Curve Sketching

We have seen how limits and derivatives can give us information about what the graph of a function looks like: where it has asymptotes, extrema, where it is increasing/decrasing, concave up/concave down, etc.. Now we are going to put all this information together to sketch the graph of a function.

Strategy

- 1. Find any x- and y-intercepts of the function.
- 2. Find the intervals on which the function is increasing and the intervals on which it is decreasing.
- 3. Find any relative extrema for the function.
- 4. Find the intervals on which the function is concave up and the intervals on which it is concave down.
- 5. Find any inflection points.
- 6. Find any asymptotes for the function.
- 7. Use the information in steps 1-6 to sketch a graph of the function.

Example 1: Use the strategy above to sketch a graph of $f(x) = \frac{2x^2}{x+1}$.



DIY

- 1. Use the following information to sketch a graph of f(x).
 - The point (-2, 0) is on the graph of f.
 - f has a horizontal asymptote at y = 0, vertical asymptotes at $x = \pm 1$, and no slant asymptotes.
 - f'(x) > 0 on the intervals $(-\infty, -1)$ and (-1, 0).
 - f'(x) < 0 on the intervals (0, 1) and $(1, \infty)$.
 - f''(x) > 0 on the intervals $(-\infty, -1)$ and $(1, \infty)$.
 - f''(x) < 0 on the interval (-1, 1).

