

p. 528; 3. $f(x) = \begin{cases} K & 0 < x < b \\ 0 & \text{otherwise} \end{cases}$

$$\hat{f}(\omega) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} f(x) e^{-i\omega x} dx =$$

$$= \frac{1}{\sqrt{2\pi}} \int_0^b K e^{-i\omega x} dx$$

$$= \frac{K}{\sqrt{2\pi}} \left[\frac{1}{-i\omega} e^{-i\omega x} \right]_{x=0}^b$$

$$= \frac{K}{\sqrt{2\pi}} \left[\frac{e^{-i\omega b}}{-i\omega} - \left(\frac{1}{-i\omega} \right) \right]$$

$$= \frac{K}{i\omega \sqrt{2\pi}} \left(1 - e^{-i\omega b} \right)$$