

Name: _____

I.D.#: _____

Recitation Instructor: _____ Time of Recitation _____

Lecturer: _____ Section#: _____

Instructions:

- (1) Fill in your name, student ID number and division and section number on the mark-sense sheet. Also fill out the information requested above.
- (2) This booklet consists of 6 pages. There are 14 questions, each worth 7 points.
- (3) Mark your answers on the mark-sense sheet. Please show your working in this booklet.
- (4) No books, notes or calculators may be used.
- (5) When you are finished with the exam hand this booklet and the mark-sense sheet, in person, to your instructor.

1. If $f(t) = \frac{t^2}{1+t^3}$, $f'(t) =$

- A. $\frac{2t - 3t^2}{(1+t^3)^2}$
- B. $\frac{1+t^2+t^3}{(1+t^3)^2}$
- C. $\frac{2t-t^4}{(1+t^3)^2}$
- D. $\frac{2t-5t^4}{(1+t^3)^2}$
- E. $\frac{2t}{(1+t^3)^2}$

2. If $f(t) = \cos(\ln(3t^2))$, $f'(t) =$

- A. $\frac{-2 \sin(\ln(3t^2))}{t}$
- B. $-\sin\left(\frac{1}{3t^2}\right)$
- C. $\frac{-\sin(\ln(3t^2))}{3t^2}$
- D. $-\frac{1}{\sin(3t^2)}$
- E. $\tan(3t^2)$

3. Given that $f(2) = 3$, $f(8) = 4$, $f'(2) = 5$, $f'(8) = -1$ and $f''(2) = 6$, evaluate

$$\frac{d}{dx}[f(x^3) \cdot f(x)]$$

at $x = 2$.

- A. 17
- B. 8
- C. 0
- D. -5
- E. -16

4. If $g(x) = -e^{-3x} + x^{21} - x^2$ then the twenty-third derivative of g , $g^{(23)}(x) =$

- A. $3^{23}e^{-3x}$
- B. $-e^{-3x}$
- C. $-3^{23}e^{-3x} + 21$
- D. 0
- E. $-3^{23}e^{-3x}$

5. If $x^3 + xy^2 + 3y^3 = \pi^{\frac{1}{2}}$ then $\frac{dy}{dx} =$

- A. $\frac{-x^2}{2xy + 9y^2}$
- B. $\frac{\pi^{\frac{1}{2}} - x^3}{xy + 3y^2}$
- C. $-(3x + y^2)$
- D. $\frac{-3x^2 - y^2}{2xy + 9y^2}$
- E. $\frac{\pi^{\frac{1}{2}}}{x^3 + x^2y + 3y^2}$

6. A spherical balloon is inflated in such a way that after t seconds $V = 36\pi\sqrt{t}$ cubic centimeters. How fast is the radius of the balloon changing when $t = 64$?

- A. 1
- B. $\frac{1}{16}$
- C. $\frac{1}{32}$
- D. $\frac{1}{64}$
- E. $\frac{1}{128}$

7. The edges of a cube are increasing at the rate of 4 inches/min. At what rate is the volume of the cube increasing when the volume is 8 cubic inches?

A. 12 in.³/min.
B. 16 in.³/min.
C. 8π in.³/min.
D. 32 in.³/min.
E. 48 in.³/min.

8. Use the fact that $(16)^{\frac{1}{4}} = 2$ and use linear approximation to approximate $(14)^{\frac{1}{4}}$.

A. $2 - \frac{1}{8}$
B. $2 - \frac{1}{16}$
C. $2 - \frac{1}{32}$
D. 2
E. $2 + \frac{1}{32}$

9. The critical numbers of $f(x) = \frac{200}{x} + 2x - 50$ are

A. 5, 0, 20
B. 5, 20
C. -10, 10
D. -10, 0, 10
E. There are none

10. Find all extreme values (if any) of $f(x) = x^2 + \frac{16}{x}$ on the interval $[1, 4]$.
- A. max. value = 20; min. value = 17
 - B. max. value = 20; min. value = 12
 - C. max, value = 18; min. value = 8
 - D. no max. value; min. value = 17
 - E. no max. value; no min. value
11. A number c in the interval $(0, 2)$ for which the line tangent to the graph of $y = x^3 - x^2$ at $x = c$ is parallel to the line through $(0, 0)$ and $(2, 4)$ is
- A. 1
 - B. $\frac{4}{3}$
 - C. $\frac{2 + \sqrt{10}}{6}$
 - D. $\frac{1 + \sqrt{7}}{3}$
 - E. $\frac{2 + \sqrt{40}}{6}$

12. Suppose you have a cache of a radioactive substance whose half-life is 250 years. How long will you have to wait for $\frac{4}{5}$ of it to decay (i.e., $\frac{1}{5}$ to remain)?
- A. $250 \frac{\ln 5}{\ln 2}$ years
 - B. $250 \frac{\ln 2}{\ln 5}$ years
 - C. $250 \ln \left(\frac{2}{5} \right)$ years
 - D. $250 \ln \left(\frac{5}{2} \right)$ years
 - E. 50 years
13. Let $f(x) = \frac{5}{x}$ and $g(x) = x^3$. Then
- A. both f and g are increasing on $(0, \infty)$
 - B. both f and g are decreasing on $(0, \infty)$
 - C. f is increasing and g is decreasing on $(0, \infty)$
 - D. f is decreasing and g is increasing on $(0, \infty)$
 - E. none of the above is true.
14. The function $h(x) = 4x^3 - 3x^4$ has
- A. no relative extrema
 - B. one relative extremum
 - C. two relative extrema
 - D. three relative extrema
 - E. four relative extrema.