

$$\text{Let } f(x) = \begin{cases} 1 & \text{if } x \text{ is rational} \\ 0 & \text{if } x \text{ is irrational} \end{cases}$$

$$\text{Let } P = \{x_0 < x_1 < x_2 < \dots < x_N\}$$

where  $x_0 = a$  and  $x_N = b$ .

For each interval ~~the~~

$(x_j, x_{j+1})$ , what is

$M_j$ ,

and what is

$m_j$ ?

What is  $\sum_{j=0}^{N-1} (x_j - x_{j-1})$  ?

(telescoping).

What is  $U(f, P)$ ? and

what is  $L(f, P)$  ?