

MATH 181, Exam II

(40) **1.** Compute the following integrals.

a) $\int \frac{2x+7}{x^2-3x-4} dx$ (Partial fractions: $x^2-3x-4 = (x+1)(x-4)$)

b) $\int \frac{2x+7}{x^2-2x+5} dx$ (Complete the square: $x^2-2x+5 = (x-1)^2+4$)

c) $\int 2x \ln(x+2) dx$ (Integration by parts)

d) Use the method of Trigonometric Substitution to reduce $\int \frac{(4-x^2)^{3/2}}{x^6} dx$ to an integral involving trigonometric functions. Do not compute the trigonometric integral.

(20) **2.** Find the solution to

$$\frac{dy}{dx} = 2x\sqrt{y^2+1}$$

that satisfies the initial condition $y(0) = 0$.

(20) **3.** Compute the limits,

a) $\lim_{x \rightarrow 0^+} x(\ln x)^2$.

b) $\lim_{x \rightarrow \infty} (\ln x)^{(1/x)}$ (Hint: Take \ln and use L'Hôpital's Rule.)

(10) **4.** Suppose the temperature of a hot rock is given by

$$T(t) = 200e^{-kt}.$$

If the temperature at time $t = 1$ is $T = 100$, what is the temperature at time $t = 3$?

(10) **5.** Show that, if $x > 0$, then

$$x^{(2x)} = (x^2)^x.$$