

# MA 15400

## Spring 2014

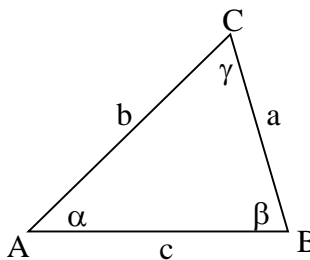
### Exam 1

PYTHAGOREAN IDENTITIES:

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$



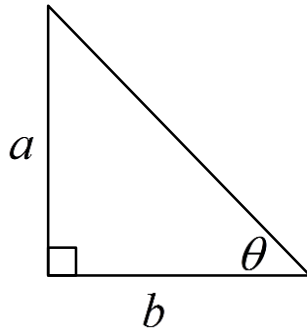
1. Find the angle that is supplementary to  $48^{\circ}57'9''$ 
  - A.  $131^{\circ}2'51''$
  - B.  $41^{\circ}52'41''$
  - C.  $41^{\circ}2'51''$
  - D.  $131^{\circ}52'41''$
  - E. None of the above
  
2. Express the angle  $153^{\circ}8'36''$  as a decimal, to the nearest ten-thousandth of an angle.
  - A.  $153.6022^{\circ}$
  - B.  $153.1433^{\circ}$
  - C.  $153.4383^{\circ}$
  - D.  $153.7667^{\circ}$
  - E. None of the above
  
3. If a circular arc of the given length  $s = 5.2$  km subtends the central angle  $\theta = 76^{\circ}$  on a circle, find the radius of the circle. Round your answer to the nearest hundredth.
  - A.  $9.95$  km
  - B.  $3.17$  km
  - C.  $12.32$  km
  - D.  $3.92$  km
  - E. None of the above

Lessons 1-11, All of Sections 6.1, 6.2, 6.3, 6.4, 6.5.

4. A pendulum in a grandfather clock is 5.2 feet long and swings back and forth along a 7-inch arc. Approximate the angle through which the pendulum passes during one swing. Round your answer to the nearest tenth of a degree. (1 foot = 12 inches)

- A.  $6.4^\circ$   
B.  $6.6^\circ$   
C.  $6.2^\circ$   
D.  $6.8^\circ$   
E. None of the above

5. Which one of the following statements is true for the given triangle?



A.  $\sec \theta = \frac{\sqrt{a^2 + b^2}}{a}$

B.  $\csc \theta = \frac{\sqrt{a^2 + b^2}}{b}$

C.  $\cos \theta = \frac{b}{\sqrt{a^2 + b^2}}$

D.  $\sin \theta = \frac{b}{\sqrt{a^2 + b^2}}$

- E. More than one of the above answers are correct.

6. Find the quadrant containing  $\theta$  if  $\sec \theta > 0$  and  $\tan \theta < 0$ .

- A. *I*  
B. *II*  
C. *III*  
D. *IV*  
E. None of the above

7. Find the exact value of  $\sin(\theta)$  if  $\theta$  is in standard position and the terminal side of  $\theta$  is in  $QIV$  and is parallel to the line through  $A(6, 2)$  and  $B(1, 8)$ .

- A.  $\frac{-6}{\sqrt{61}}$   
B.  $\frac{5}{\sqrt{61}}$   
C.  $\frac{-5}{\sqrt{61}}$   
D.  $\frac{6}{\sqrt{61}}$

8. Let  $P(t)$  be the point on the unit circle  $U$  that corresponds to  $t$ .

If  $P(t) = \left(\frac{5}{13}, \frac{-12}{13}\right)$ , find  $P(-t + \pi)$

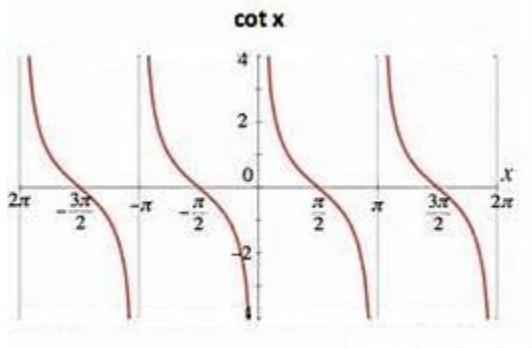
- A.  $\left(\frac{5}{13}, \frac{-12}{13}\right)$   
B.  $\left(\frac{-5}{13}, \frac{-12}{13}\right)$   
C.  $\left(\frac{-5}{13}, \frac{12}{13}\right)$   
D.  $\left(\frac{5}{13}, \frac{12}{13}\right)$

E. None of the above

9. Find the exact value of  $\sec\left(\frac{-13\pi}{2}\right)$

- A.  $-2$   
B.  $1$   
C.  $0$   
D.  $-1$   
E. None of the above

10. Use the graph to complete the statement: As  $x \rightarrow \pi^-$ ,  $\cot(x) \rightarrow$  \_\_\_\_\_



- A.  $-\infty$
- B. 0
- C. 1
- D.  $\infty$
- E. None of the above

11. Find the reference angle  $\theta_R$  if  $\theta = \frac{5\pi}{3}$

- A.  $\theta_R = \frac{2\pi}{3}$
- B.  $\theta_R = \frac{-\pi}{3}$
- C.  $\theta_R = \frac{4\pi}{3}$
- D.  $\theta_R = \frac{\pi}{3}$
- E. None of the above

12. Find the exact value of  $\cos\left(\frac{11\pi}{6}\right)$ .

- A.  $\frac{-1}{2}$
- B.  $\frac{\sqrt{3}}{2}$
- C.  $\frac{1}{2}$
- D.  $\frac{-\sqrt{3}}{2}$
- E. None of the above

Lessons 1-11, All of Sections 6.1, 6.2, 6.3, 6.4, 6.5.

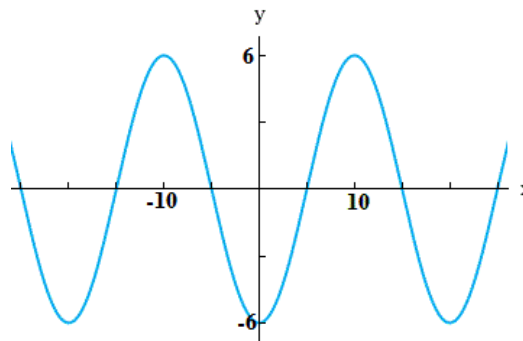
13. Approximate, to the nearest  $0.1^\circ$ , all angles  $\theta$  in the interval  $[0^\circ, 360^\circ)$  that satisfy the equation  $\sec \theta = 4.5387$ .

- A.  $\theta = 77.3^\circ, 102.7^\circ$
- B.  $\theta = 12.7^\circ, 167.3^\circ$
- C.  $\theta = 77.3^\circ, 282.7^\circ$
- D.  $\theta = 12.7^\circ, 347.3^\circ$
- E. None of the above

14. Approximate, to the nearest 0.0001 radians, all angles  $\theta$  in the interval  $[0, 2\pi)$  that satisfy equation  $\tan \theta = -1.0383$ .

- A.  $\theta = 2.3374, 3.9458$
- B.  $\theta = 0.8042, 3.9458$
- C.  $\theta = 0.8042, 5.4790$
- D.  $\theta = 2.3374, 5.4790$
- E. None of the above

Use the graph of the **sine** function to answer Questions 15, 16, and 17.



15. Find the amplitude

- A. 6
- B. -12
- C. 12
- D. -6

16. Find the period

- A. 10
- B. 15
- C. 20
- D. 5

17. Find the Phase Shift

- A. -5
- B. -15
- C. -10
- D. -20

Question	Answers	
1.	A	$131^{\circ}2'51''$
2.	B	$153.1433^{\circ}$
3.	D	$3.92 \text{ km}$
4.	A	$6.4^{\circ}$
5.	C	$\cos \theta = \frac{b}{\sqrt{a^2 + b^2}}$
6.	D	$IV$
7.	A	$\frac{-6}{\sqrt{61}}$
8.	B	$\left(\frac{-5}{13}, \frac{-12}{13}\right)$
9.	E	Undefined
10.	A	$-\infty$
11.	D	$\theta_R = \frac{\pi}{3}$
12.	B	$\frac{\sqrt{3}}{2}$
13.	C	$\theta = 77.3^{\circ}, 282.7^{\circ}$
14.	D	$\theta = 2.3374, 5.4790$
15.	A	6
16.	C	20
17.	B	-15