Problem No. 5 (Fall 2003 Series)

The triangle \( \triangle \) has angles \( \alpha, \beta, \gamma \) opposite respectively to the sides \( a, b, c \). Show that \( \triangle \) is equilateral if and only if

\[
ab \cos \gamma = ac \cos \beta = bc \cos \alpha.
\]