Problem No. 5 (Spring 2010 Series)

Let $R$ be a given positive real number, and $k$ any fixed positive integer. Show that there are at most finitely many $k$-tuples of positive integers $a_1, \ldots, a_k$ such that

$$R = \frac{1}{a_1} + \cdots + \frac{1}{a_k}.$$