

MA 16200
EXAM 2 Form 01
October 17, 2019

NAME _____ YOUR TA'S NAME _____

STUDENT ID # _____ RECITATION TIME _____

Be sure the paper you are looking at right now is GREEN! Write the following in the TEST/QUIZ NUMBER boxes (and blacken in the appropriate spaces below the boxes):

01

You must use a #2 pencil on the mark-sense sheet (answer sheet). On the mark-sense sheet, fill in your TA's name and the COURSE number. Fill in your NAME and STUDENT IDENTIFICATION NUMBER and blacken in the appropriate spaces. Fill in your four-digit SECTION NUMBER. If you do not know your section number, ask your TA. Sign the mark-sense sheet.

There are 12 questions, each worth 8 points (you will automatically earn 4 point for taking the exam). Blacken in your choice of the correct answer in the spaces provided for questions 1–12. Do all your work in this exam booklet. Use the back of the test pages for scrap paper. Turn in both the scantron and the exam booklet when you are finished.

If you finish the exam before 7:20, you may leave the room after turning in the scantron sheet and the exam booklet. You may not leave the room before 6:50. If you don't finish before 7:20, you MUST REMAIN SEATED until your TA comes and collects your scantron sheet and your exam booklet.

EXAM POLICIES

1. Students may not open the exam until instructed to do so.
2. Students must obey the orders and requests by all proctors, TAs, and lecturers.
3. No student may leave in the first 20 min or in the last 10 min of the exam.
4. Books, notes, calculators, or any electronic devices are not allowed on the exam, and they should not even be in sight in the exam room. Students may not look at anybody else's test, and may not communicate with anybody else except, if they have a question, with their TA or lecturer.
5. After time is called, the students have to put down all writing instruments and remain in their seats, while the TAs will collect the scantrons and the exams.
6. Any violation of these rules and any act of academic dishonesty may result in severe penalties. Additionally, all violators will be reported to the Office of the Dean of Students.

I have read and understand the exam rules stated above:

STUDENT NAME: _____

STUDENT SIGNATURE: _____

1. Compute

$$\int -9x \cos 5x \, dx$$

A. $-\frac{9}{25} \cos 5x - \frac{9}{5}x \sin 9x + C$

B. $-\frac{9}{5} \cos 5x - 9x \sin 5x + C$

C. $-\frac{9}{25} \cos 5x - \frac{9}{5} \sin 9x + C$

D. $-\frac{9}{25} \cos 5x - \frac{9}{5}x \sin 5x + C$

E. $\frac{9}{25} \cos 5x + \frac{9}{5}x \sin 5x + C$

2. Compute

$$\int (2x - 1) \ln(10x) \, dx$$

A. $(x^2 - x) \ln(10x) - x^2 + x + C$

B. $(x^2 - x) \ln(10x) - \frac{x^2}{2} + x + C$

C. $(x^2 - x) \ln(10x) - \frac{x^2}{2} + 2x + C$

D. $(\frac{x^2}{2} - x) \ln(10x) - \frac{x^2}{4} + x + C$

E. $(\frac{x^2}{2} - x) \ln(10x) + \frac{x^2}{2} + 2x + C$

3. A cylindrical water tank has a height of 7 m and a radius of 2 m. If the tank is full of water, how much work, in Joules, is required to pump the water to the level of the top and out of the tank? Express your answer in terms of π , g (acceleration due to gravity in m/s^2), and ρ (the density of water in kg/m^3).

- A. $40\pi\rho g$
- B. $\frac{49}{2}\pi\rho g$
- C. $686\pi\rho g$
- D. $98\pi\rho g$
- E. $49\pi\rho g$

4. Compute

$$\int 7 \sec^4 x \, dx$$

- A. $\frac{7}{3} \tan^3 x + C$
- B. $-\frac{7}{3} \tan^3 x + C$
- C. $7(\sec x + \tan x)^5 + C$
- D. $\frac{7}{3} \tan x + 7 \tan^3 x + C$
- E. $7 \tan x + \frac{7}{3} \tan^3 x + C$

5. Evaluate

$$\int_0^{\frac{1}{4}} 5 \sin^4(2\pi x) dx$$

- A. $\frac{15}{32} - \frac{5}{\pi}$
- B. $\frac{15}{16}$
- C. $\frac{15}{32}$
- D. $\frac{15}{16} - \frac{5}{8\pi}$
- E. $\frac{5}{8\pi}$

6. Use a trigonometric substitution to evaluate

$$\int_0^1 \frac{dx}{\sqrt{64 - x^2}}$$

- A. $8 \cos^{-1}(\frac{1}{8})$
- B. $\frac{1}{8} \sin^{-1}(\frac{1}{8})$
- C. $\sin^{-1}(\frac{1}{8})$
- D. $\cos^{-1}(\frac{1}{8})$
- E. $\frac{1}{8} \cos^{-1}(\frac{1}{8})$

7. After a proper trigonometric substitution is used to transform $\int_1^4 \frac{dt}{t^2 - 2t + 10}$ into $\int_a^b f(\theta) d\theta$, what is the new upper integration limit b ?

- A. $\frac{\pi}{6}$
- B. $\frac{\pi}{4}$
- C. $\frac{\pi}{2}$
- D. $\frac{\pi}{3}$
- E. π

8. Use the fact that

$$\int \frac{2x^4 + 15x^3 + 9x^2 + 11x + 3}{x^5 + x^4 - x - 1} dx = 5 \ln|x - 1| - 3 \ln|x + 1| - \frac{3}{x + 1} + 2 \tan^{-1}(x) + C$$

to find the partial fraction expansion of $\frac{2x^4 + 15x^3 + 9x^2 + 11x + 3}{x^5 + x^4 - x - 1}$

- A. $\frac{5}{x - 1} + \frac{-3}{x + 1} + \frac{3}{(x + 1)^2} + \frac{2}{x^2 + 1}$
- B. $\frac{5}{x - 1} + \frac{-3}{x + 1} + \frac{-3x}{(x + 1)^2} + \frac{2}{x^2 + 1}$
- C. $\frac{5}{x - 1} + \frac{-3}{x + 1} + \frac{-3}{(x + 1)^2} + \frac{2x}{x^2 + 1}$
- D. $\frac{-5}{x - 1} + \frac{3}{x + 1} + \frac{3}{(x + 1)^2} + \frac{-2}{x^2 + 1}$
- E. $\frac{-5}{x - 1} + \frac{3}{x + 1} + \frac{3x}{(x + 1)^2} + \frac{2x}{x^2 + 1}$

9. After a long division, the rational expression $\frac{x^3 + 2}{x^3 - 2x^2 + x}$ can be written as

$$A + \frac{B}{x} + \frac{C}{x-1} + \frac{D}{(x-1)^2}$$

Find D

- A. 3
 - B. 2
 - C. 1
 - D. -2
 - E. -3
10. Which of the following improper integrals are convergent?

I. $\int_0^{\infty} \cos \pi x \, dx$

II. $\int_1^{\infty} x e^{-x^2} \, dx$

III. $\int_{-1}^1 \frac{1}{x^2} \, dx$

- A. I, II, III
- B. II only
- C. III only
- D. I, II only
- E. II, III only

11. Which of the following sequences converge?

I. $\left\{ \frac{n}{2n + (-1)^n} \right\}_{n=1}^{\infty}$

II. $\left\{ \sin \frac{(2n-1)\pi}{2} \right\}_{n=1}^{\infty}$

III. $\{a_n\}_{n=1}^{\infty}$ where $a_1 = 1$, $a_{n+1} = \frac{a_n}{2}$

- A. All of them
- B. None of them
- C. I only
- D. I and III only
- E. III only

12. Find a formula for the n^{th} partial sum of the infinite series

$$\sum_{n=1}^{\infty} \frac{1}{3^n}$$

- A. $\frac{3^n - 1}{3^n}$
- B. $\frac{3^n + 1}{2 \cdot 3^n}$
- C. $\frac{1}{3^n}$
- D. $\frac{1}{n3^n}$
- E. $\frac{3^n - 1}{2 \cdot 3^n}$