

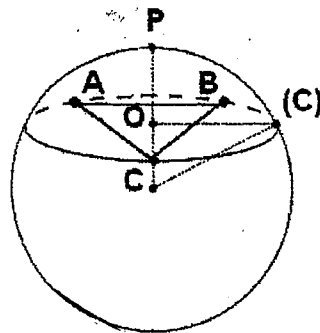
PROBLEM OF THE WEEK

Solution of Problem No. 9 (Spring 2012 Series)

Problem: Prove there is no distance preserving map from a spherical cap to the plane.

Solution: (by Hubert Desprez, Paris, France)

Let $\varphi : \pi \rightarrow \pi'$ such a map, and (C) a circle as boundary of cap of sphere, and (ABC) an equilateral triangle in (C) .



$OA = OB = OC$ and $PA = PB = PC$ imply that O' and P' are both circumcenters of triangle $A'B'C'$: a contradiction with $O'P' = OP > 0$, so there is no such φ .

The problem was also solved by:

Undergraduates: Kaibo Gong (Sr. Math)

Graduates: Dat Tran (Math), Yu Tsumura (Math), Tairan Yuwen (Chemistry)

Others: Manuel Barbero (New York), Gruian Cornel (Cluj-Napoca, Romania), Tom Engelsman (Tampa, FL), Talal Al Fares (Hasbaya, Nabatieh, Lebanon), Elie Ghosn (Montreal, Quebec), Steven Landy (Physics Faculty, IUPUI), Sorin Rubinstein (TAU faculty, Israel), Steve Spindler (Chicago)