

MA 15400

Spring 2014

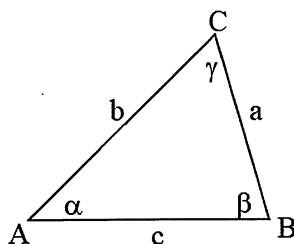
Exam 1

PYTHAGOREAN IDENTITIES:

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$



Solutions

1. Find the angle that is supplementary to $48^\circ 57' 9''$

$$\begin{array}{r}
 179^\circ 59' 60'' \\
 - 48^\circ 57' 9'' \\
 \hline
 131^\circ 2' 51''
 \end{array}$$

- A. $131^\circ 2' 51''$
- B. $41^\circ 52' 41''$
- C. $41^\circ 2' 51''$
- D. $131^\circ 52' 41''$
- E. None of the above

2. Express the angle $153^\circ 8' 36''$ as a decimal, to the nearest ten-thousandth of an angle.

$$\begin{array}{l}
 \frac{8'}{60} = 0.1333 \\
 \frac{36''}{3600} = 0.0100 \\
 \hline
 0.1433 \\
 153.1433^\circ
 \end{array}$$

- A. 153.6022°
- B. 153.1433°
- C. 153.4383°
- D. 153.7667°
- E. None of the above

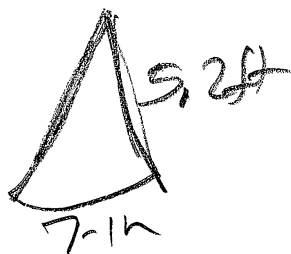
3. If a circular arc of the given length $s = 5.2$ km subtends the central angle $\theta = 76^\circ$ on a circle, find the radius of the circle. Round your answer to the nearest hundredth.

$$\begin{array}{l}
 s = r\theta \\
 5.2 = r \left(\frac{76^\circ \pi}{180^\circ} \right) \\
 5.2 = r(1.3265) \\
 \frac{5.2}{1.3265} = r \\
 r = 3.92
 \end{array}$$

- A. 9.95 km
- B. 3.17 km
- C. 12.32 km
- D. 3.92 km
- E. None of the above

4. A pendulum in a grandfather clock is 5.2 feet long and swings back and forth along a 7-inch arc. Approximate the angle through which the pendulum passes during one swing. Round your answer to the nearest tenth of a degree.

(1 foot = 12 inches)



$$S = r\theta$$

$$7 = (62.4)\theta$$

$$\frac{7}{62.4} = \theta$$

$$\theta = 0.112$$

$$\frac{5.2}{12} = 62.4 \text{ in}$$

$$\theta = 0.112 \left(\frac{180^\circ}{\pi} \right)$$

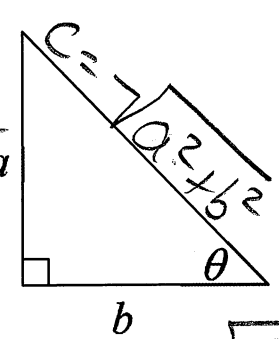
$$\theta = 6.4^\circ$$

- A. 6.4°
- B. 6.6°
- C. 6.2°
- D. 6.8°
- E. None of the above

5. Which one of the following statements is true for the given triangle?

$$\sin \theta = \frac{a}{\sqrt{a^2+b^2}}$$

$$\cos \theta = \frac{b}{\sqrt{a^2+b^2}}$$



$$c^2 = a^2 + b^2$$

$$c = \sqrt{a^2 + b^2}$$

$$\tan \theta = \frac{a}{b}$$

$$\csc \theta = \frac{\sqrt{a^2+b^2}}{a}$$

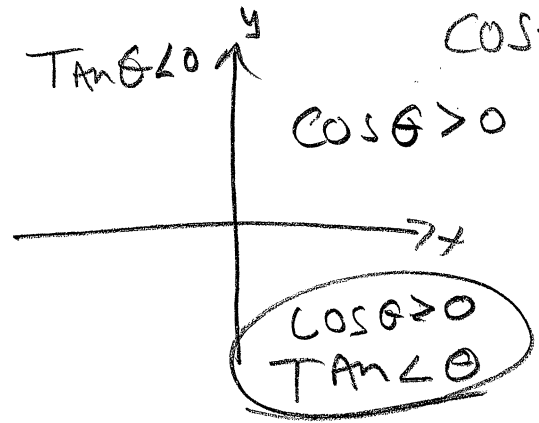
$$\sec \theta = \frac{\sqrt{a^2+b^2}}{b}$$

$$\cot \theta = \frac{b}{a}$$

- A. $\sec \theta = \frac{\sqrt{a^2+b^2}}{a}$ X
- B. $\csc \theta = \frac{\sqrt{a^2+b^2}}{b}$ X
- C. $\cos \theta = \frac{b}{\sqrt{a^2+b^2}}$ ✓
- D. $\sin \theta = \frac{b}{\sqrt{a^2+b^2}}$ X

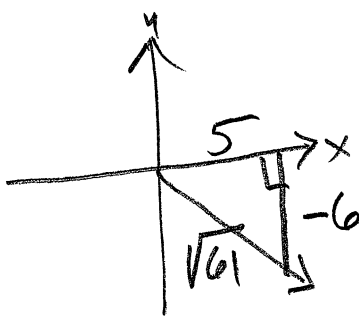
- E. More than one of the above answers are correct. X

6. Find the quadrant containing θ if $\sec \theta > 0$ and $\tan \theta < 0$.



- A. I
- B. II
- C. III
- D. IV
- E. None of the above

7. Find the exact value of $\sin(\theta)$ if θ is in standard position and the terminal side of θ is in QIV and is parallel to the line through $A(6,2)$ and $B(1,8)$.



$$m = \frac{8-2}{1-6} = \frac{6}{-5}$$

$$\tan \theta = -\frac{6}{5} = \frac{y}{x}$$

$$c^2 = 5^2 + 6^2$$

$$c = \sqrt{61}$$

$$\sin \theta = \frac{-6}{\sqrt{61}}$$

A. $\frac{-6}{\sqrt{61}}$

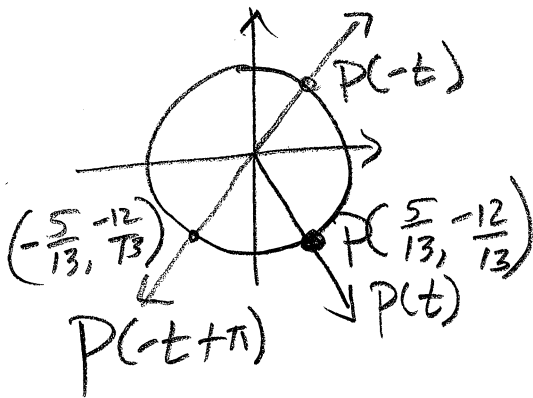
B. $\frac{5}{\sqrt{61}}$

C. $\frac{-5}{\sqrt{61}}$

D. $\frac{6}{\sqrt{61}}$

8. Let $P(t)$ be the point on the unit circle U that corresponds to t .

If $P(t) = \left(\frac{5}{13}, \frac{-12}{13}\right)$, find $P(-t + \pi)$



A. $\left(\frac{5}{13}, \frac{-12}{13}\right)$

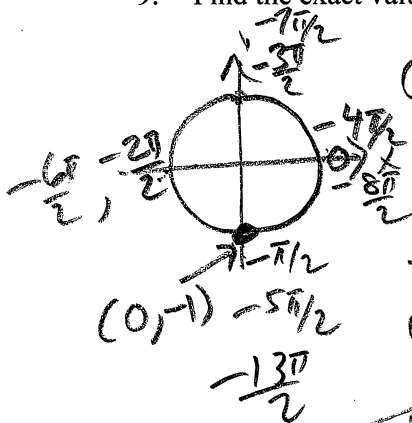
B. $\left(\frac{-5}{13}, \frac{-12}{13}\right)$

C. $\left(\frac{-5}{13}, \frac{12}{13}\right)$

D. $\left(\frac{5}{13}, \frac{12}{13}\right)$

E. None of the above

9. Find the exact value of $\sec\left(\frac{-13\pi}{2}\right)$



Count $-\frac{\pi}{2}$ 13 times
Starting At 0 And
going clockwise

$$\cos \frac{-13\pi}{2} = 0$$

$$\sec \frac{-13\pi}{2} = \text{undefined}$$

A. -2

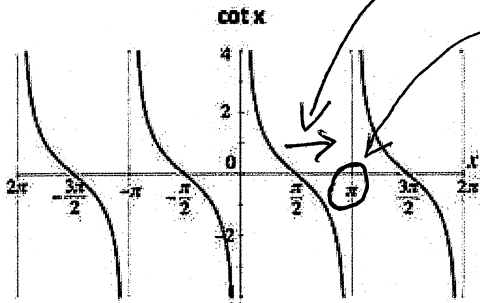
B. 1

C. 0

D. -1

E. None of the above

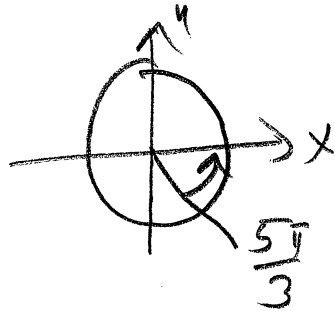
10. Use the graph to complete the statement: As $x \rightarrow \pi^-$ $\cot(x) \rightarrow$ _____



AS $x \rightarrow \pi$
 From the left, $\cot(x)$ is going towards $-\infty$

- A. $-\infty$
- B. 0
- C. 1
- D. ∞
- E. None of the above

11. Find the reference angle θ_r if $\theta = \frac{5\pi}{3}$



$$\begin{aligned} \theta_r &= 2\pi - \frac{5\pi}{3} \\ &= \frac{6\pi}{3} - \frac{5\pi}{3} \\ &= \frac{\pi}{3} \end{aligned}$$

A. $\theta_r = \frac{2\pi}{3}$

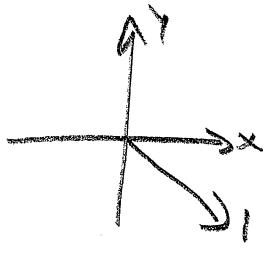
B. $\theta_r = \frac{-\pi}{3}$

C. $\theta_r = \frac{4\pi}{3}$

D. $\theta_r = \frac{\pi}{3}$

E. None of the above

12. Find the exact value of $\cos\left(\frac{11\pi}{6}\right)$.



$$\begin{aligned} \theta_r &= \frac{\pi}{6} \\ \cos \frac{\pi}{6} &= \frac{\sqrt{3}}{2} \\ \cos \frac{11\pi}{6} &= \frac{\sqrt{3}}{2} \end{aligned}$$

A. $\frac{-1}{2}$

B. $\frac{\sqrt{3}}{2}$

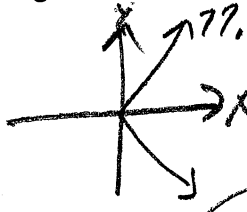
C. $\frac{1}{2}$

D. $\frac{-\sqrt{3}}{2}$

E. None of the above

13. Approximate, to the nearest 0.1°, all angles θ in the interval $[0^\circ, 360^\circ)$ that satisfy the equation $\sec \theta = 4.5387$.

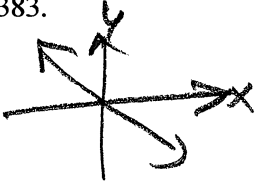
$\frac{1}{\sec \theta} = \frac{1}{4.5387}$
 $\cos \theta = 0.2203$
 $\theta = \cos^{-1}(0.2203)$
 $\theta_1 = 77.3^\circ$
 $\theta_2 = 360^\circ - 77.3^\circ$
 $\theta_2 = 282.7^\circ$



A. $\theta = 77.3^\circ, 102.7^\circ$
 B. $\theta = 12.7^\circ, 167.3^\circ$
 C. $\theta = 77.3^\circ, 282.7^\circ$
 D. $\theta = 12.7^\circ, 347.3^\circ$
 E. None of the above

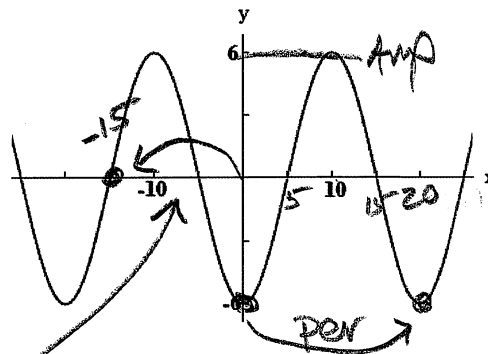
14. Approximate, to the nearest 0.0001 radians, all angles θ in the interval $[0, 2\pi)$ that satisfy equation $\tan \theta = -1.0383$.

$\theta = \tan^{-1}(-1.0383)$
 $\theta = -0.8042$
 $\theta_R = 0.8042$
 $\theta_1 = \pi - 0.8042$
 $\theta_2 = 2\pi - 0.8042$
 $\theta_1 = 2.3374$
 $\theta_2 = 5.4790$



A. $\theta = 2.3374, 3.9458$
 B. $\theta = 0.8042, 3.9458$
 C. $\theta = 0.8042, 5.4790$
 D. $\theta = 2.3374, 5.4790$
 E. None of the above

Use the graph of the sine function to answer Questions 15, 16, and 17.



15. Find the amplitude

- A. 6
- B. -12
- C. 12
- D. -6

16. Find the period

- A. 10
- B. 15
- C. 20
- D. 5

17. Find the Phase Shift

- A. -5
- B. -15
- C. -10
- D. -20

Question	Answers	
1.	A	$131^{\circ}2'51''$
2.	B	153.1433°
3.	D	3.92 km
4.	A	6.4°
5.	C	$\cos \theta = \frac{b}{\sqrt{a^2 + b^2}}$
6.	D	IV
7.	A	$\frac{-6}{\sqrt{61}}$
8.	B	$\left(\frac{-5}{13}, \frac{-12}{13}\right)$
9.	E	Undefined
10.	A	$-\infty$
11.	D	$\theta_R = \frac{\pi}{3}$
12.	B	$\frac{\sqrt{3}}{2}$
13.	C	$\theta = 77.3^{\circ}, 282.7^{\circ}$
14.	D	$\theta = 2.3374, 5.4790$
15.	A	6
16.	C	20
17.	B	-15