

NAME \_\_\_\_\_

STUDENT ID # \_\_\_\_\_

RECITATION INSTRUCTOR \_\_\_\_\_

RECITATION TIME \_\_\_\_\_

DIRECTIONS

- 1) Fill in the above information. Also write your name at the top of each page of the exam.
- 2) The exam has 6 pages, including this one.
- 3) Problems 1 through 6 are multiple choice; circle the correct answer. No partial credit for these problems.
- 4) Problems 7 through 9 are problems to be worked out. Partial credit for correct work is possible. Write your answer in the box provided. **YOU MUST SHOW SUFFICIENT WORK TO JUSTIFY YOUR ANSWERS. CORRECT ANSWERS WITH INCONSISTENT WORK MAY NOT RECEIVE CREDIT.**
- 5) Points for each problem are given in parenthesis in the left margin.
- 6) No books, notes, or calculators may be used on this test.

Page 2	/16
Page 3	/16
Page 4	/16
Page 5	/22
Page 6	/30
TOTAL	/100

- (8) 1. Find the volume of the solid region in the first octant bounded above by the plane  $x + z = 3$ , on the sides by the planes  $x + y = 1$ ,  $x = 0$ , and  $y = 0$  and below by the plane  $z = 0$ .

A.  $\frac{5}{3}$

B.  $\frac{2}{3}$

C.  $\frac{1}{2}$

D.  $\frac{4}{3}$

E. 2

- (8) 2. Find the surface area of the part of the parabolic cylinder  $z = y^2$  that lies over the triangle with vertices  $(0, 0)$ ,  $(0, 1)$ ,  $(1, 1)$  in the  $xy$ -plane.

A.  $\frac{1}{12}(5\sqrt{5} - 1)$

B.  $\frac{5}{12}\sqrt{5}$

C.  $\frac{2}{3}$

D.  $\frac{1}{4}$

E.  $\frac{1}{12}$

(8) 3. The iterated triple integral  

$$\int_{-2}^2 \int_0^{\sqrt{4-x^2}} \int_x^{3+x^2+y^2} 10y \, dz \, dy \, dx$$
 in cylindrical coordinates is:

- A.  $\int_0^\pi \int_0^2 \int_{\cos \theta}^{3+r^2} 10r \sin \theta \, dz \, dr \, d\theta$
- B.  $\int_0^{\frac{\pi}{2}} \int_0^2 \int_{r \cos \theta}^{3+r^2} 10r \sin \theta \, dz \, dr \, d\theta$
- C.  $\int_0^\pi \int_{-2}^2 \int_{r \cos \theta}^{3+r^2} 10r^2 \sin \theta \, dz \, dr \, d\theta$
- D.  $\int_0^\pi \int_0^2 \int_{r \cos \theta}^{3+r^2} 10r^2 \sin \theta \, dz \, dr \, d\theta$
- E.  $\int_0^{\frac{\pi}{2}} \int_{-2}^2 \int_{r \cos \theta}^{3+r^2} 10r^2 \sin \theta \, dz \, dr \, d\theta$

(8) 4. If  $\vec{F}(x, y, z) = xy\vec{i} + z^2\vec{j} + e^y\vec{k}$  then  $\vec{F} \cdot \text{curl } \vec{F} =$

- A. 0
- B.  $xy^2$
- C.  $xy(e^y - 2z) - xe^y$
- D.  $e^y(xy + 2z - x) - yz^2$
- E.  $e^y(xy + 2z - x)$

(8) 5. Compute  $\int_C 6x \, ds$  where  $C$  is the graph of  $y = x^2$  for  $0 \leq x \leq 1$ .

- A.  $5\sqrt{5} - 1$
- B.  $\frac{1}{2} (5\sqrt{5} - 1)$
- C. 3
- D. 2
- E.  $\frac{3}{2}$

(8) 6. Compute  $\int_C e^x dx + 3xy \, dy + xyz \, dz$  where  $C$  is the curve parametrized by  $\vec{r}(t) = t\vec{i} + t\vec{j} + 2t\vec{k}$  for  $0 \leq t \leq 1$ .

- A.  $e$
- B.  $e + \frac{1}{3}$
- C.  $e + \frac{1}{2}$
- D.  $e + 1$
- E.  $e + \frac{3}{2}$

(11) 7. Find a function  $f(x, y)$  whose gradient is:

$$\text{grad } f(x, y) = (3x^2e^{2y} - y)\vec{i} + (2x^3e^{2y} - x + 2y)\vec{j}$$

and  $f(1, 0) = 3$ .

$$f(x, y) =$$

(11) 8. Use Green's Theorem to evaluate  $\int_C (y^3 + 2y)dx + 3xy^2dy$ , where  $C$  is the circle  $x^2 + y^2 = 16$  oriented counterclockwise.

(30) 9. Let  $D$  be the solid region above the upper nappe of the cone  $z^2 = x^2 + y^2$  and below the sphere  $x^2 + y^2 + z^2 = 18$ . If  $\vec{F}(x, y, z) = 3x^2\vec{i} + \vec{j} + \frac{1}{2}z^2\vec{k}$ , express the triple integral  $\iiint_D \operatorname{div} \vec{F} dV$  as an iterated triple integral in (a) rectangular coordinates, (b) cylindrical coordinates, and (c) spherical coordinates. (Include the limits of integration.)

(a) Rectangular coordinates

(b) Cylindrical coordinates

(c) Spherical coordinates