

MA 16500
EXAM 3 INSTRUCTIONS
VERSION 01
November 13, 2017

Your name _____ Your TA's name _____

Student ID # _____ Section # and recitation time _____

1. You must use a #2 pencil on the scantron sheet (answer sheet).
2. Check that the cover of your exam booklet is GREEN and that it has VERSION 01 on the top. Write 01 in the TEST/QUIZ NUMBER boxes and blacken in the appropriate spaces below.
3. On the scantron sheet, fill in your **TA's name (NOT the lecturer's name)** and the course number.
4. Fill in your NAME and PURDUE ID NUMBER, and blacken in the appropriate spaces.
5. Fill in the four-digit **SECTION NUMBER**.
6. Sign the scantron sheet.
7. Blacken your choice of the correct answer in the space provided for each of the questions 1–12. **All the answers must be marked on the scantron sheet.** In case what is marked on the scantron sheet is different from what is marked on the exam booklet, we compute the final score based upon what is marked on the scantron sheet.
8. While marking all your answers on the scantron sheet, you should **show your work on the exam booklet**. In case of a suspicious activity of academic dishonesty and/or under certain circumstances, we require that the correct answer on the scantron sheet must be supported by the work on the exam booklet.
9. There are 12 questions, each worth 8 points. The maximum possible score is $8 \times 12 + 4$ (for taking the exam) = 100 points.
10. NO calculators, electronic device, books, or papers are allowed. Use the back of the test pages for scrap paper.
11. After you finish the exam, turn in BOTH the scantron sheet and the exam booklet.
12. If you finish the exam before 8:55, you may leave the room after turning in the scantron sheets and the exam booklets. If you don't finish before 8:55, you should REMAIN SEATED until your TA comes and collects your scantron sheet and exam booklet.

Exam Policies

1. Students must take pre-assigned seats and/or follow TAs' seating instructions.
2. Students may not open the exam until instructed to do so.
3. No student may leave in the first 20 min or in the last 5 min of the exam.
4. Students late for more than 20 min will not be allowed to take the exam; they will have to contact their lecturer within one day for permission to take a make-up exam.
5. After time is called, the students have to put down all writing instruments and remain in their seats, while the TAs will collect the scantron sheet and the exam booklet.
6. Any violation of the above rules may result in score of zero.

Rules Regarding Academic Dishonesty

1. You are not allowed to seek or obtain any kind of help from anyone to answer questions on the exam. If you have questions, consult only your instructor.
2. You are not allowed to look at the exam of another student. You may not compare answers with anyone else or consult another student until after you have finished your exam, handed it in to your instructor and left the room.
3. You may not consult notes, books, calculators. You may not handle cell phones or cameras, or any electronic devices until after you have finished your exam, handed it in to your instructor and left the room.
4. Anyone who violates these instructions will have committed an act of academic dishonesty. Penalties for academic dishonesty can be very severe and may include an F in the course. All cases of academic dishonesty will be reported immediately to the Office of the Dean of Students.

I have read and understand the exam policies and the rules regarding the academic dishonesty stated above:

STUDENT NAME: _____

STUDENT SIGNATURE: _____

Questions

1. Consider the function $f(x) = xe^{-2x}$.

Let M be the absolute maximum value of $f(x)$ and m be the absolute minimum value of $f(x)$ on the closed interval $[0, 2]$.

What is $M + m$?

- A. $\frac{1}{e^2}$
- B. $\frac{1}{2e}$
- C. $\frac{e^2 + 2}{e^4}$
- D. $\frac{e^3 + 4}{2e^4}$
- E. $\frac{1}{e}$

2. The derivative of a function f is given by

$$f'(x) = (x - 1)x(x + 1)^2(x + 2)^3.$$

The function f has a local maximum only at

- A. $x = -2$
- B. $x = 0$
- C. $x = -1$ and $x = 1$
- D. $x = -1$ and $x = 0$
- E. $x = -2$ and $x = 0$

3. The second derivative of a function f is given by

$$f''(x) = (x + 3)^5(x + 1)^4x^3(x - 1)^2(x - 3)$$

How many inflection points does the graph of $y = f(x)$ have?

- A. 0
- B. 1
- C. 2
- D. 3
- E. 4

4. Compute the following limits:

$$(a) \lim_{x \rightarrow 0} \frac{\sin x - x}{x^3}; \quad (b) \lim_{x \rightarrow 0} \frac{\sin x}{x + 1}$$

- A. (a) $\frac{1}{3}$; (b) 1
- B. (a) ∞ ; (b) 0
- C. (a) ∞ ; (b) 1
- D. (a) $-\frac{1}{6}$; (b) 0
- E. (a) $-\frac{1}{6}$; (b) 1

5. Compute the following limit

$$\lim_{x \rightarrow \infty} (x + e^{3x})^{\frac{1}{x}}.$$

- A. 1
- B. e
- C. e^3
- D. 3
- E. ∞

6. Find the equation of the slant asymptote to the graph of the function

$$f(x) = \frac{-6x^4 + 2x^3 + 3}{2x^3 + 1}.$$

A. $y = 3x$

B. $y = -3x - 1$

C. $y = -3x + 1$

D. $y = 6x - 2$

E. $y = -6x + 2$

7. Determine the exact value of

$$\sin^{-1}\left(\frac{1}{3}\right) + \cos^{-1}\left(\frac{1}{3}\right).$$

HINT: Consider the function

$$F(x) = \sin^{-1}(x) + \cos^{-1}(x)$$

over the interval $[0, \frac{1}{3}]$.

Compute its derivative and use Mean Value Theorem.

- A. $\frac{\pi}{2}$
- B. π
- C. 0
- D. $\frac{\pi}{4}$
- E. $-\frac{\pi}{3}$

8. Compute

$$\lim_{x \rightarrow \infty} x \tan\left(\frac{5}{x}\right).$$

- A. ∞
- B. 0
- C. 5
- D. $\frac{1}{5}$
- E. DNE

9. Choose the picture from below that best describes the graph of the function

$$f(x) = \frac{x^2}{x^2 - 4}.$$

A.

B.

C.

D.

E.

10. The sum of two positive number is 16.

What is the smallest possible value of the sum of their squares?

A. 162

B. 128

C. 98

D. 72

E. 50

11. A box with square base and open top must have a volume of 4 m^3 .
Find the height of the box that has the smallest possible surface area.

- A. 4
- B. $3/2$
- C. $1/2$
- D. $1/4$
- E. 1

12. Find the equation of the line through the point $(4, 3)$ that cuts off the triangle of least area from the first quadrant.

A. $y = -\frac{4}{3}x + 8$

B. $y = -\frac{4}{3}x + \frac{25}{3}$

C. $y = -x + 7$

D. $y = -\frac{3}{4}x + 6$

E. $y = \frac{3}{4}x$