

## **Undergraduate Research Project**

| Project Name:             | Topology and Social Choice: From Arrow's Theorem to Recent Advances  | Number of Positions: | 1-2 |
|---------------------------|--|----------------------|-----|
| Supervisor:               | Sam Nariman  |                      |     |
| Supervisor e-mail:        | snariman@purdue.edu  |                      |     |
| Project Description:      | This project explores the intersection of topology and social choice theory.<br>Arrow's impossibility theorem is a cornerstone result showing that no voting<br>system can satisfy certain fairness criteria simultaneously. There are topological<br>proofs using combinatorial geometry that revealed new insights into these<br>theorems. One part of the project introduces students to these topological<br>methods.<br>The project will also study a recent result by Moses Charikar and collaborators on<br>appeasing the majority by shortlisting a committee with the minimum number of<br>members. These approaches blend tools from geometry, topology, probability and<br>combinatorics. |                      |     |
| Final Deliverables:       | A carefully written exposition accessible to advanced undergraduates, and a short seminar talk. Optional: A simple simulation or visualization of voting paradoxes.  |                      |     |
| Weekly Working<br>Hours   | 6-8 hours  |                      |     |
| For Credits/<br>Voluntary | Either   |                      |     |
| Desired<br>Qualifications | Required: Linear algebra, Topology, discrete math<br>Preferred: Probability  |                      |     |

If you are interested in participating in this research project, please send an e-mail to the supervisor e-mail listed above together with a resume, a list of what courses you've taken or a copy of your transcript, and a personal statement explaining why you are interested in this project.