

- 1) If $f(x) = 5x^2 - 2$, find and simplify the difference quotient $\frac{f(x+h) - f(x)}{h}$.

A. $2x + 5h$
B. $10x + h$
C. $5h$
D. $10x + 5h$
E. $2x + h$

- 2) Find $\frac{dy}{dx}$ where $y = \frac{2}{3}x - \sqrt{x} + \frac{1}{x^3}$.

A. $\frac{dy}{dx} = \frac{2}{3} - \frac{1}{2\sqrt{x}} + \frac{1}{3x^2}$
B. $\frac{dy}{dx} = -\frac{2}{3} - \frac{1}{\sqrt{x}} - \frac{3}{x^4}$
C. $\frac{dy}{dx} = -\frac{2}{3} - \frac{1}{2\sqrt{x}} - \frac{3}{x^4}$
D. $\frac{dy}{dx} = \frac{2}{3} - \frac{1}{\sqrt{x}} + \frac{1}{3x^2}$
E. $\frac{dy}{dx} = \frac{2}{3} - \frac{1}{2\sqrt{x}} - \frac{3}{x^4}$

- 3) If $j(x) = \left(x - \frac{1}{x}\right)(3x^2 + 1)$, then $j'(x) =$ which choice?

A. $9x^2 + \frac{1}{x^2} - 2$
B. $9x^2 + 5$
C. $3x^3 - 2x + \frac{1}{x}$
D. $6x^2 + 6$
E. $9x^2 + \frac{1}{x^2} - 8$

- 4) Find the x -coordinate only of any point(s) at which the graph of the function f below would have a horizontal tangent line.

$$f(x) = \frac{2}{3}x^3 + x^2 - 12x - 6$$

- A. $x = -3, 2$
- B. $x = -12$
- C. $x = -3, 0, 2$
- D. $x = 12$
- E. $x = -2, 3$

- 5) The revenue, in dollars, from selling x DVD players is $R(x) = 100x + \frac{3000}{x}$. Use the marginal revenue function to estimate the additional revenue from the sale of the 11th unit once 10 units have been sold.

- A. \$74.00
- B. \$72.73
- C. \$70.00
- D. \$74.79
- E. \$72.00

- 6) Find the following limit.
- $$\lim_{x \rightarrow 2} \left(\frac{x^2 - 7x + 10}{x^2 - 4} \right)$$

- A. $-\frac{3}{4}$
- B. 0
- C. $-\frac{5}{2}$
- D. 1
- E. This limit does not exist.

7) Find the following limit.

$$\lim_{h \rightarrow 0} \left(\frac{2(x+h)^2 - (x+h) + 3 - (2x^2 - x + 3)}{h} \right)$$

- A. -1
- B. $4x+1$
- C. $1-4x$
- D. $-4-4x$
- E. $4x-1$

8) Find the slope of the line tangent to the graph of $g(x) = x + \frac{1}{x}$ at the point $\left(2, \frac{5}{2}\right)$.

- A. $m = -\frac{3}{4}$
- B. $m = \frac{3}{4}$
- C. $m = -1$
- D. $m = 1$
- E. $m = \frac{5}{4}$

9) Find the **average** rate of change of the function $f(x) = x^2 - 2x^{3/2}$ on the interval $[1, 9]$.

- A. 1.25
- B. 3.5
- C. 3.25
- D. 1
- E. 9.5

- 10) Find the equation of the line tangent to the graph of $y = 3x^3 - 2x^2 + 7x - 5$ at the point $(-1, -17)$.
- A. $y = 17x + 288$
B. $y = 17x$
C. $y = 20x - 3$
D. $y = 20x + 3$
E. $y = -20x + 3$
- 11) The number of bacteria N (in millions) found in a culture after t hours, is given by the function $N(t) = 3t(t - 10)^2 + 40$. How is the population of bacteria changing after 8 hours? Hint: Rewrite the function N as a polynomial.
- A. It is decreasing by 84 million/hour
B. It is increasing by 84 million/hour
C. It is decreasing by 44 million/hour
D. It is decreasing by 96 million/hour
E. It is increasing by 96 million/hour
- 12) Find the slope of the line tangent to the graph of $g(x) = \left(2x + \frac{8}{x^2}\right)(x^2 - x)$ at the point $(2, 12)$.
- A. $m = 26$
B. $m = 18$
C. $m = 0$
D. $m = 14$
E. $m = 20$

- 13) Complete the table below to find the following limit. $\lim_{x \rightarrow 2} f(x)$ where $f(x) = \left(\frac{x^3 - 2x - 4}{x - 2} \right)$

x	1.9	1.99	1.999	2.001	2.01	2.1
$f(x)$						

- A. 9.7
 B. 9.8
 C. 9.9
 D. 10.0
 E. 10.1

- 14) Find the following limit.

$$\lim_{x \rightarrow -\infty} \left(\frac{2x^2 + 3x - 1}{3x^2 + 5} \right)$$

- A. $-\frac{2}{3}$
 B. $\frac{3}{2}$
 C. 0
 D. ∞
 E. None of the above.

- 15) Find the following limit.

$$\lim_{x \rightarrow 0} \left(\frac{\sqrt{x+9} - 3}{x} \right)$$

- A. 6
 B. 1
 C. $\frac{1}{6}$
 D. 0
 E. The limit does not exist.

- 16) Find an equation of the line tangent to $f(x) = 2x^2 - \sqrt{x} + 2$ at the point $(1, 3)$. Write the equation in standard form.
- A. $11x - 2y = 5$
B. $7x - 2y = 13$
C. $11x - 2y = 31$
D. $7x - 2y = 1$
E. $7x - 2y = -6$
- 17) The weekly profit function for a certain grain business is given by $P(x) = 10x + 15x^2$, where x is in pounds and profit P is in dollars. Find the average rate of change of profit in the interval $[6, 7]$. Find the marginal profit when x is 6 pounds. **How much greater** is the average rate of change in profit you found than the marginal profit at $x = 6$ pounds that you found?
- A. \$10
B. \$15
C. \$20
D. \$25
E. \$30