Lecture 14: Reinforcement Learning

Adapted from http://cs231n.stanford.edu/slides/2018/cs231n_2018_lecture14.pdf for Purdue MA 598, Spring 2019

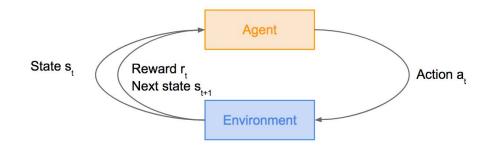
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Today: Reinforcement Learning

Problems involving an **agent** interacting with an **environment**, which provides numeric **reward** signals

Goal: Learn how to take actions in order to maximize reward



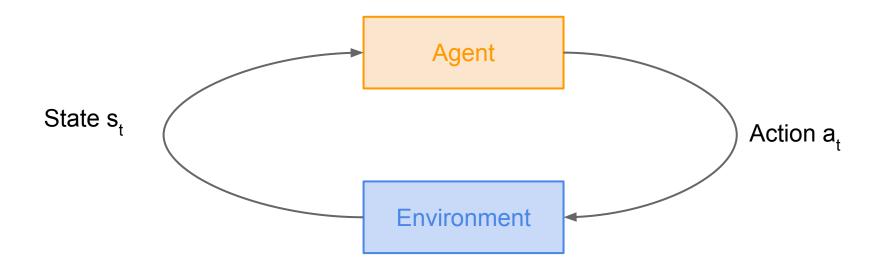


Atari games figure copyright Volodymyr Mnih et al., 2013. Reproduced with permission.

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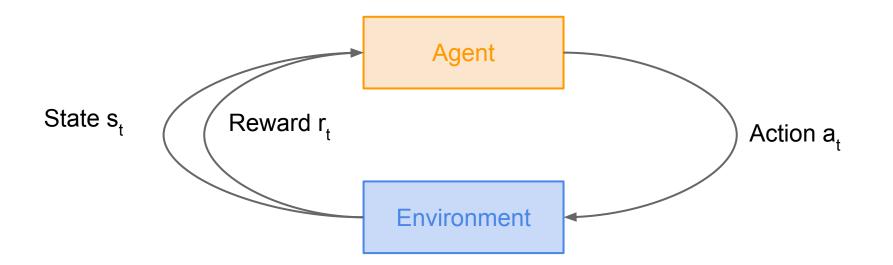
Reinforcement Learning



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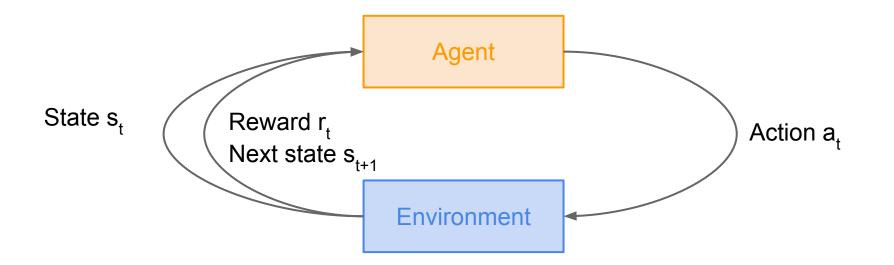
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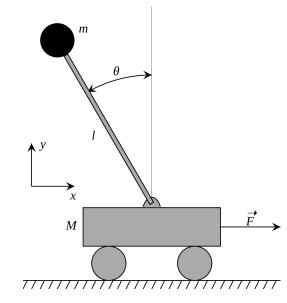
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Cart-Pole Problem



Objective: Balance a pole on top of a movable cart

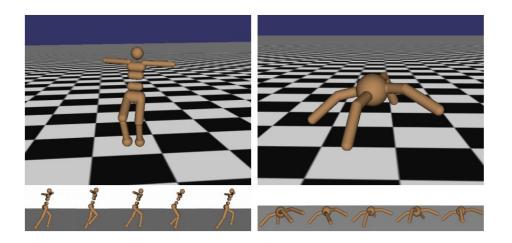
State: angle, angular speed, position, horizontal velocityAction: horizontal force applied on the cartReward: 1 at each time step if the pole is upright

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Robot Locomotion



Objective: Make the robot move forward

State: Angle and position of the joints Action: Torques applied on joints Reward: 1 at each time step upright + forward movement

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Atari Games



Objective: Complete the game with the highest score

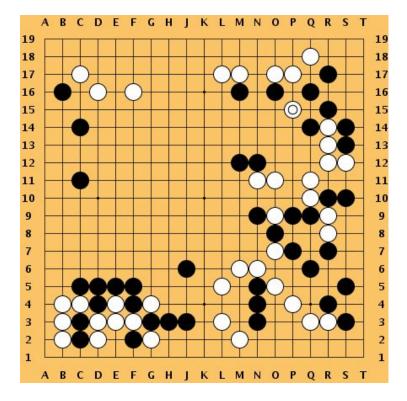
State: Raw pixel inputs of the game state **Action:** Game controls e.g. Left, Right, Up, Down **Reward:** Score increase/decrease at each time step

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Go



Objective: Win the game!

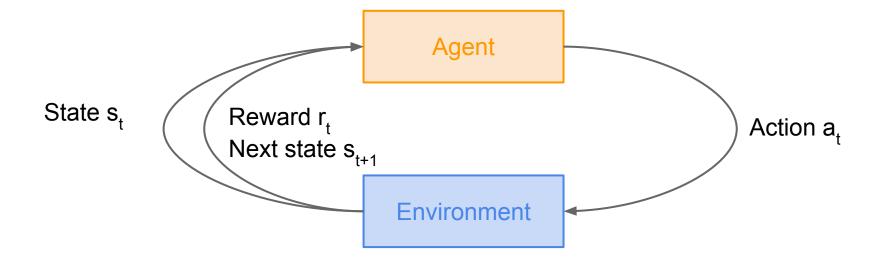
State: Position of all piecesAction: Where to put the next piece downReward: 1 if win at the end of the game, 0 otherwise

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How can we mathematically formalize the RL problem?



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Markov Decision Process

- Mathematical formulation of the RL problem
- Markov property: Current state completely characterises the state of the world

Defined by: $(\mathcal{S}, \mathcal{A}, \mathcal{R}, \mathbb{P}, \gamma)$

- ${\cal S}$: set of possible states
- \mathcal{A} : set of possible actions
- ${\cal R}\,$: distribution of reward given (state, action) pair
- ℙ : transition probability i.e. distribution over next state given (state, action) pair
- γ : discount factor

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Markov Decision Process

- At time step t=0, environment samples initial state $s_0 \sim p(s_0)$
- Then, for t=0 until done:
 - Agent selects action a,
 - Environment samples reward $r_t \sim R(. | s_t, a_t)$
 - Environment samples next state $s_{t+1} \sim P(.|s_t, a_t)$
 - Agent receives reward r, and next state s, +1

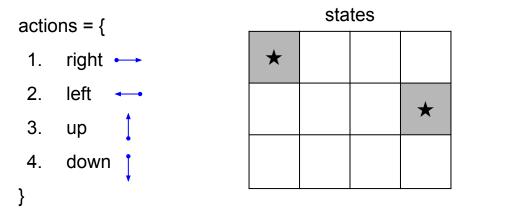
- A policy π is a function from S to A that specifies what action to take in each state
- **Objective**: find policy $\mathbf{\pi}^*$ that maximizes cumulative discounted reward: $\sum \gamma^t r_t$



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A simple MDP: Grid World



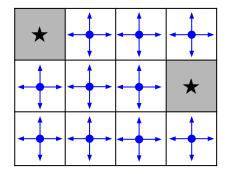
Set a negative "reward" for each transition (e.g. r = -1)

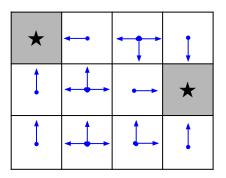
Objective: reach one of terminal states (greyed out) in least number of actions

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A simple MDP: Grid World





Random Policy

Optimal Policy

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The optimal policy π^*

We want to find optimal policy π^* that maximizes the sum of rewards.

How do we handle the randomness (initial state, transition probability...)?

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The optimal policy π^*

We want to find optimal policy π^* that maximizes the sum of rewards.

How do we handle the randomness (initial state, transition probability...)? Maximize the **expected sum of rewards!**

Formally:
$$\pi^* = \arg \max_{\pi} \mathbb{E}\left[\sum_{t \ge 0} \gamma^t r_t | \pi\right]$$
 with $s_0 \sim p(s_0), a_t \sim \pi(\cdot | s_t), s_{t+1} \sim p(\cdot | s_t, a_t)$

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Definitions: Value function and Q-value function

Following a policy produces sample trajectories (or paths) s_0 , a_0 , r_0 , s_1 , a_1 , r_1 , ...

How good is a state?

The **value function** at state s, is the expected cumulative reward from following the policy from state s: $V^{\pi}(s) = \mathbb{E}\left[\sum \gamma^{t} r_{t} | s_{0} = s, \pi\right]$

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$$V^{\pi}(s) = \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | s_0 = s, \pi
ight]$$

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Definitions: Value function and Q-value function

Following a policy produces sample trajectories (or paths) s₀, a₀, r₀, s₁, a₁, r₁, ...

How good is a state?

The **value function** at state s, is the expected cumulative reward from following the policy from state s: $V^{\pi}(a) = \mathbb{E} \left[\sum_{n} e^{t} n | a = a \pi \right]$

$$V^{\pi}(s) = \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | s_0 = s, \pi
ight]$$

How good is a state-action pair?

The **Q-value function** at state s and action a, is the expected cumulative reward from taking action a in state s and then following the policy:

$$Q^{\pi}(s,a) = \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | s_0 = s, a_0 = a, \pi
ight]$$

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Bellman equation

The optimal Q-value function Q* is the maximum expected cumulative reward achievable from a given (state, action) pair:

$$Q^*(s,a) = \max_{\pi} \mathbb{E}\left[\sum_{t \ge 0} \gamma^t r_t | s_0 = s, a_0 = a, \pi
ight]$$

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Bellman equation

The optimal Q-value function Q* is the maximum expected cumulative reward achievable from a given (state, action) pair:

$$Q^*(s,a) = \max_{\pi} \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | s_0 = s, a_0 = a, \pi
ight]$$

Q* satisfies the following **Bellman equation**:

$$Q^*(s,a) = \mathbb{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q^*(s',a') | s, a \right]$$

Intuition: if the optimal state-action values for the next time-step Q*(s',a') are known, then the optimal strategy is to take the action that maximizes the expected value of $r + \gamma Q^*(s',a')$

I.e., we can reduce the problem to taking one step plus knowing the solution after that step. This yields an iterative approach.

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Bellman equation

The optimal Q-value function Q* is the maximum expected cumulative reward achievable from a given (state, action) pair:

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Intuition: if the optimal state-action values for the next time-step Q*(s',a') are known, then the optimal strategy is to take the action that maximizes the expected value of $r + \gamma Q^*(s',a')$

The optimal policy π^* corresponds to taking the best action in any state as specified by Q^{*}

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Value iteration algorithm: Use Bellman equation as an iterative update

$$Q_{i+1}(s,a) = \mathbb{E}\left[r + \gamma \max_{a'} Q_i(s',a')|s,a\right]$$

 Q_i will converge to Q^* as i -> infinity

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Value iteration algorithm: Use Bellman equation as an iterative update

$$Q_{i+1}(s,a) = \mathbb{E}\left[r + \gamma \max_{a'} Q_i(s',a')|s,a\right]$$

 Q_i will converge to Q^* as i -> infinity

(the map is a contraction because the discount factor is less than 1)

What's the problem with this?

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Value iteration algorithm: Use Bellman equation as an iterative update

$$Q_{i+1}(s,a) = \mathbb{E}\left[r + \gamma \max_{a'} Q_i(s',a')|s,a\right]$$

 Q_i will converge to Q^* as i -> infinity

What's the problem with this?

Not scalable. Must compute Q(s,a) for every state-action pair. If state is e.g. current game state pixels, computationally infeasible to compute for entire state space!

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Value iteration algorithm: Use Bellman equation as an iterative update

$$Q_{i+1}(s,a) = \mathbb{E}\left[r + \gamma \max_{a'} Q_i(s',a')|s,a\right]$$

 Q_i will converge to Q^* as i -> infinity

What's the problem with this?

Not scalable. Must compute Q(s,a) for every state-action pair. If state is e.g. current game state pixels, computationally infeasible to compute for entire state space!

Solution: use a function approximator to estimate Q(s,a). E.g. a neural network!

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Q-learning: Use a function approximator to estimate the action-value function

$$Q(s, a; \theta) \approx Q^*(s, a)$$

function parameters (weights)

If the function approximator is a deep neural network => deep q-learning!

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Remember: want to find a Q-function that satisfies the Bellman Equation:

$$Q^*(s,a) = \mathbb{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q^*(s',a') | s, a \right]$$

Forward Pass

Loss function: $L_i(\theta_i) = \mathbb{E}_{s,a \sim \rho(\cdot)} \left[(y_i - Q(s,a;\theta_i))^2 \right]$ where $y_i = \mathbb{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q(s',a';\theta_{i-1}) | s, a \right]$

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Remember: want to find a Q-function that satisfies the Bellman Equation:

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where $y_i = \mathbb{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q(s',a';\theta_{i-1}) | s, a \right]$

Backward Pass

Gradient update (with respect to Q-function parameters θ):

$$-\nabla_{\theta_i} L_i(\theta_i) = 2\mathbb{E}_{s,a \sim \rho(\cdot); s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q(s',a';\theta_{i-1}) - Q(s,a;\theta_i) \right] \nabla_{\theta_i} Q(s,a;\theta_i)$$

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Remember: want to find a Q-function that satisfies the Bellman Equation:

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where
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Backward Pass

Gradient update (with respect to Q-function parameters θ):

Iteratively try to make the Q-value close to the target value (y_i) it should have, if Q-function corresponds to optimal Q* (and optimal policy π*)

$$-\nabla_{\theta_i} L_i(\theta_i) = 2\mathbb{E}_{s,a \sim \rho(\cdot); s' \sim \mathcal{E}} \left[(r + \gamma \max_{a'} Q(s',a';\theta_{i-1}) - Q(s,a;\theta_i)) \nabla_{\theta_i} Q(s,a;\theta_i) \right]$$

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[Mnih et al. NIPS Workshop 2013; Nature 2015]

Case Study: Playing Atari Games



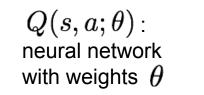
Objective: Complete the game with the highest score

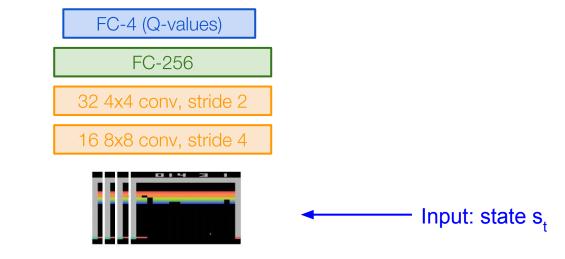
State: Raw pixel inputs of the game state **Action:** Game controls e.g. Left, Right, Up, Down **Reward:** Score increase/decrease at each time step

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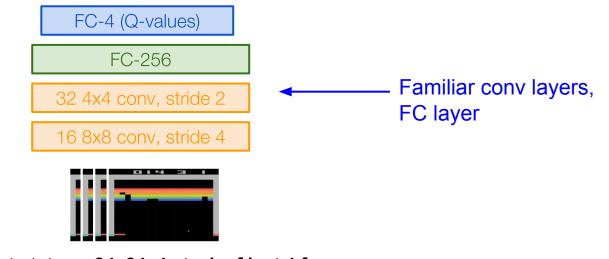


Current state s_t: 84x84x4 stack of last 4 frames (after RGB->grayscale conversion, downsampling, and cropping)

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Q(s,a; heta): neural network with weights heta

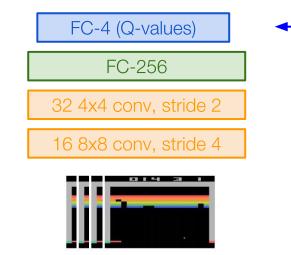


Current state s_t: 84x84x4 stack of last 4 frames (after RGB->grayscale conversion, downsampling, and cropping)

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Q(s,a; heta) : neural network with weights heta



Last FC layer has 4-d output (if 4 actions), corresponding to $Q(s_t, a_1)$, $Q(s_t, a_2)$, $Q(s_t, a_3)$, $Q(s_t, a_4)$

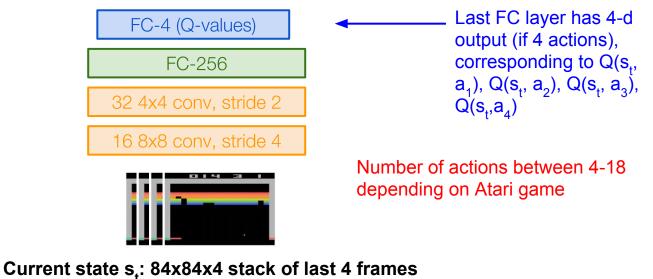
Action: Game controls e.g. Left, Right, Up, Down

Current state s_t: 84x84x4 stack of last 4 frames (after RGB->grayscale conversion, downsampling, and cropping)

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Q(s,a; heta) : neural network with weights heta



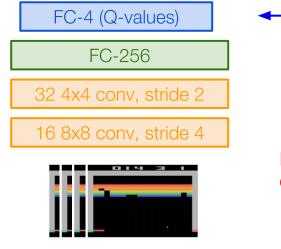
(after RGB->grayscale conversion, downsampling, and cropping)

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Q(s,a; heta): neural network with weights heta

A single feedforward pass to compute Q-values for all actions from the current state => efficient!



Last FC layer has 4-d output (if 4 actions), corresponding to Q(s_t, a₁), Q(s_t, a₂), Q(s_t, a₃), Q(s_t, a₄)

Number of actions between 4-18 depending on Atari game

Current state s_t: 84x84x4 stack of last 4 frames (after RGB->grayscale conversion, downsampling, and cropping)

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Training the Q-network: Loss function (from before)

Remember: want to find a Q-function that satisfies the Bellman Equation:

$$Q^*(s,a) = \mathbb{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q^*(s',a') | s, a \right]$$

Forward Pass

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Loss function:
$$L_i(\theta_i) = \mathbb{E}_{s,a \sim \rho(\cdot)} \left[(y_i - Q(s,a;\theta_i))^2 \right]$$

where
$$y_i = \mathbb{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q(s', a'; \theta_{i-1}) | s, a \right]$$

Backward Pass

Gradient update (with respect to Q-function parameters θ):

Iteratively try to make the Q-value
close to the target value
$$(y_i)$$
 it
should have, if Q-function
corresponds to optimal Q* (and
optimal policy π^*)

$$-\nabla_{\theta_i} L_i(\theta_i) = 2\mathbb{E}_{s,a \sim \rho(\cdot); s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q(s',a';\theta_{i-1}) - Q(s,a;\theta_i) \right] \nabla_{\theta_i} Q(s,a;\theta_i)$$

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Training the Q-network: Experience Replay

Learning from batches of consecutive samples is problematic:

- Samples are correlated => inefficient learning
- Current Q-network parameters determines next training samples (e.g. if maximizing action is to move left, training samples will be dominated by samples from left-hand size) => can lead to bad feedback loops

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Training the Q-network: Experience Replay

Learning from batches of consecutive samples is problematic:

- Samples are correlated => inefficient learning
- Current Q-network parameters determines next training samples (e.g. if maximizing action is to move left, training samples will be dominated by samples from left-hand size) => can lead to bad feedback loops

Address these problems using **experience replay**

- Continually update a **replay memory** table of transitions (s_t, a_t, r_t, s_{t+1}) as game (experience) episodes are played
- Train Q-network on random minibatches of transitions from the replay memory, instead of consecutive samples

Each transition can also contribute to multiple weight updates => greater data efficiency

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Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory \mathcal{D} to capacity N Initialize replay memory, Q-network Initialize action-value function Q with random weights for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ for t = 1, T do With probability ϵ select a random action a_t otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ Execute action a_t in emulator and observe reward r_t and image x_{t+1} Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D} Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from \mathcal{D} Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3 end for end for

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Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory \mathcal{D} to capacity N Initialize action-value function Q with random weights ——— Play M episodes (full games) for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ for t = 1, T do With probability ϵ select a random action a_t otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ Execute action a_t in emulator and observe reward r_t and image x_{t+1} Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D} Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from \mathcal{D} Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3 end for end for

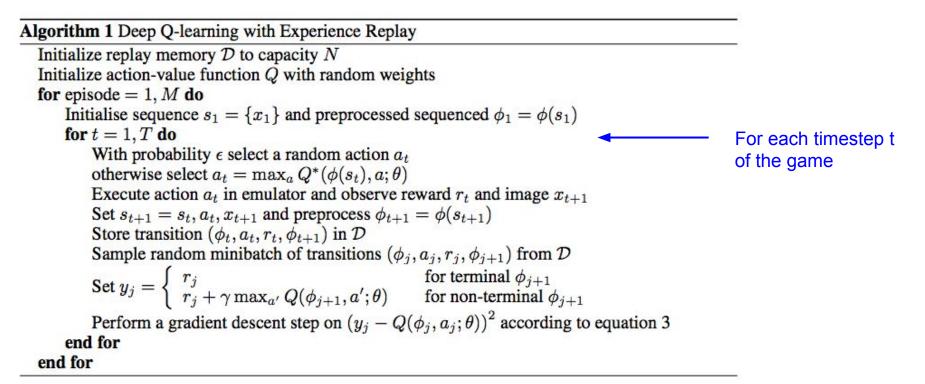
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Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory \mathcal{D} to capacity N Initialize action-value function Q with random weights for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ Initialize state for t = 1, T do (starting game With probability ϵ select a random action a_t screen pixels) at the otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ beginning of each Execute action a_t in emulator and observe reward r_t and image x_{t+1} episode Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D} Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from \mathcal{D} Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3 end for end for

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Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory \mathcal{D} to capacity N Initialize action-value function Q with random weights for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ for t = 1, T do With probability ϵ select a random action a_t With small probability, otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ select a random Execute action a_t in emulator and observe reward r_t and image x_{t+1} action (explore), Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ otherwise select Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D} greedy action from Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from \mathcal{D} current policy Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3 end for end for

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Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory \mathcal{D} to capacity N Initialize action-value function Q with random weights for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ for t = 1, T do With probability ϵ select a random action a_t otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ Execute action a_t in emulator and observe reward r_t and image x_{t+1} Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ Take the action $(a_{,})$, and observe the Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D} Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from \mathcal{D} reward r, and next Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ state s₊₊₁ Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3 end for end for

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Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory \mathcal{D} to capacity N Initialize action-value function Q with random weights for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ for t = 1, T do With probability ϵ select a random action a_t otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ Execute action a_t in emulator and observe reward r_t and image x_{t+1} Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ Store transition in Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D} replay memory Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from \mathcal{D} Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3 end for end for

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Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory \mathcal{D} to capacity N Initialize action-value function Q with random weights for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ for t = 1, T do With probability ϵ select a random action a_t otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ Execute action a_t in emulator and observe reward r_t and image x_{t+1} Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D} Experience Replay: Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from \mathcal{D} Sample a random Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ minibatch of transitions from replay memory Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3 and perform a gradient end for descent step end for

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https://www.youtube.com/watch?v=V1eYniJ0Rnk

Another one: https://youtu.be/yxMWqmFu538

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