## Definite Integrals I

We have seen how to approximate the (signed) area under a curve using left and right Riemann sums. As we increase the number of rectangles used, the estimate gets closer to the actual area. If we let the number of rectangles $(n)$ approach infinity (take the limit as $n \rightarrow \infty$ ), then we get the exact area between the curve and the $x$-axis. We denote the exact area between the curve and the $x$-axis using a definite integral:

$$
\int_{a}^{b} f(x) d x
$$

This definite integral is equal to the area between the curve $f(x)$ and the $x$-axis on the interval $[a, b]$. We call $a$ the lower limit of integration, $b$ the upper limit of integration, and $f(x)$ the integrand. The $d x$ tells us to take the integral (antiderivative) with respect to the variable $x$.

Geometric Interpretation: Definite Integral of a function $=$ area between the graph of the function and the $x$-axis.

Example 1: Evaluate $\int_{2}^{5} 2 d x$ by using geometric formulas.

Example 2: Evaluate $\int_{-2}^{4} 3 x d x$ by using geometric formulas.

Example 3: Write an integral that represents the shaded area.


## DIY

1. Write an integral that represents the shaded area.

2. Evaluate $\int_{4}^{6} \frac{1}{2} x d x$ by using geometric formulas. Recall that the area of a trapezoid is $A=\frac{1}{2}$ (base $1+$ base 2 ) (height).
