k^4}{k^p + 2}}$  converges.

A.  $p > 1$

B.  $p > 5$

C.  $p \geq 6$

D.  $p > 6$

E.  $p > 7$

2.  $\sum_{k=0}^{\infty} \frac{2 + 2^k}{3^k} =$

A.  $\infty$

B. 3

C.  $8/3$

D. 6

E.  $14/33$



3. Find the length of the curve  $y = f(x)$  from  $x = 0$  to  $x = \pi/3$ , given its derivative  $f'(x) = \sqrt{\sec^2 x \tan^2 x - 1}$ .

- A. 2
- B.  $\sqrt{3}/3$
- C. 4
- D.  $\sqrt{2}$
- E. 1

4. The area of the surface obtained by revolving the curve  $y = 2\sqrt{x}$  from  $(0, 0)$  to  $(1, 2)$  about the  $x$ -axis is:

- A.  $2\pi/3$
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- D.  $8\pi(2\sqrt{2} - 1)/3$
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5. Find the  $x$ -coordinate,  $\bar{x}$ , of the centroid for the region bounded by  $y = 2x$  and  $y = x^2$ .

- A.  $2/3$
- B.  $5/3$
- C.  $2$
- D.  $3/2$
- E.  $1$

6. Consider the two series

$$\sum_{n=0}^{\infty} \frac{n^2 - 1}{3n^4 + 1}, \quad \sum_{n=0}^{\infty} \frac{1}{\sqrt{n^2 + 1}}.$$

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- E. None of the above

7.  $\int_0^{\pi/2} \cos^4 x \, dx =$

- A.  $\pi/6$
- B.  $2\pi/9$
- C.  $3\pi/16$
- D.  $\pi/5$
- E.  $5\pi/8$

8. To compute  $\int \frac{x^2 + 1}{x^2 - 4x + 4} \, dx$ , one should reduce the integrand to

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- B.  $x + \frac{A}{x-2} + \frac{B}{(x-2)^2}$
- C.  $\frac{A}{x-2} + \frac{B}{(x-2)^2}$
- D.  $1 + \frac{A}{x-2} + \frac{B}{(x-2)^2}$
- E.  $\frac{A}{x^2} + \frac{B}{x} + C$

9.  $\int_0^{\pi/2} \sin^3 t \cos^4 t \, dt =$

- A. 5/12
- B. 1/7
- C. 2/35
- D. 3/28
- E. 5/16

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- E.  $2\pi/9$

12.  $\int_2^{\infty} \frac{2+u}{u^2} du =$

- A. 1
- B. 2
- C.  $1/2$
- D. The integral is divergent
- E.  $\ln 2$

MA 16200 Exam II, Oct 19, 2017

Name \_\_\_\_\_

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Recitation Instructor \_\_\_\_\_

Recitation Section Number and Time \_\_\_\_\_

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## Questions

1.  $\int_0^{\pi/2} \sin^3 t \cos^4 t dt =$

- A.  $2/35$
- B.  $5/12$
- C.  $1/7$
- D.  $3/28$
- E.  $5/16$

2. To compute  $\int_0^1 \frac{x^2}{\sqrt{x^2 - 2x + 2}} dx$ , the first step is to reduce the integral to:

- A.  $\int_0^{\pi/2} \sin^2 t \tan t dt$
- B.  $\int_0^{\pi/2} \sin^2 t (1 + \sec t) dt$
- C.  $\int_{-\pi/4}^{\pi/4} (1 + \sin t)^2 \tan t dt$
- D.  $\int_{-\pi/4}^0 (1 + \tan t)^2 \sec t dt$
- E.  $\int_0^{\pi/4} \tan^2 t \sec t dt$

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- E.  $\pi/12$

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- A. 1
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- C.  $1/2$
- D.  $\ln 2$
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- D.  $\frac{A}{x-2} + \frac{B}{(x-2)^2}$
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- B.  $8\pi(2\sqrt{2} - 1)/3$
- C.  $8\pi$
- D.  $8\pi(\sqrt{2} - 1)/3$
- E.  $4\pi(\sqrt{2} - 1)/3$

**MA 16200 – Fall 2017**

**Exam 2**

**GREEN Test – Version 13**

<b>1</b>	<b>C</b>
<b>2</b>	<b>D</b>
<b>3</b>	<b>E</b>
<b>4</b>	<b>C</b>
<b>5</b>	<b>E</b>
<b>6</b>	<b>D</b>
<b>7</b>	<b>C</b>
<b>8</b>	<b>D</b>
<b>9</b>	<b>C</b>
<b>10</b>	<b>C</b>
<b>11</b>	<b>D</b>
<b>12</b>	<b>D</b>

# MA 16200 – Fall 2017

## Exam 1

<b>GREEN Test – Version 24</b>
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<b>1</b>	<b>B</b>
<b>2</b>	<b>E</b>
<b>3</b>	<b>A</b>
<b>4</b>	<b>D</b>
<b>5</b>	<b>D</b>
<b>6</b>	<b>E</b>
<b>7</b>	<b>A</b>
<b>8</b>	<b>C</b>
<b>9</b>	<b>C</b>
<b>10</b>	<b>B</b>
<b>11</b>	<b>B</b>
<b>12</b>	<b>B</b>

# MA 16200 – Fall 2017

## Exam 2

<b>GREEN Test – Version 57</b>
--------------------------------

<b>1</b>	<b>D</b>
<b>2</b>	<b>D</b>
<b>3</b>	<b>E</b>
<b>4</b>	<b>D</b>
<b>5</b>	<b>E</b>
<b>6</b>	<b>C</b>
<b>7</b>	<b>C</b>
<b>8</b>	<b>D</b>
<b>9</b>	<b>C</b>
<b>10</b>	<b>C</b>
<b>11</b>	<b>C</b>
<b>12</b>	<b>D</b>

**MA 16200 – Fall 2017**

**Exam 2**

**GREEN Test – Version 68**

<b>1</b>	<b>A</b>
<b>2</b>	<b>D</b>
<b>3</b>	<b>B</b>
<b>4</b>	<b>B</b>
<b>5</b>	<b>D</b>
<b>6</b>	<b>E</b>
<b>7</b>	<b>B</b>
<b>8</b>	<b>E</b>
<b>9</b>	<b>A</b>
<b>10</b>	<b>C</b>
<b>11</b>	<b>C</b>
<b>12</b>	<b>B</b>