## **Related Rates I**

## Strategy

- 1. Read the problem carefully; underline given numerical information.
- 2. Draw a diagram.
- 3. Assign variables to functions of time (what changes with respect to time?).
- 4. In terms of your variables, write out what you know and what you want to find.
- 5. Relate what we know and what we want to find using an equation with the variables assigned in step 3.
- 6. Use implicit differentiation to differentiate both sides of the equation with respect to time, t.
- 7. Substitute the given information and solve for the rate we want to find. Do not substitute too early!

Recall that rates of change correspond to derivatives of functions.

Example 1: The radius of a spherical balloon is increasing at a rate of 5 mm/s. How fast is the volume increasing when the radius is 50 mm? Note that the volume of a sphere is given by  $V = \frac{4}{3}\pi r^3$ , where r is the radius of the sphere.

Example 2: The length of a rectangle is decreasing at a rate of 3 in/s and its width is decreasing at a rate of 2 in/s. When the length is 10 in and the width is 8 in, how fast is the area of the rectangle decreasing?

Example 3: Gravel is dumped out of a dump truck onto the ground at 4 ft<sup>3</sup>/s, forming a conical pile whose base diameter is always equal to its height. How fast is the height of the pile increasing when the pile is 5 ft high? Note that the volume of a cone is  $V = \frac{1}{3}\pi r^2 h$ , where r is the radius of the base and h is the height of the cone.